

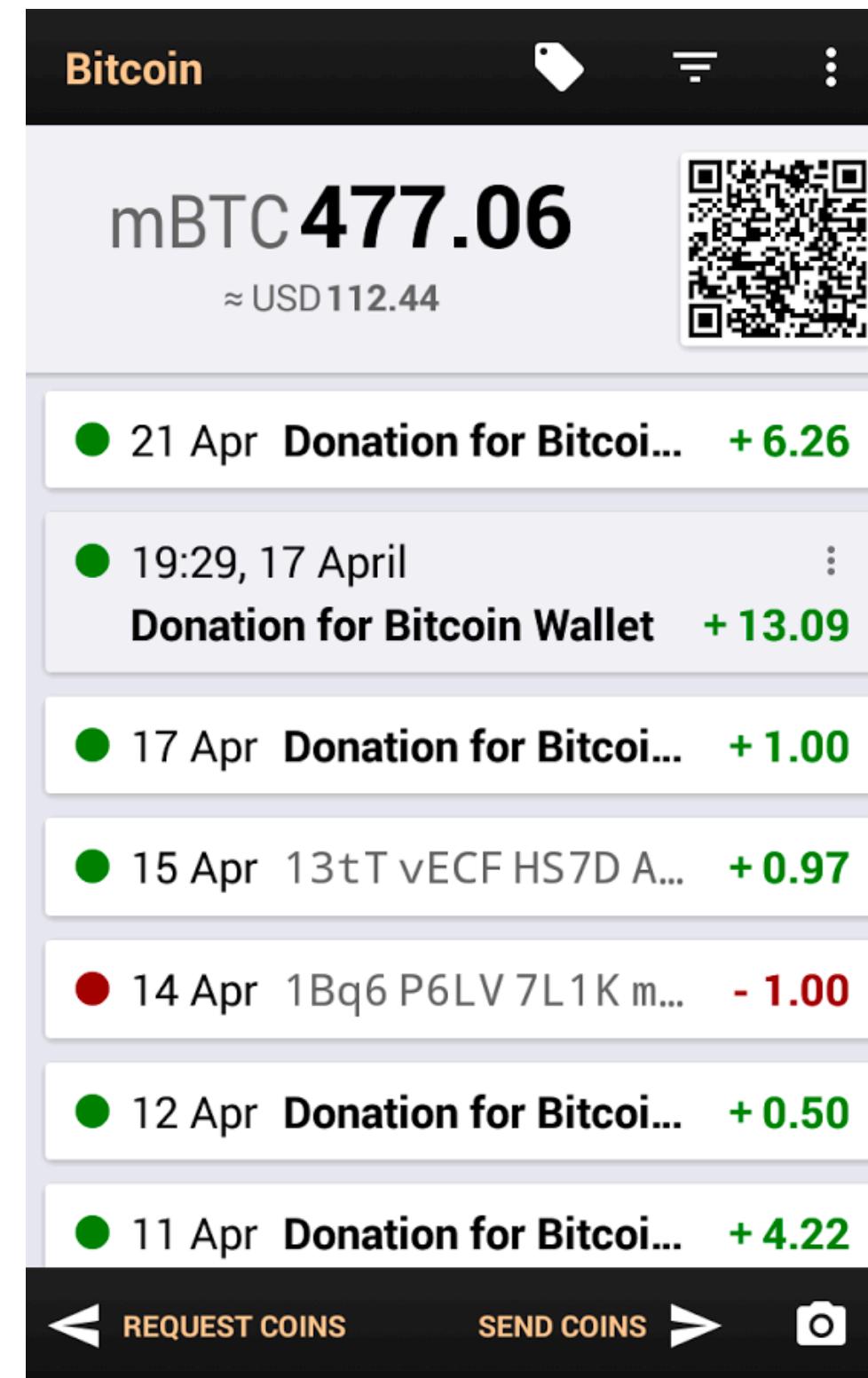


# Applying Private Information Retrieval to Lightweight Bitcoin Clients

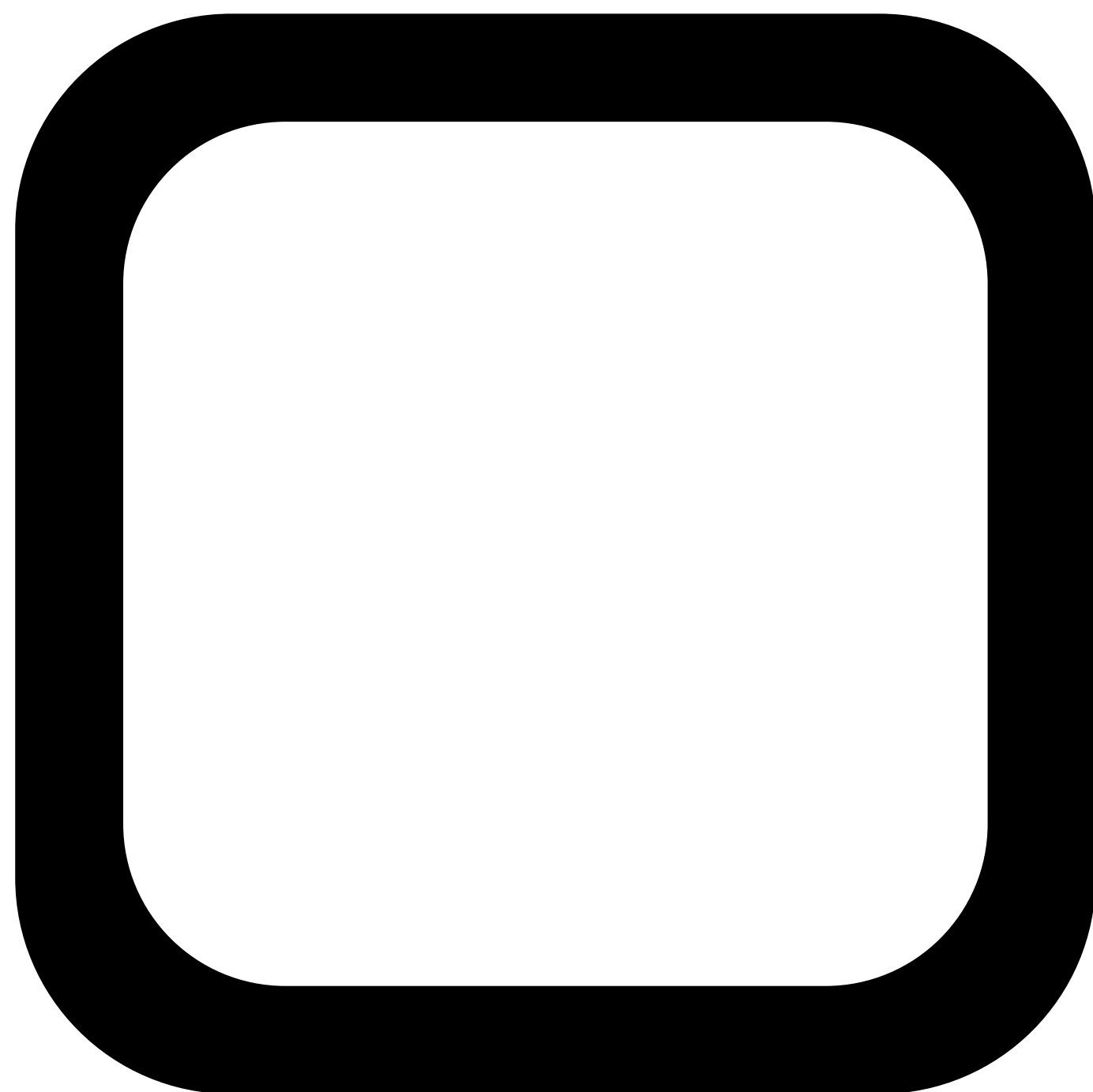
Kaihua Qin, Henryk Hadass, [Arthur Gervais](#) and Joel Reardon



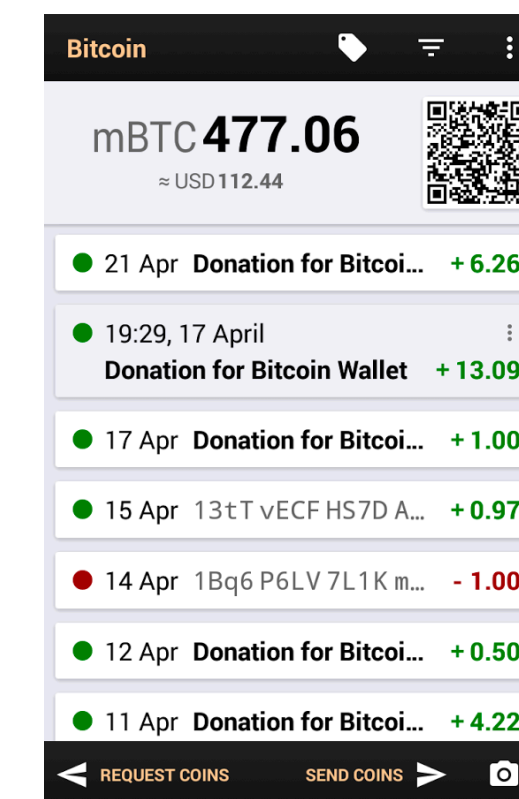
# Bitcoin SPV Clients



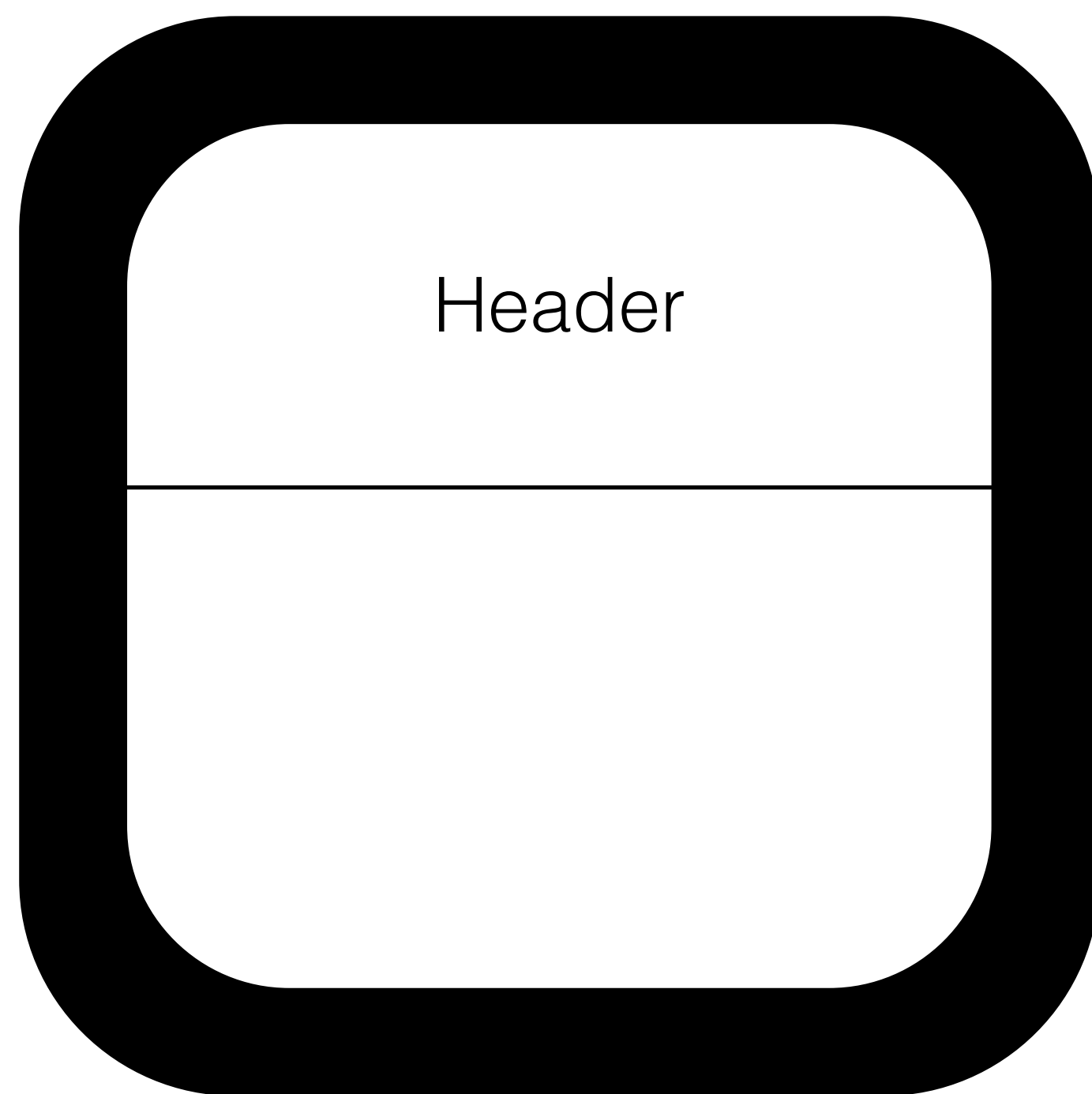
# Simple Payment Verification (SPV) Clients



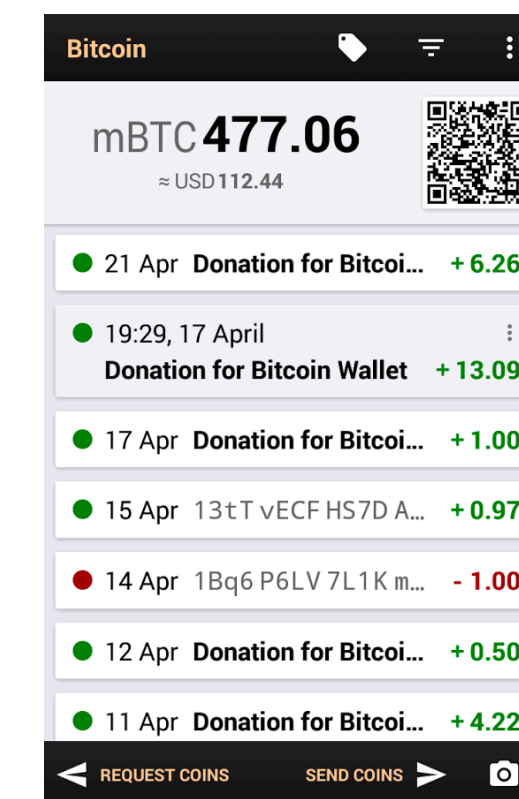
Blockchain Block



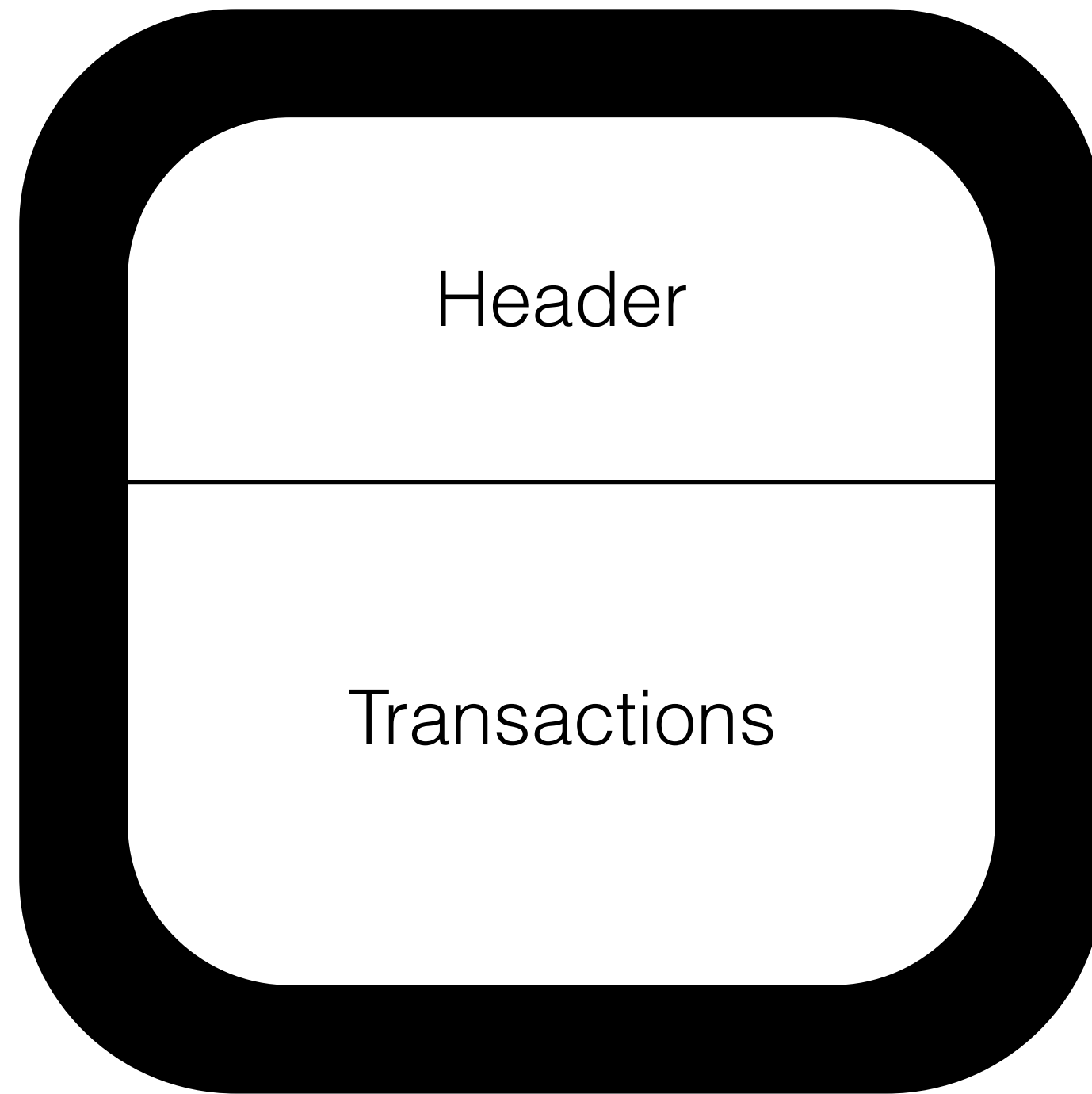
# Simple Payment Verification (SPV) Clients



Blockchain Block



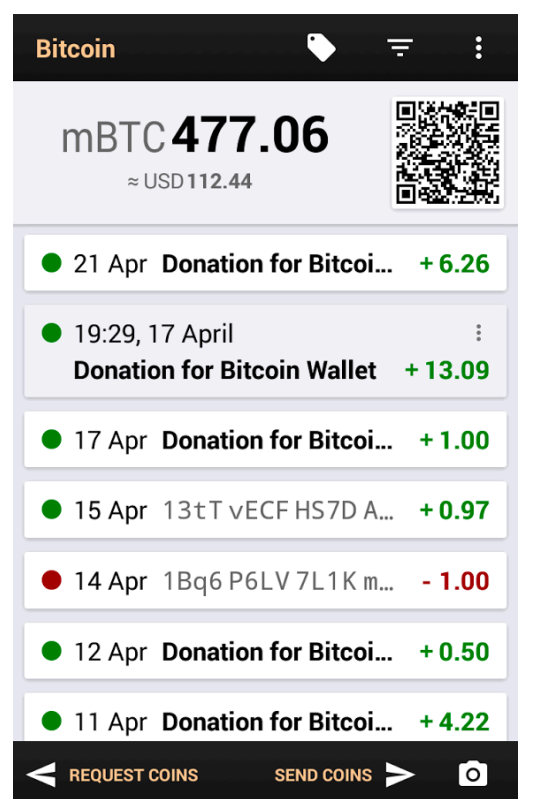
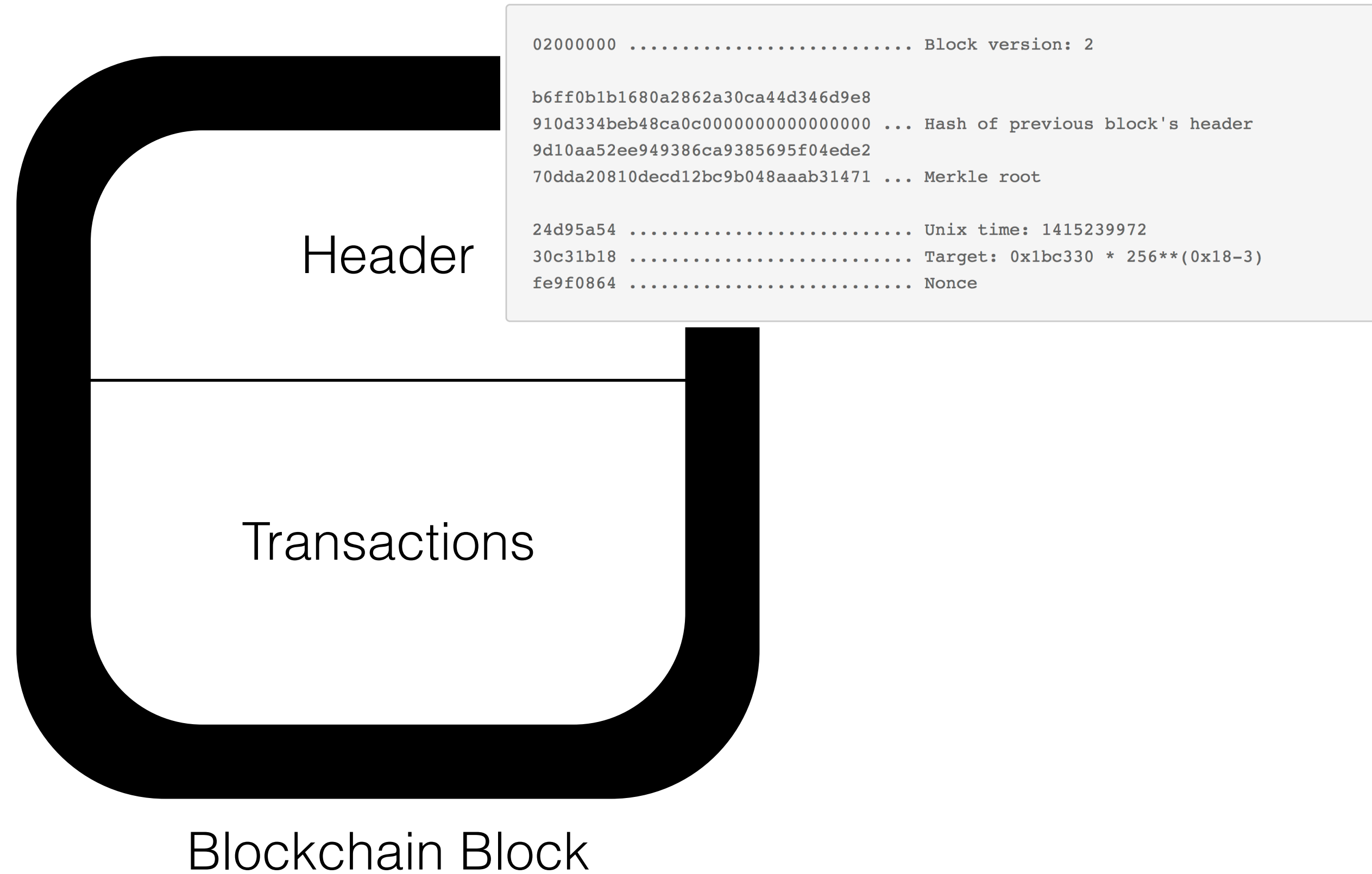
# Simple Payment Verification (SPV) Clients



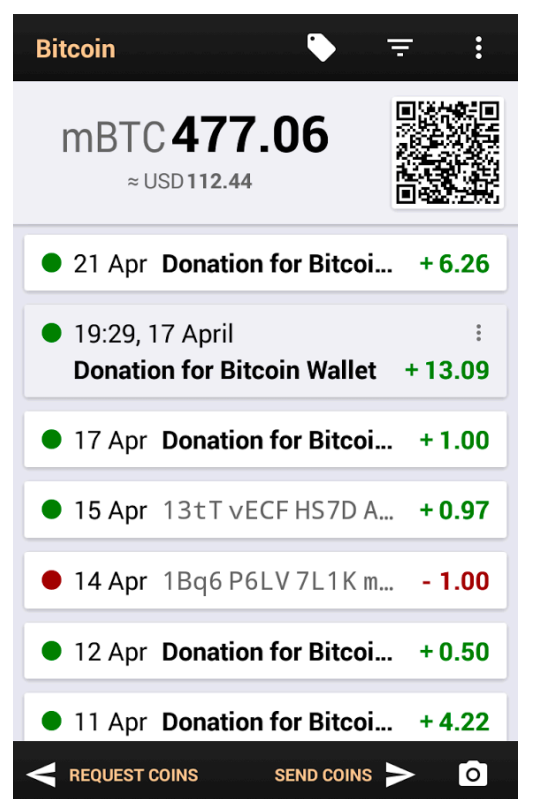
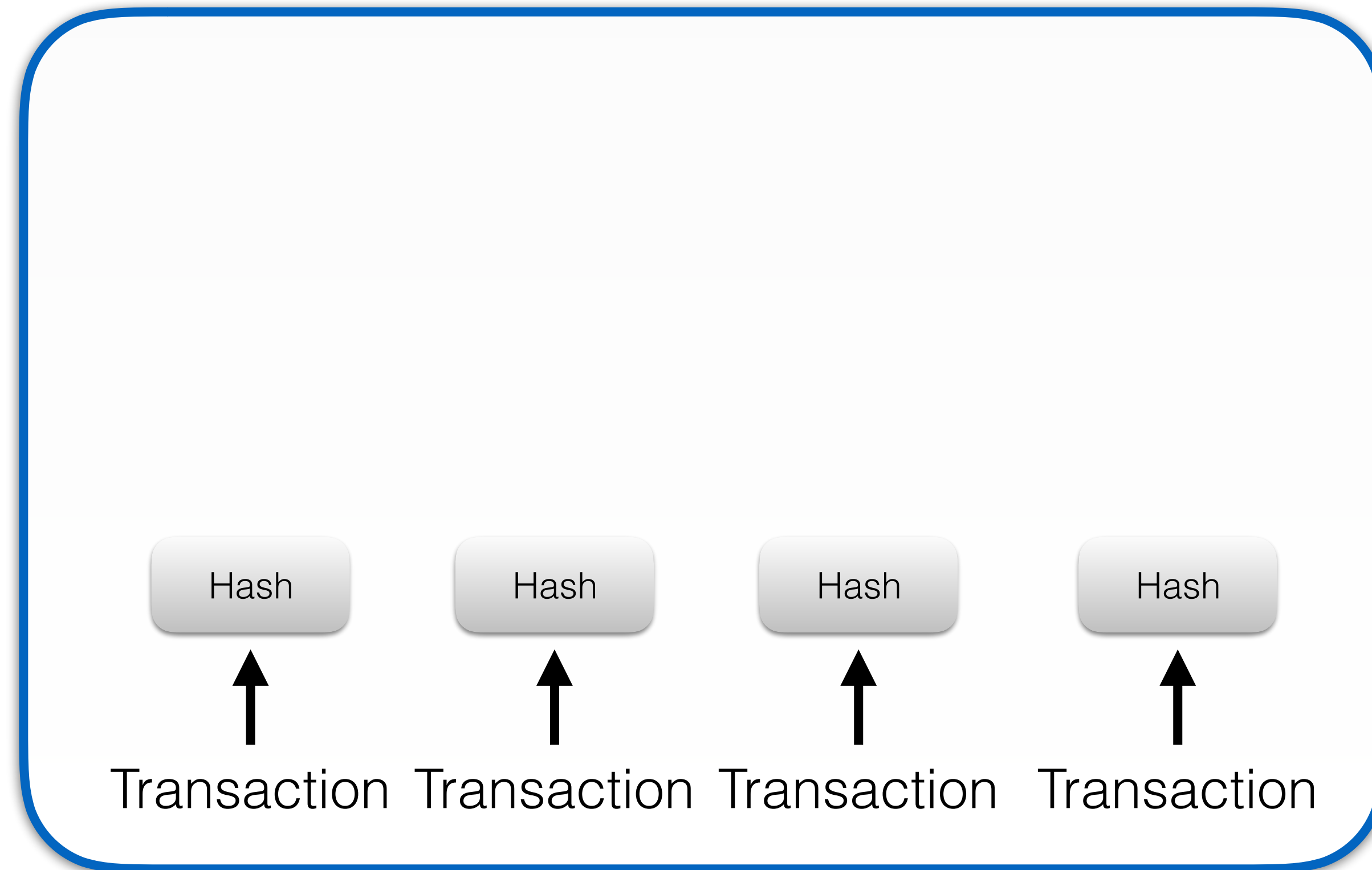
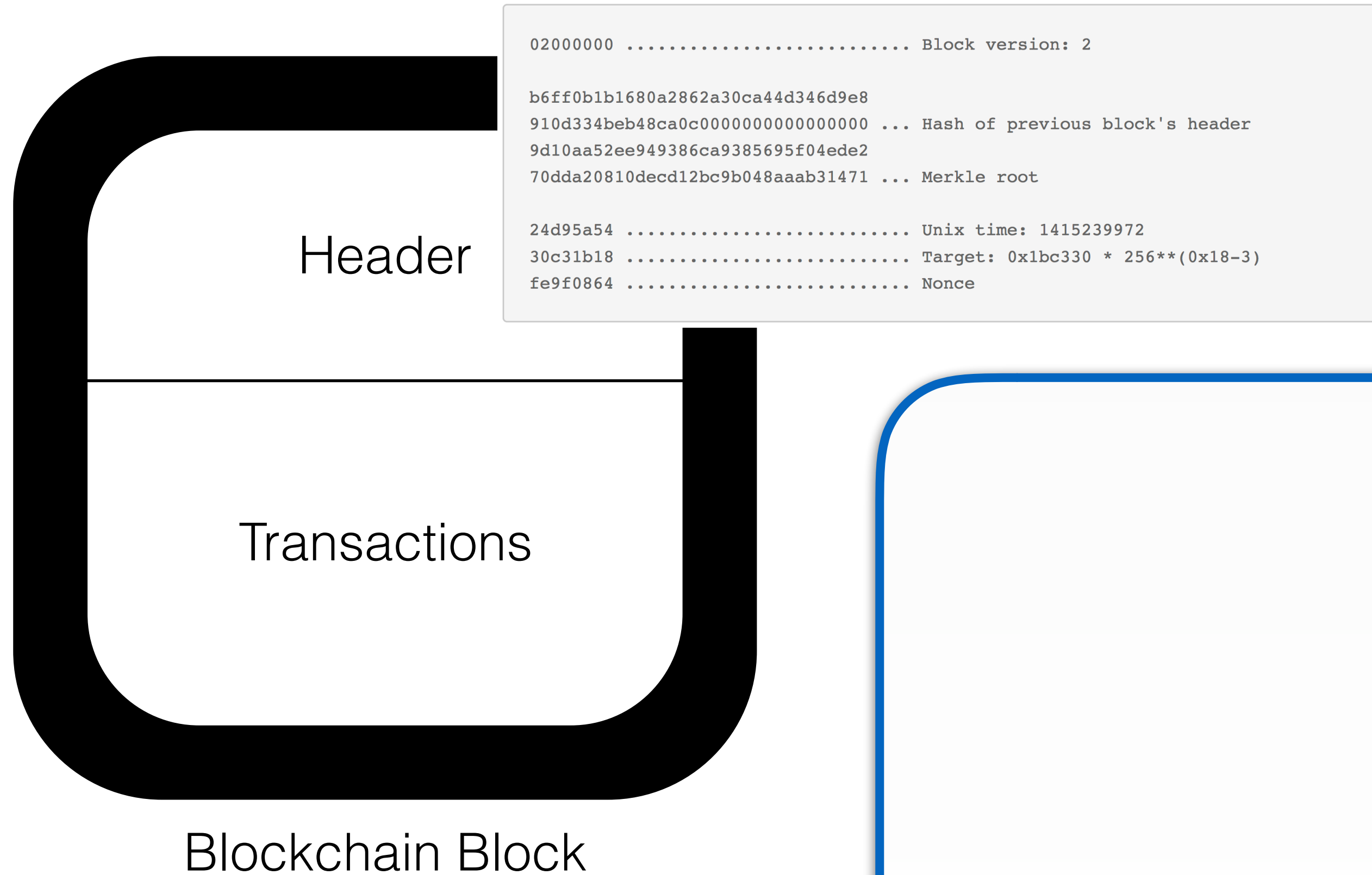
Blockchain Block



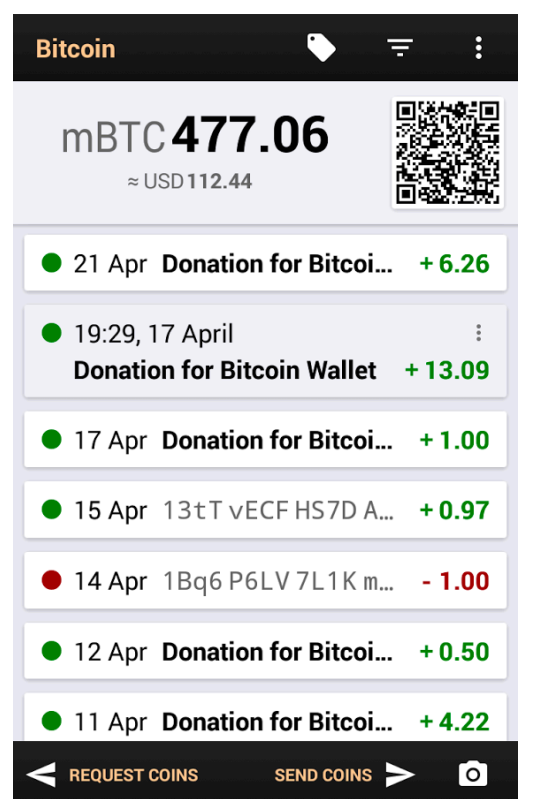
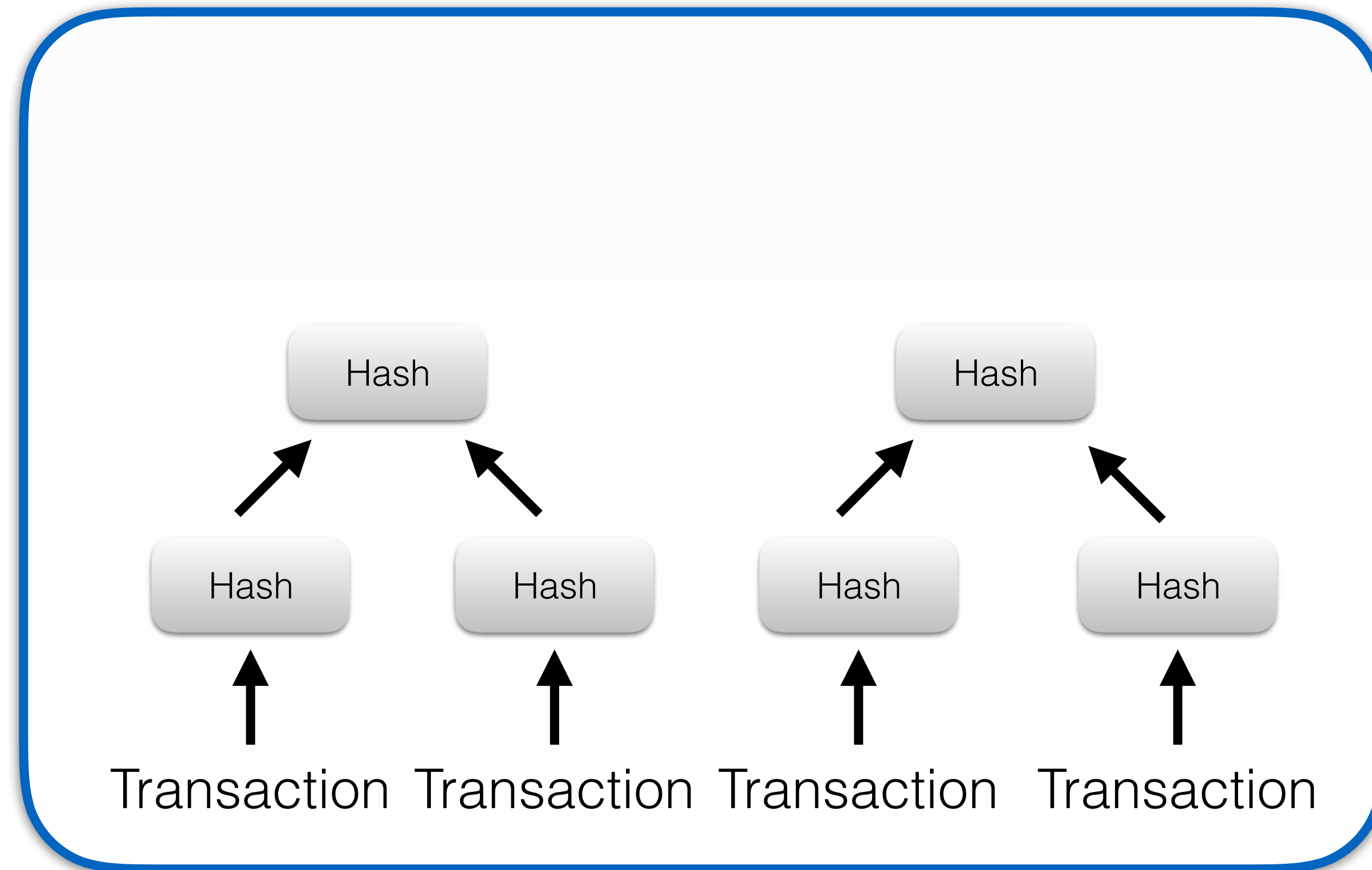
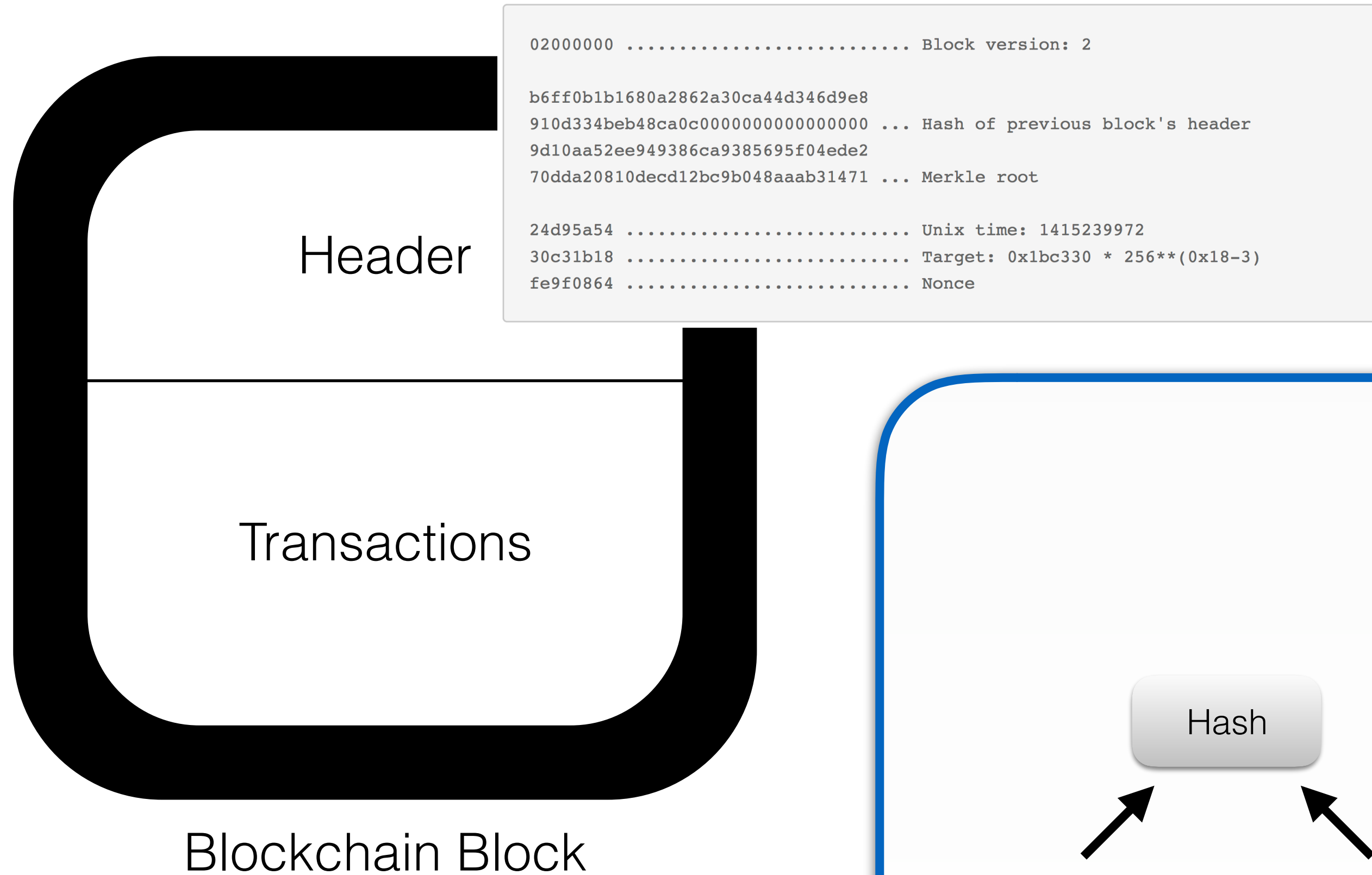
# Simple Payment Verification (SPV) Clients



# Simple Payment Verification (SPV) Clients

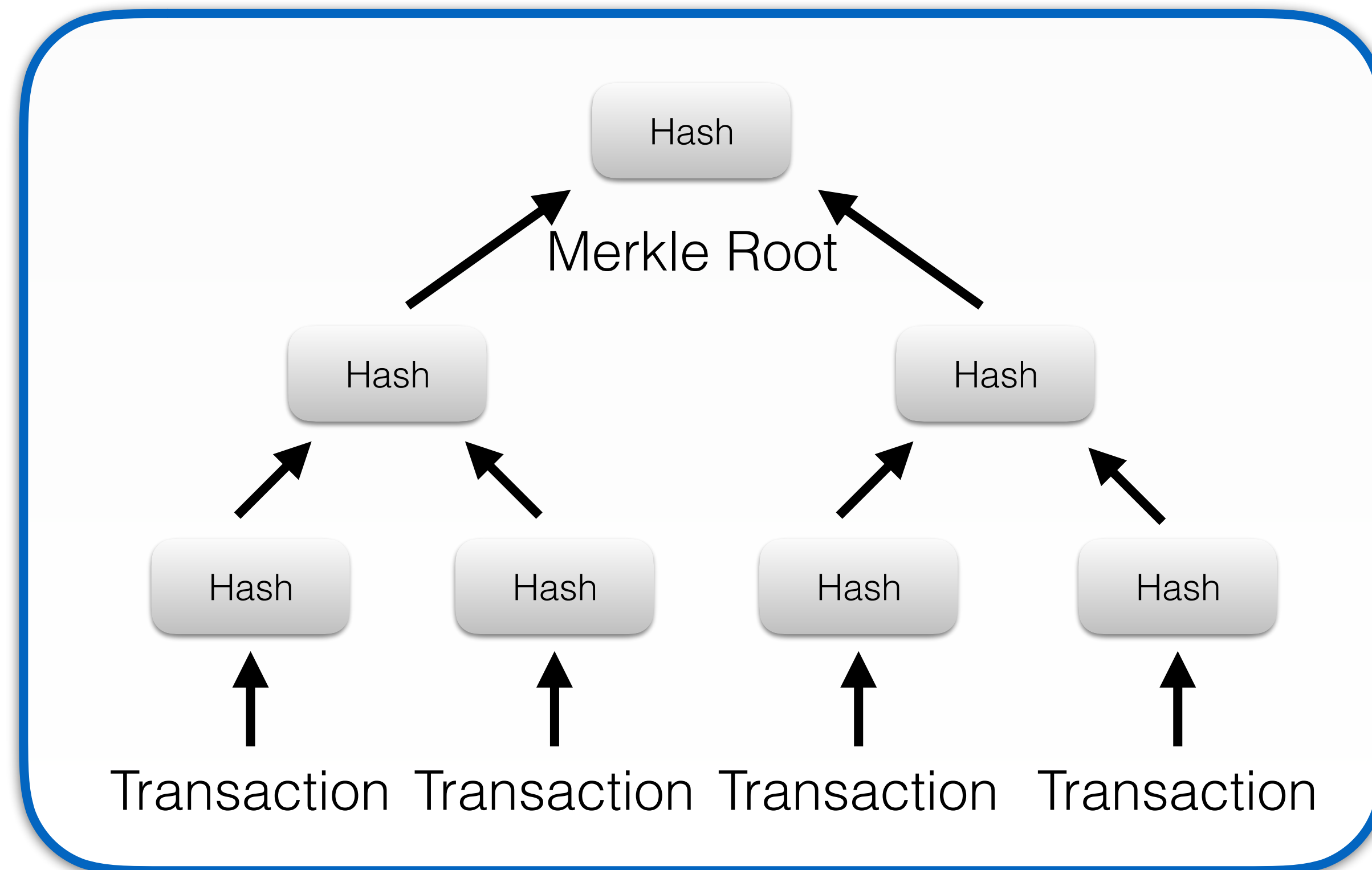
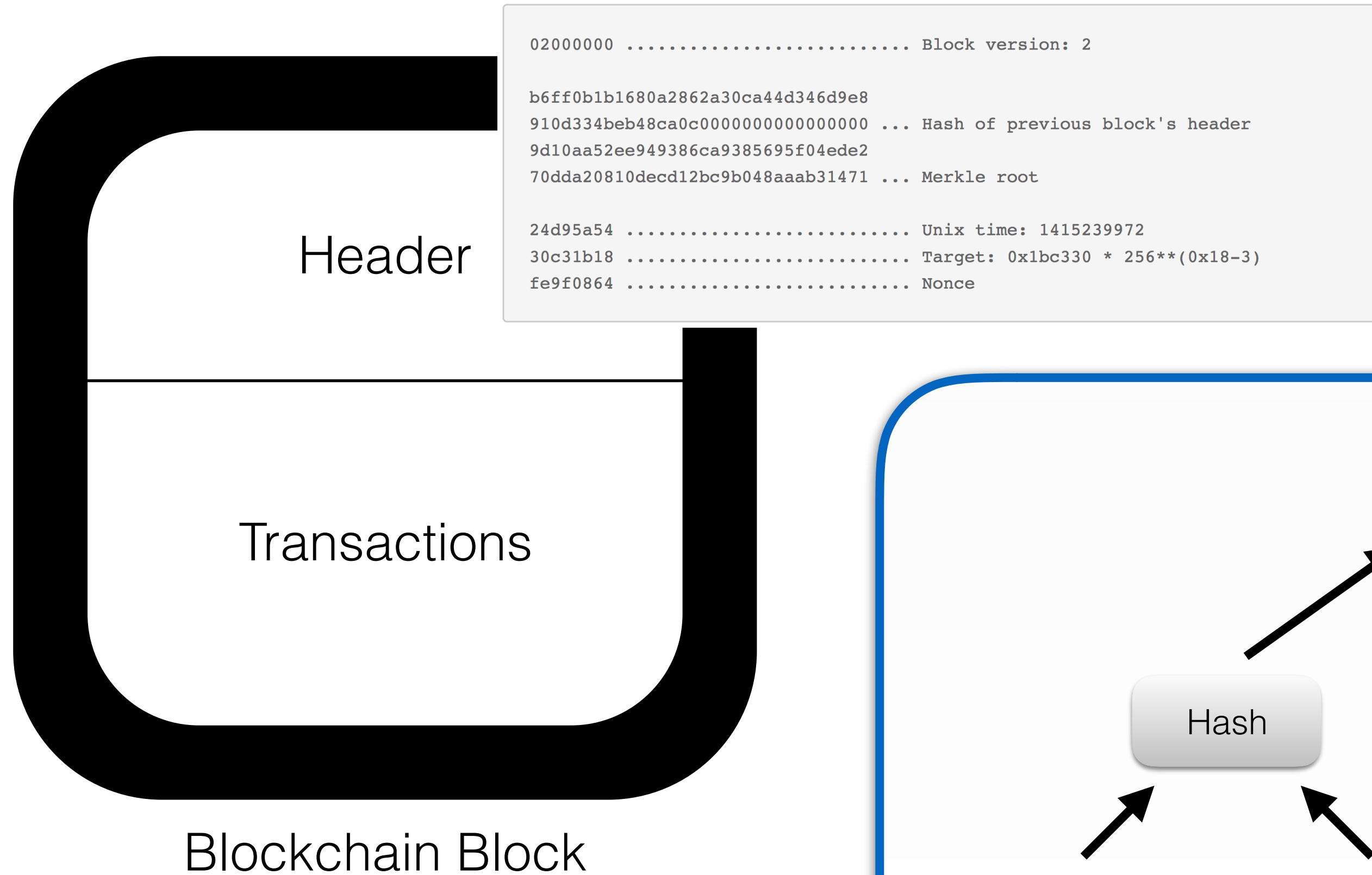


# Simple Payment Verification (SPV) Clients





# Simple Payment Verification (SPV) Clients



# Simple Payment Verification (SPV) Clients

SPV client



Full Bitcoin  
node



# Simple Payment Verification (SPV) Clients

SPV client



Did I receive new coins?

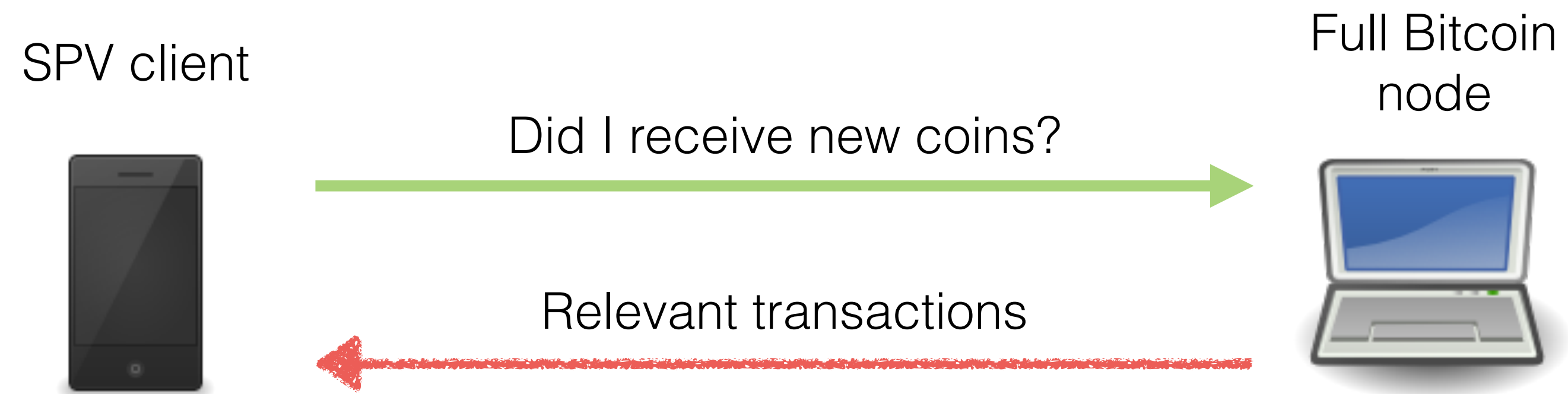


Full Bitcoin  
node

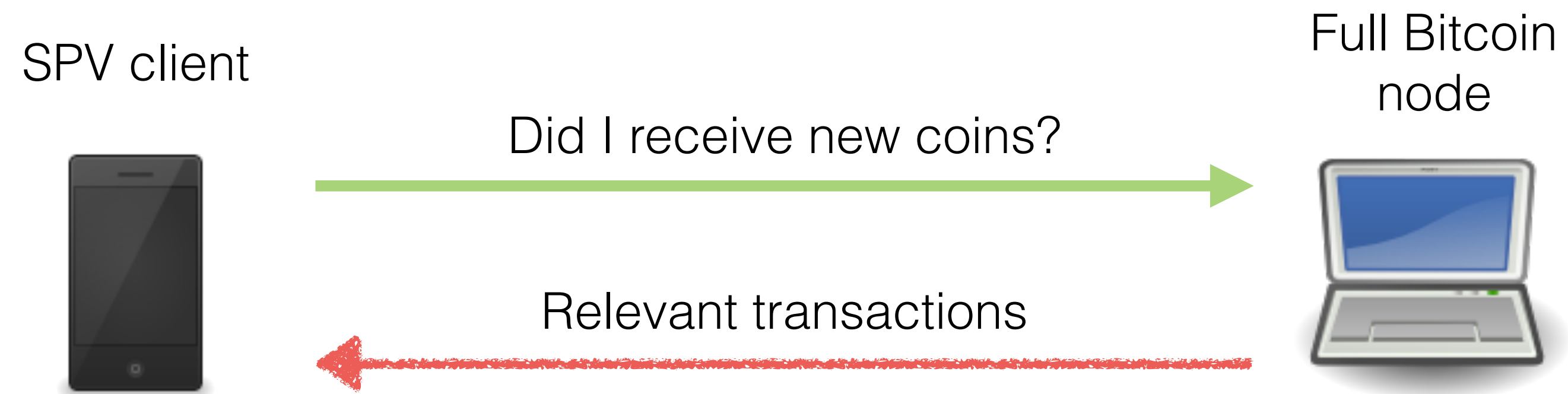




# Simple Payment Verification (SPV) Clients



# Simple Payment Verification (SPV) Clients



**Privacy!**

# Bloom Filter



**Bloom filter**





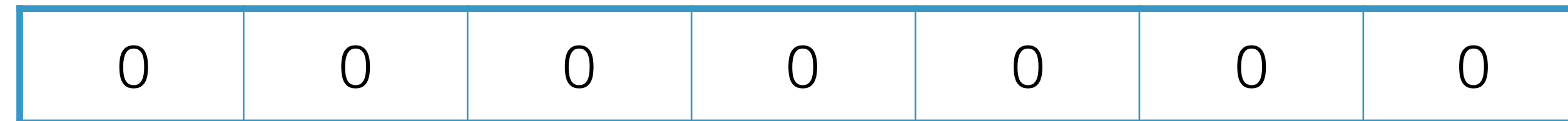
# Bloom Filter



Insertion

$\{ @_1, @_2, @_3 \}$

**Bloom filter**



# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**



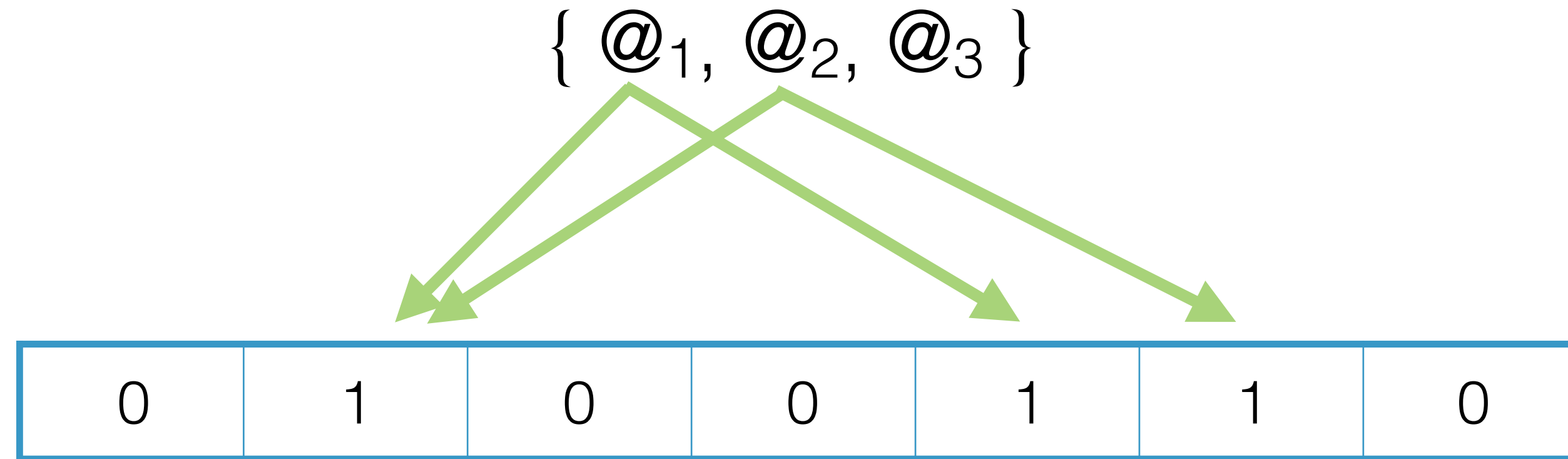
# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**



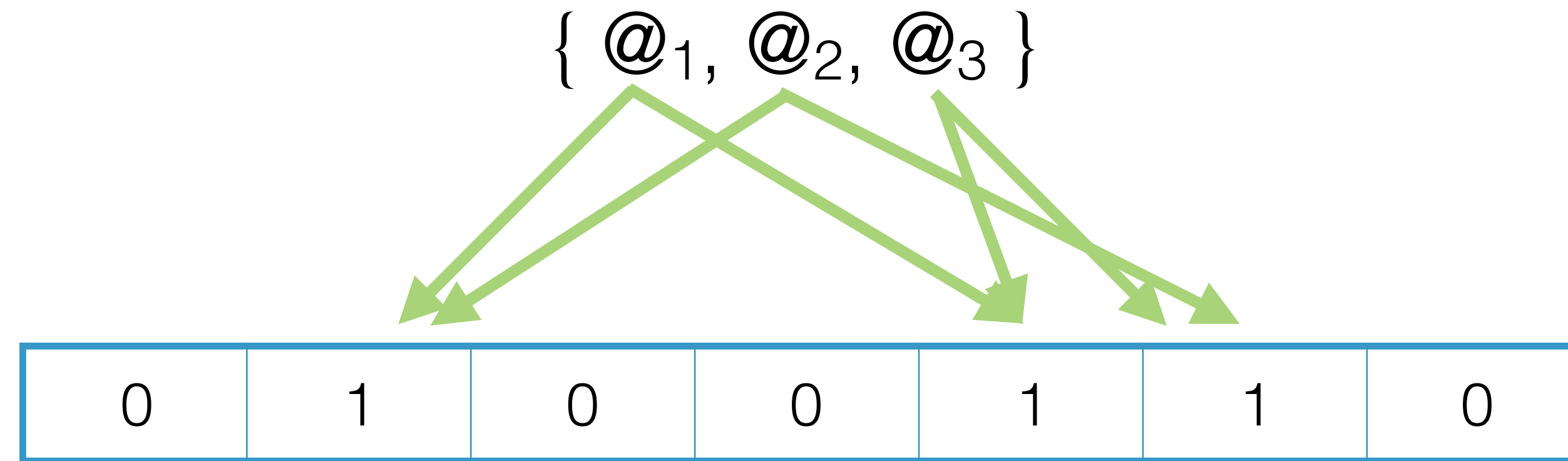


# Bloom Filter



Insertion

**Bloom filter**



# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**



Membership test

{ @<sub>1</sub>, @<sub>4</sub>, @<sub>5</sub> }

# Bloom Filter



Insertion

$\{ @_1, @_2, @_3 \}$

**Bloom filter**



Membership test

$\{ @_1, @_4, @_5 \}$

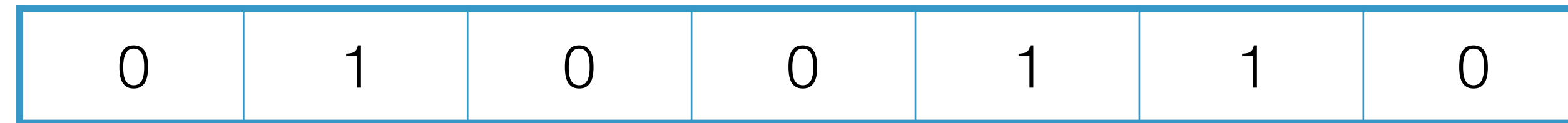
# Bloom Filter



Insertion

$\{ @_1, @_2, @_3 \}$

**Bloom filter**



Membership test

$\{ @_1, @_4, @_5 \}$

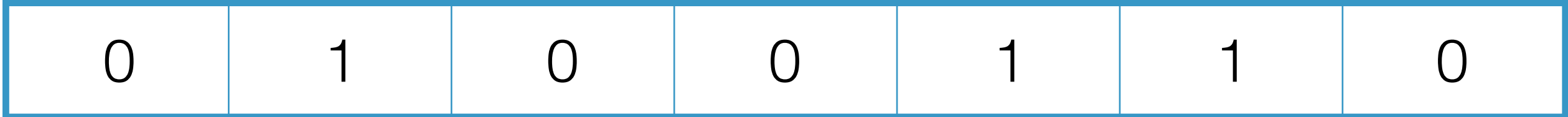
# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**

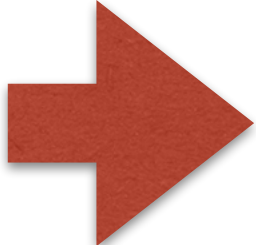


Membership test

{ @<sub>1</sub>, @<sub>4</sub>, @<sub>5</sub> }



@<sub>4</sub> False positive



**target False Positive Rate (FPR)**



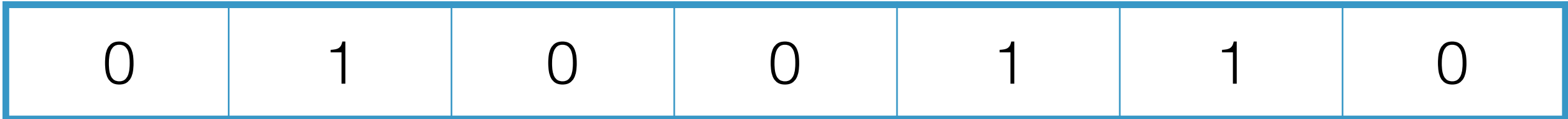
# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**



Membership test

{ @<sub>1</sub>, @<sub>4</sub>, @<sub>5</sub> }

! @<sub>4</sub> False positive

➔ **target False Positive Rate (FPR)**

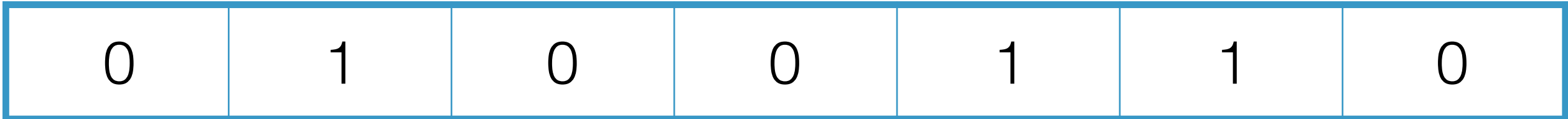
# Bloom Filter



Insertion

{ @<sub>1</sub>, @<sub>2</sub>, @<sub>3</sub> }

**Bloom filter**



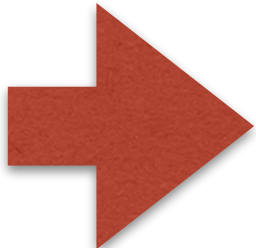
Membership test

{ @<sub>1</sub>, @<sub>4</sub>, @<sub>5</sub> }



@<sub>4</sub> False positive

@<sub>5</sub> True negative



**target False Positive Rate (FPR)**

# BIP-37 (Bloom Filters)

SPV client



Full Bitcoin  
node



Full Bitcoin  
node

# BIP-37 (Bloom Filters)

SPV client



@<sub>1</sub>  
@<sub>2</sub>  
@<sub>3</sub>

0 1 0 0 1 1 0

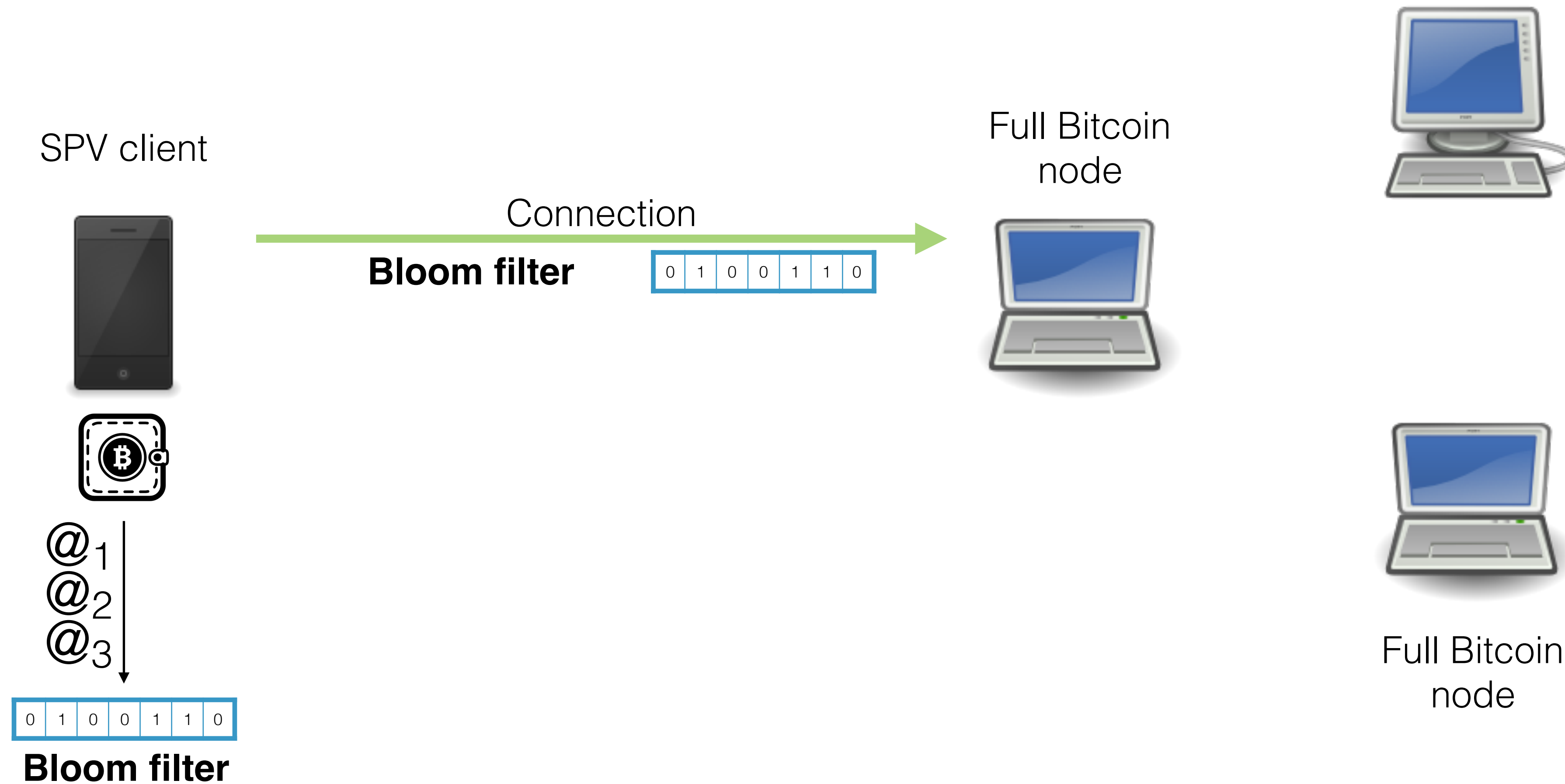
**Bloom filter**

Full Bitcoin  
node



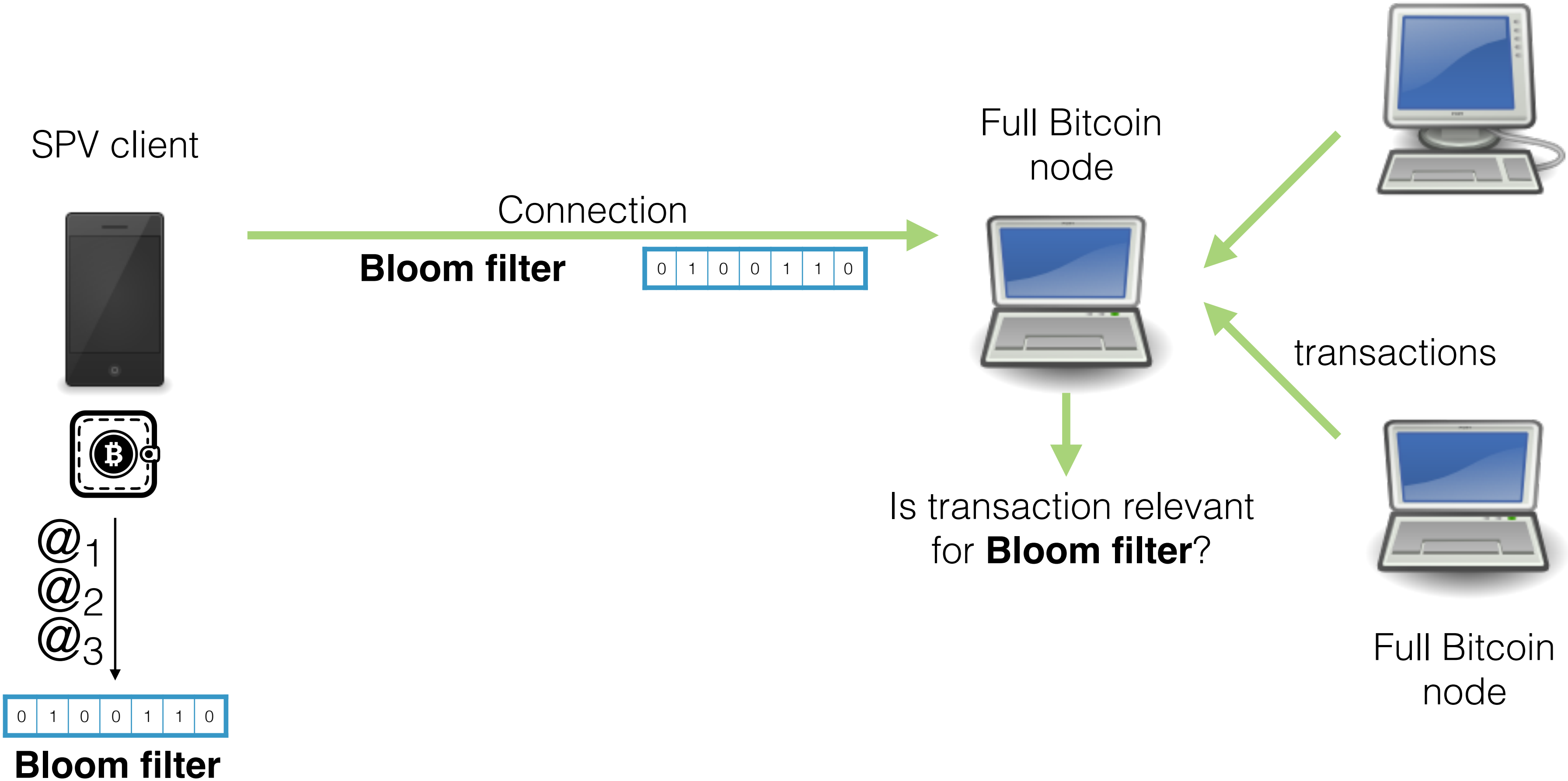
Full Bitcoin  
node

# BIP-37 (Bloom Filters)

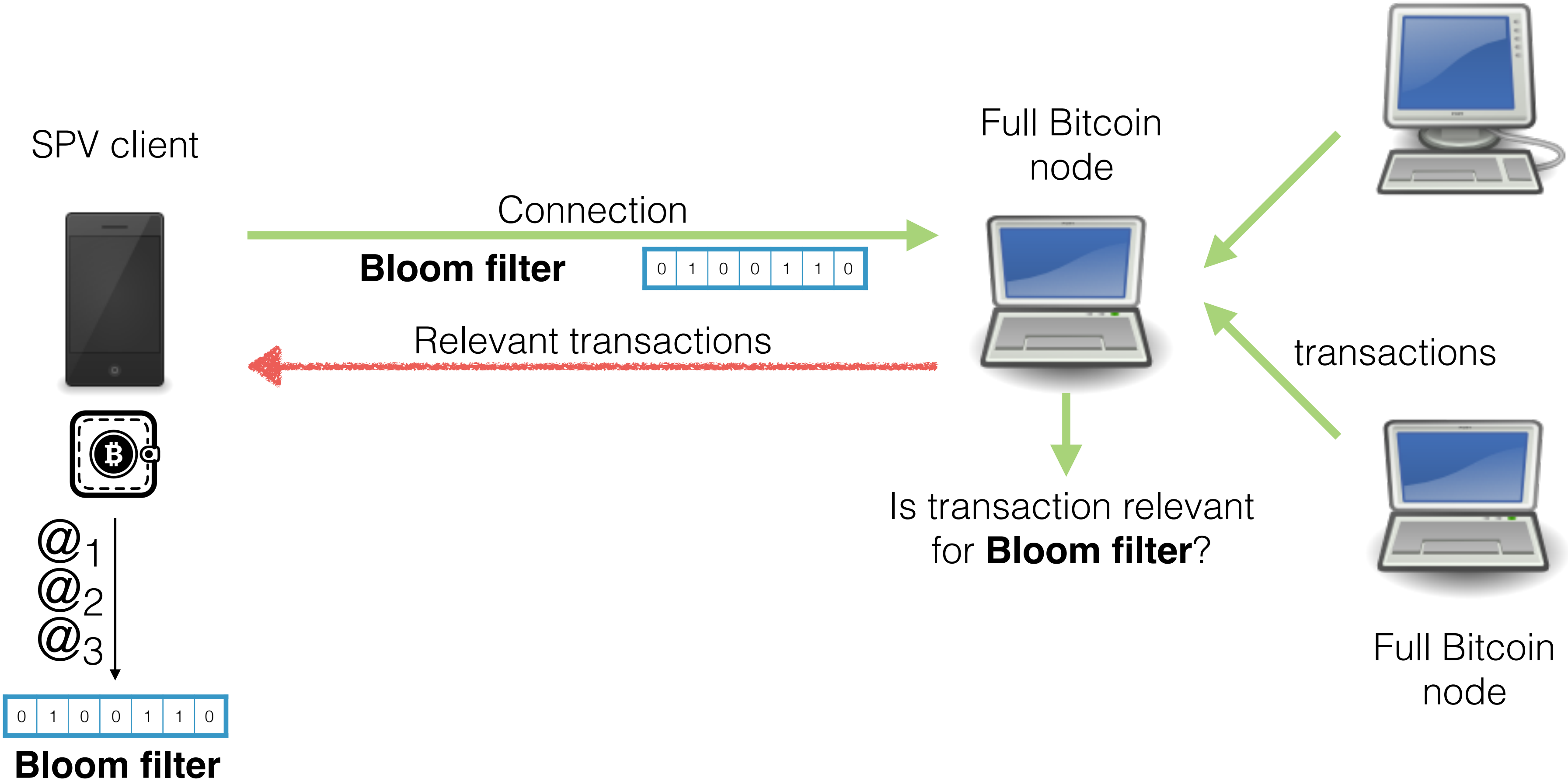




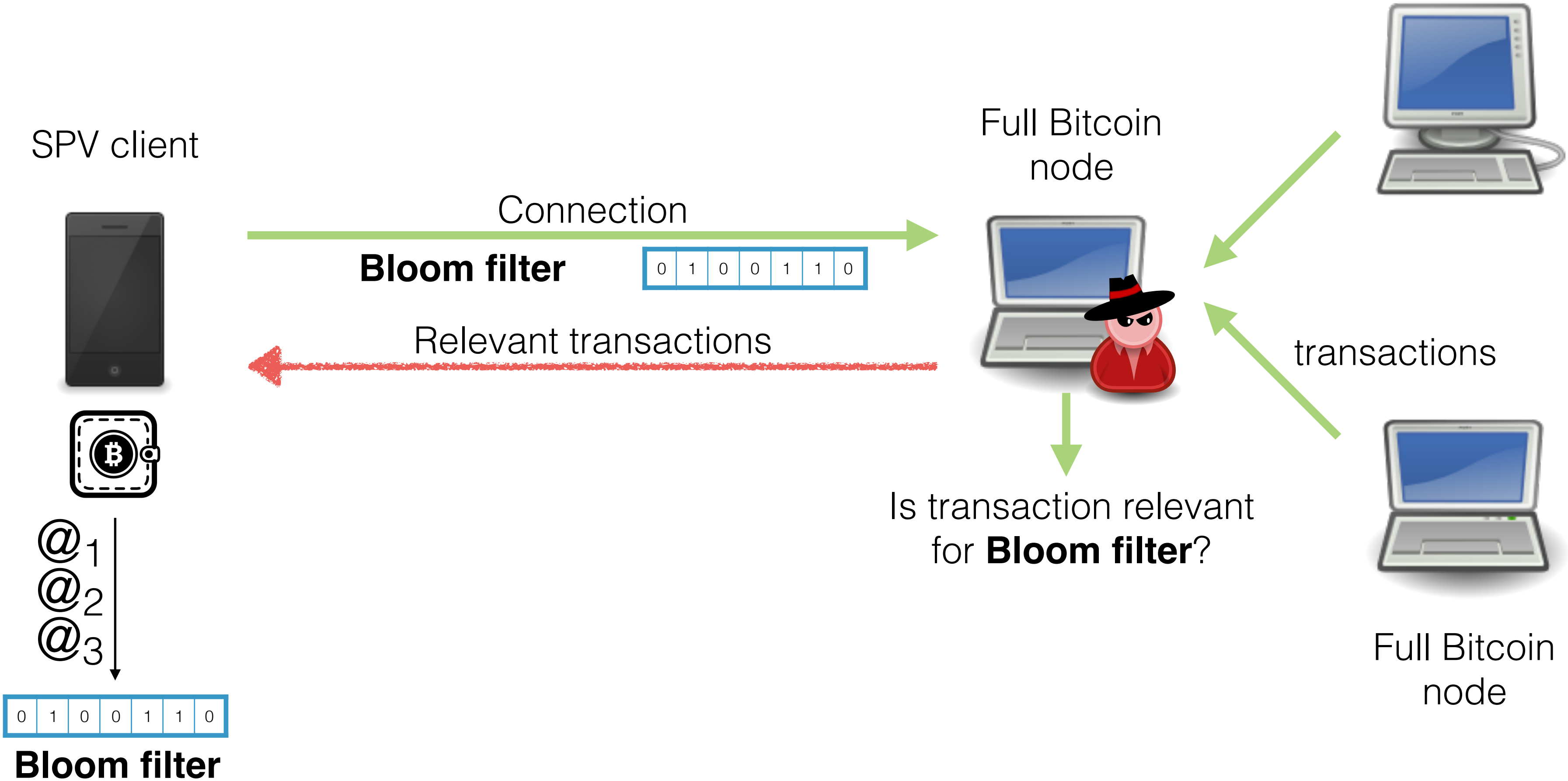
# BIP-37 (Bloom Filters)



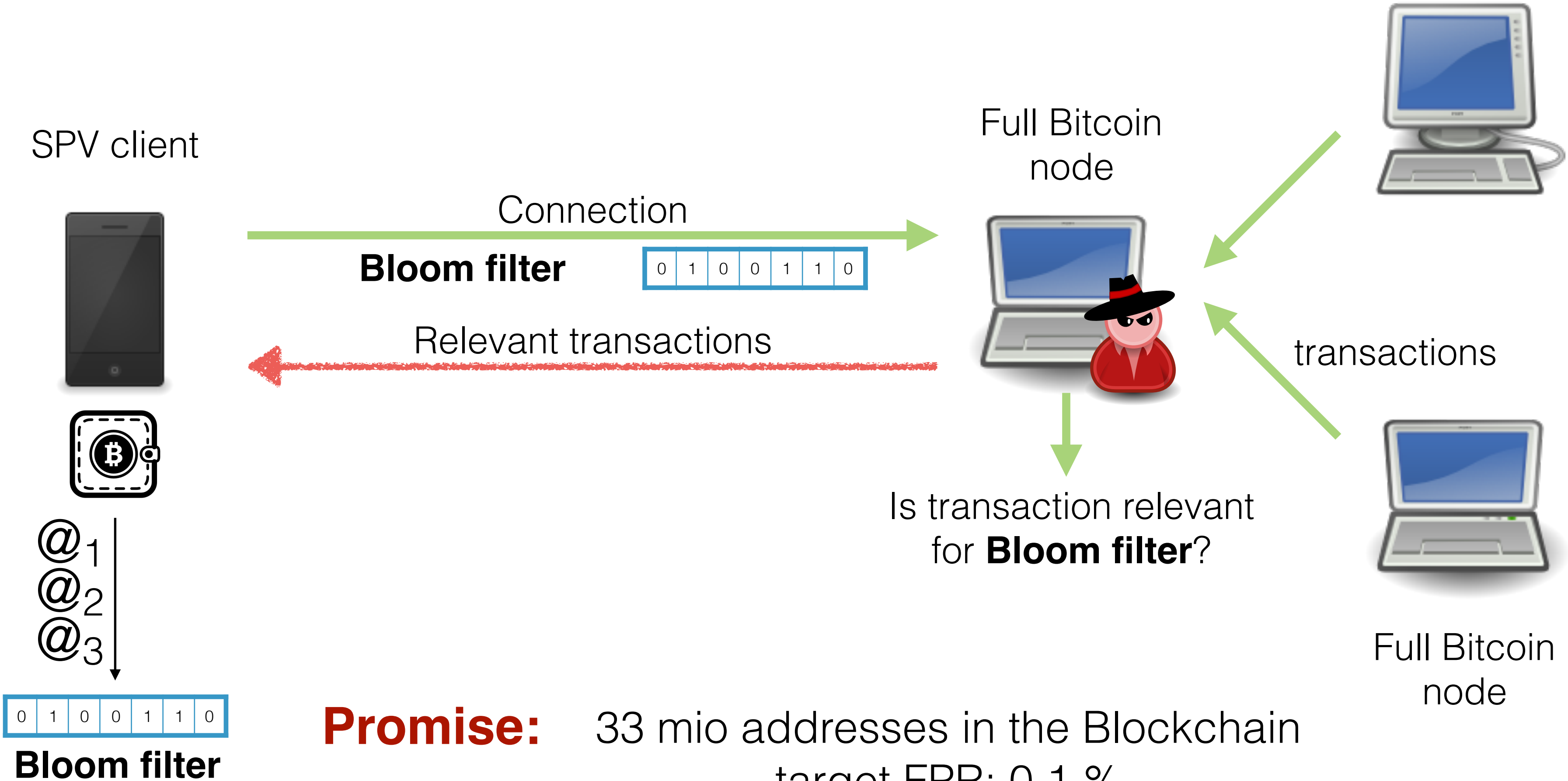
# BIP-37 (Bloom Filters)



# BIP-37 (Bloom Filters)

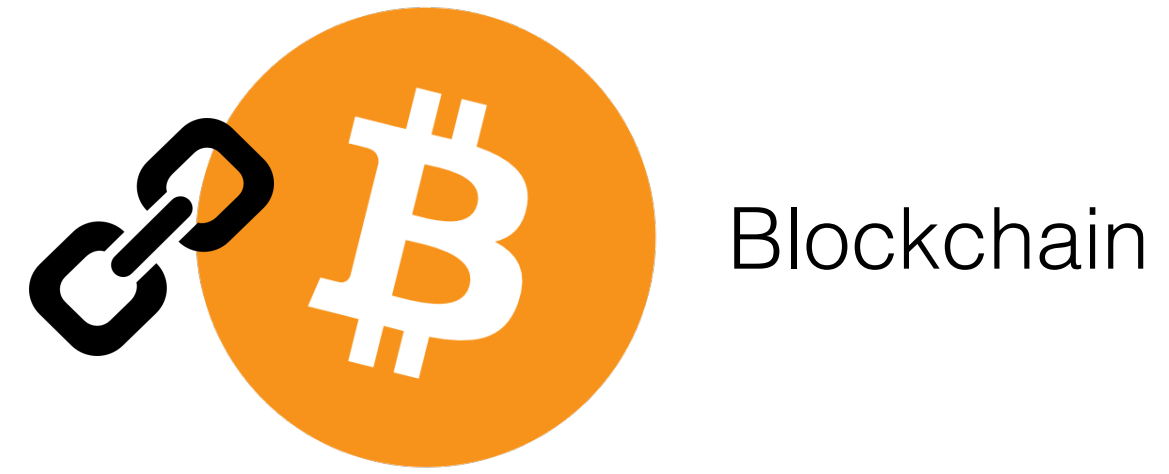


# BIP-37 (Bloom Filters)



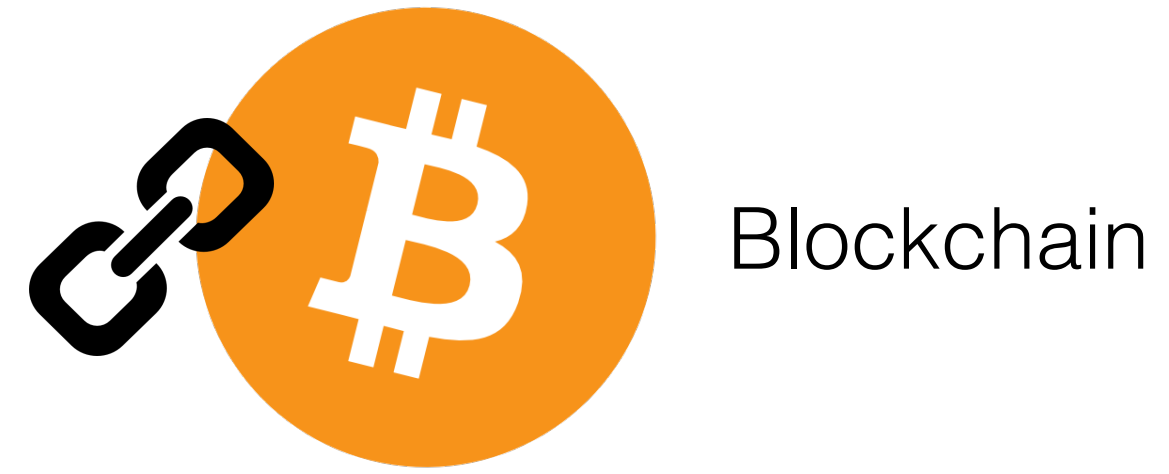
**Promise:** 33 mio addresses in the Blockchain  
 target FPR: 0.1 %  
 "User addresses hidden amongst  
 33 000" false positives

# Model and Privacy measure





# Model and Privacy measure

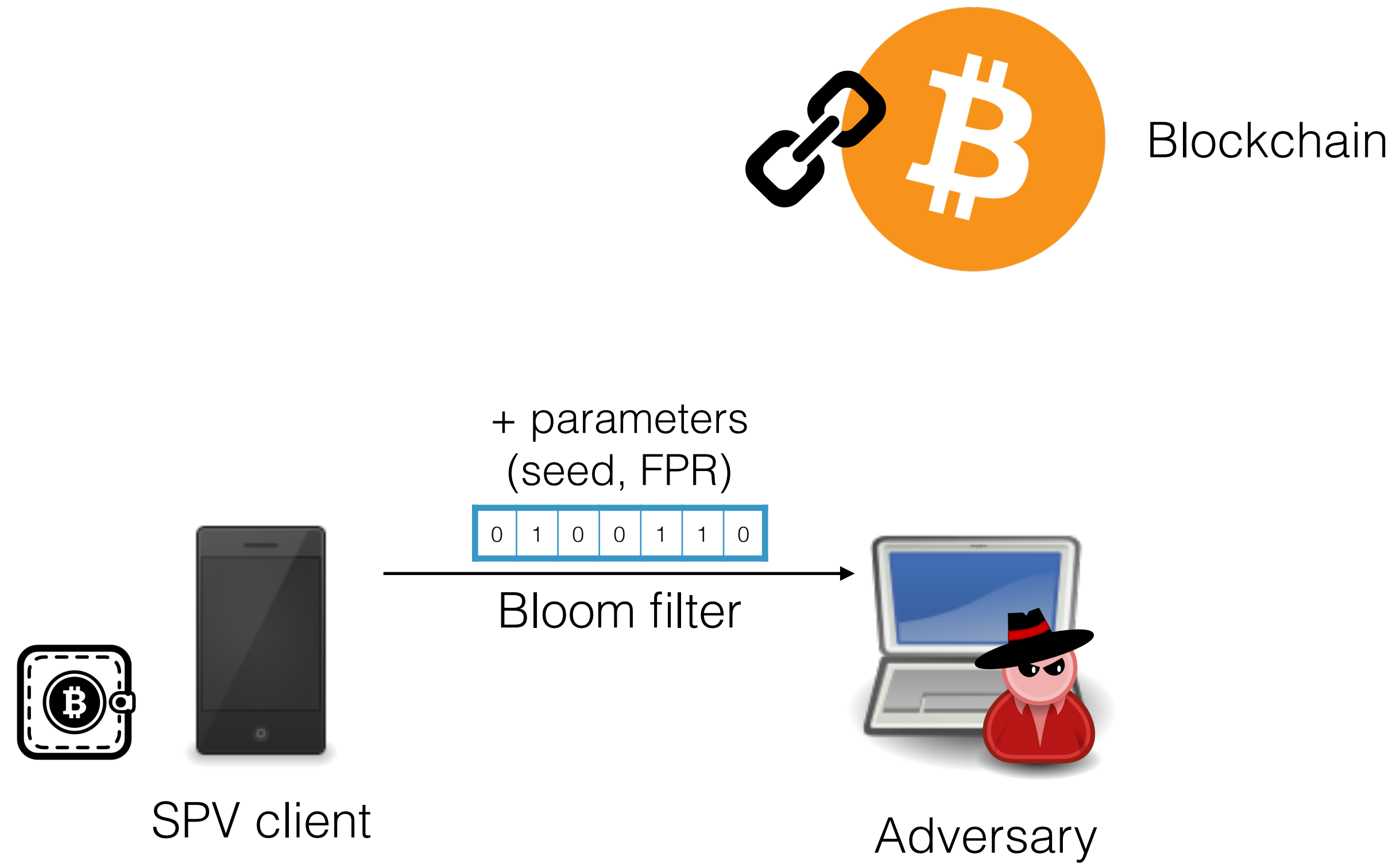


SPV client

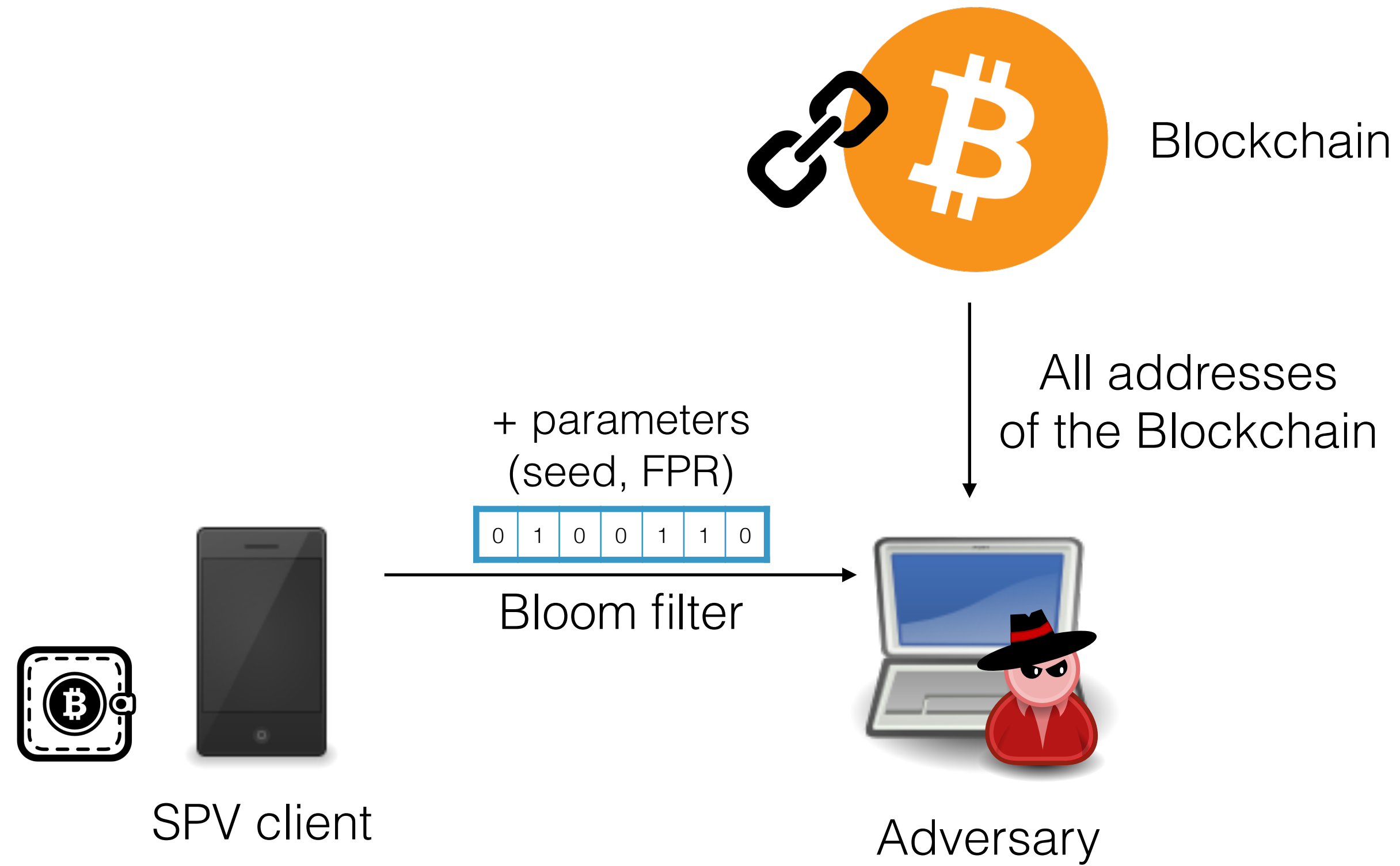


Adversary

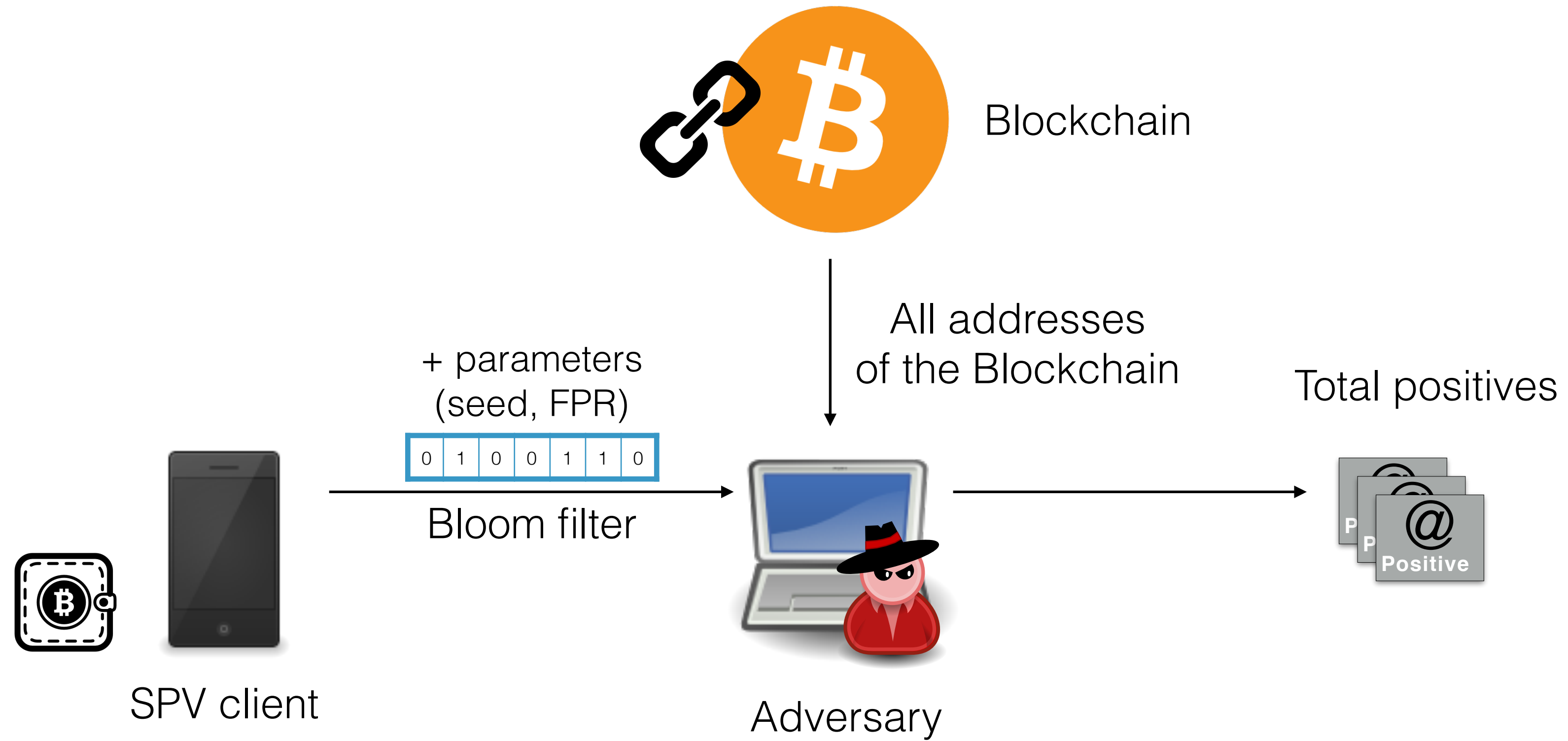
# Model and Privacy measure



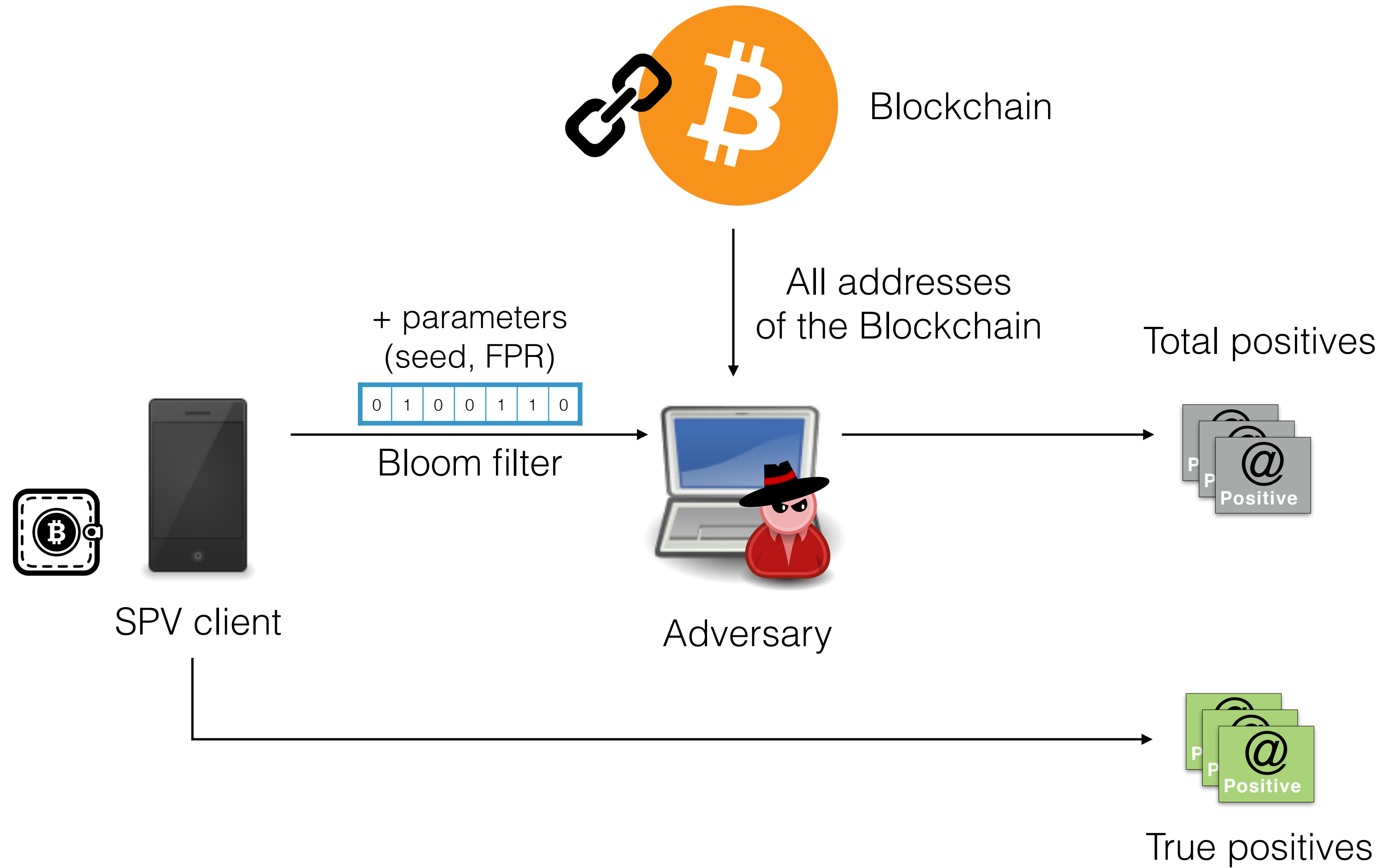
# Model and Privacy measure



# Model and Privacy measure

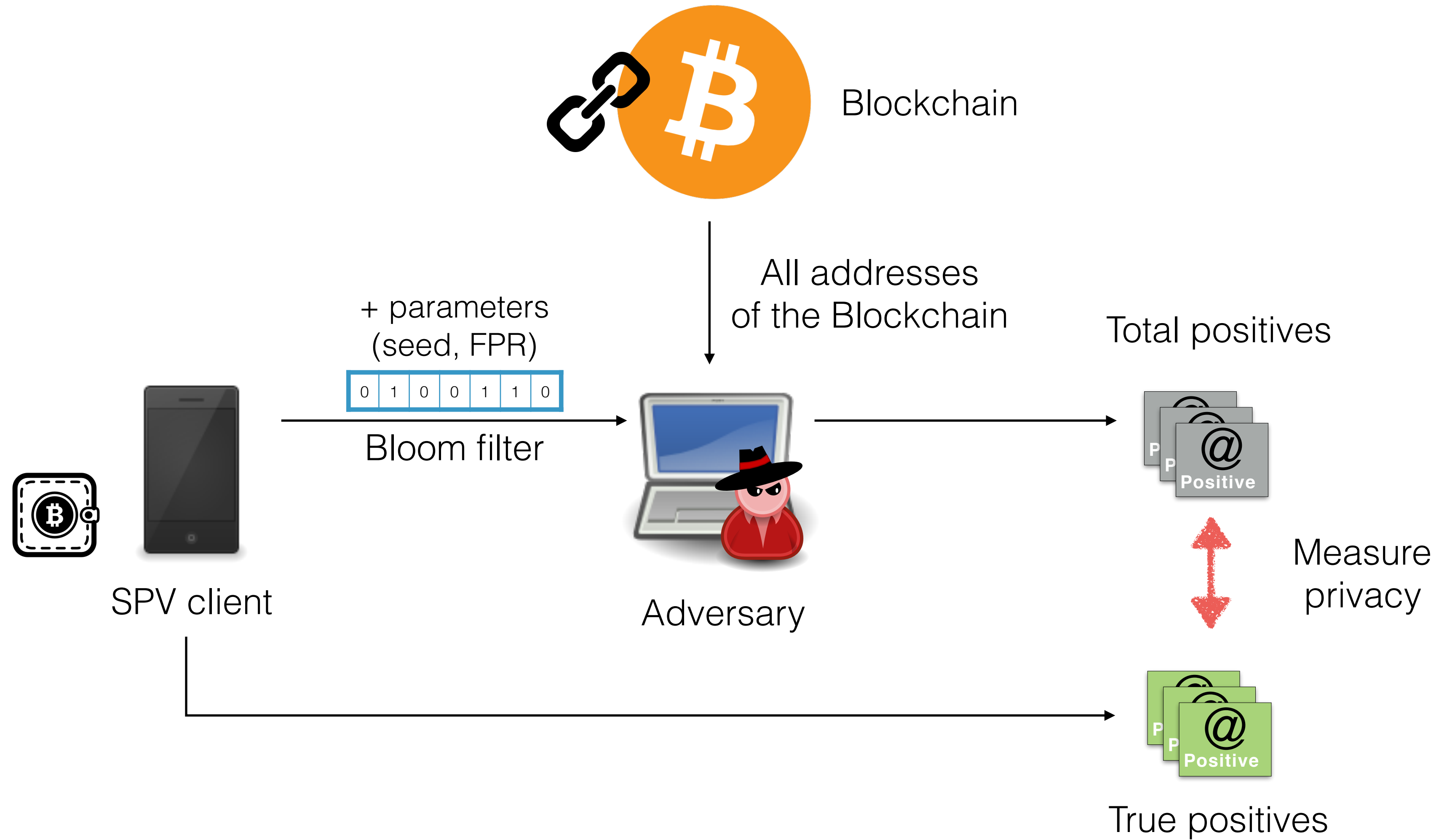


# Model and Privacy measure

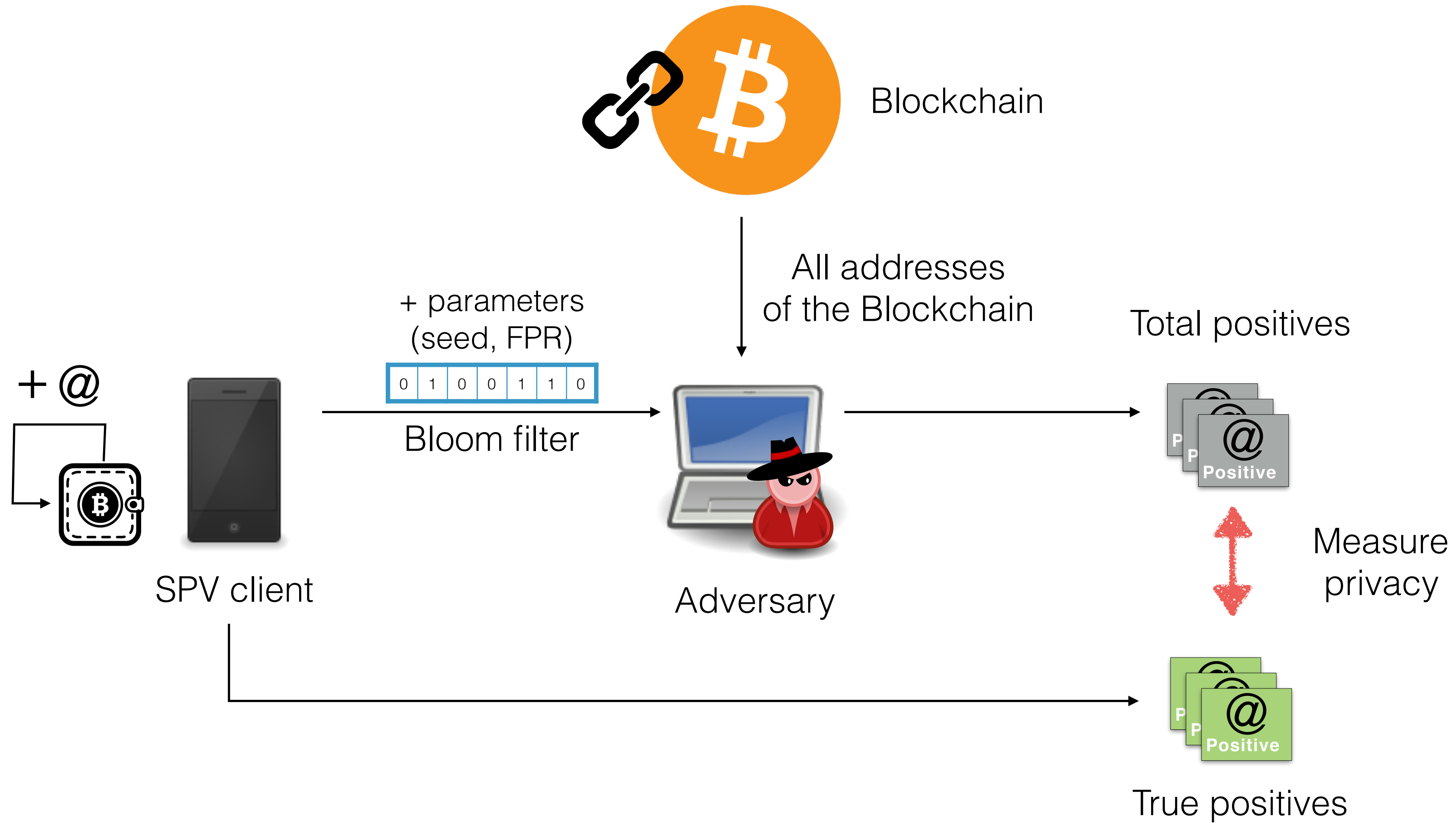




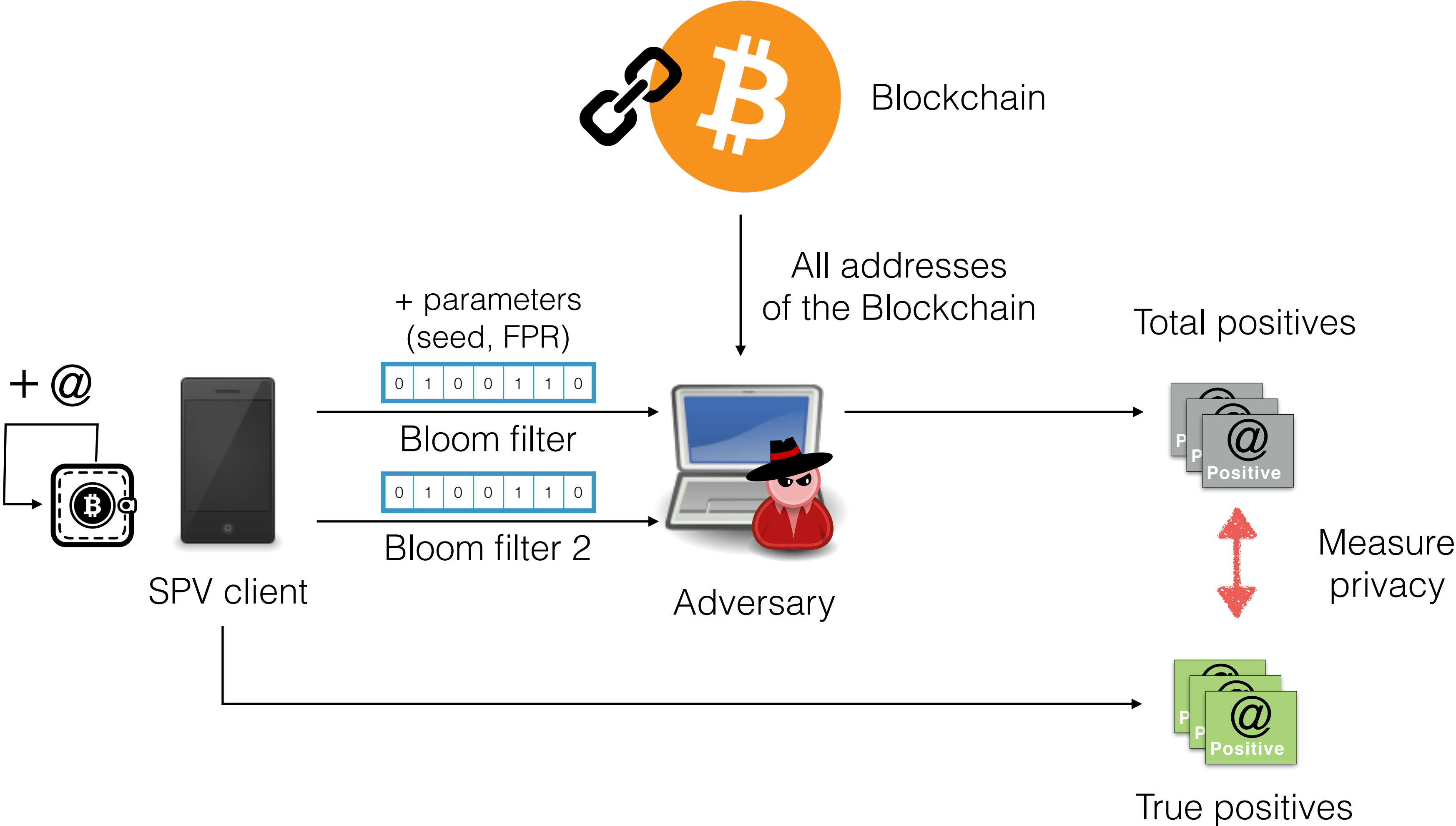
# Model and Privacy measure



# Model and Privacy measure

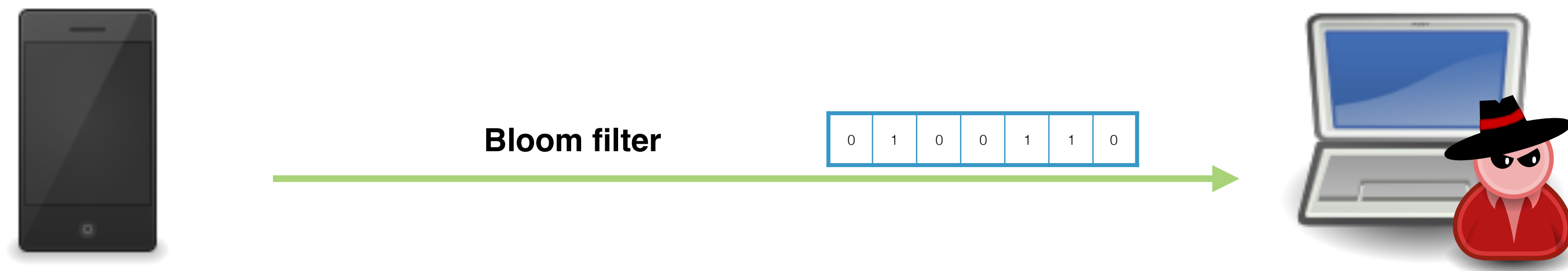


# Model and Privacy measure

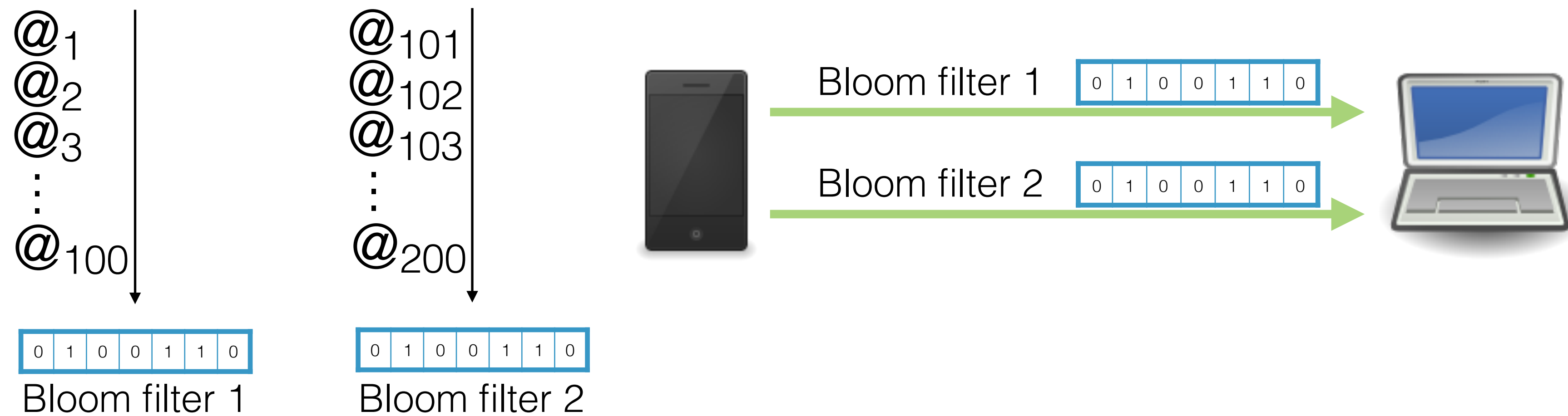


# SPV + Bloom Filter

1. Given **one** Bloom filter, Bitcoin addresses partially linkable
  - Addresses **linkable** if  $< 20$  addresses in wallet
2. Given **multiple** Bloom filter, addresses nearly always linkable



# Proposed solution



- Pre-generate Bitcoin addresses and insert into filter
- Keep state about outsourced Bloom filter ↻
- Overhead: For 100 addresses, < 1 kb

# Private Information Retrieval

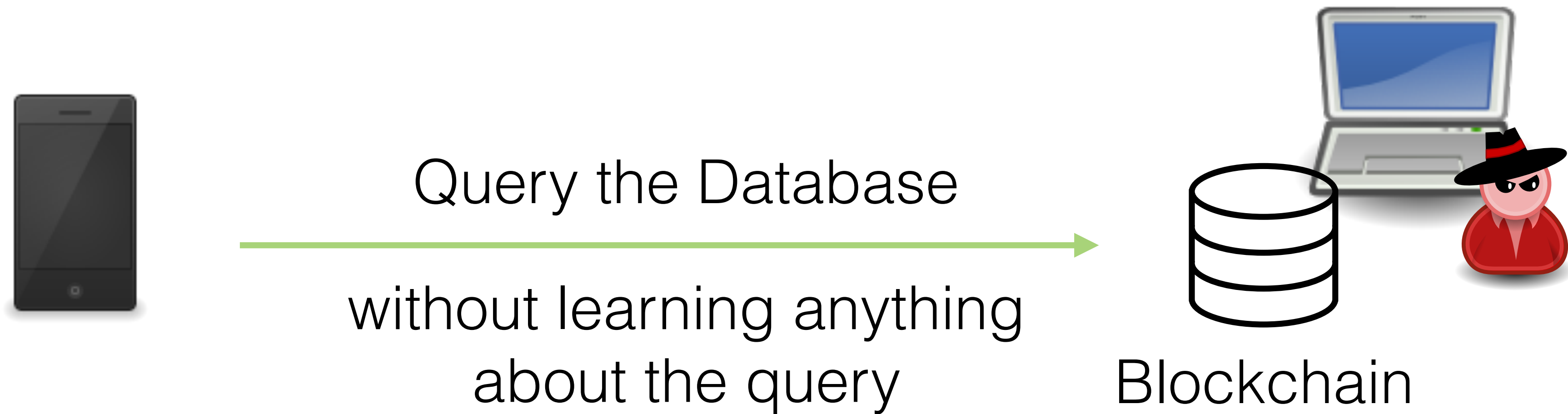


Query the Database  
without learning anything  
about the query



Blockchain

# Private Information Retrieval



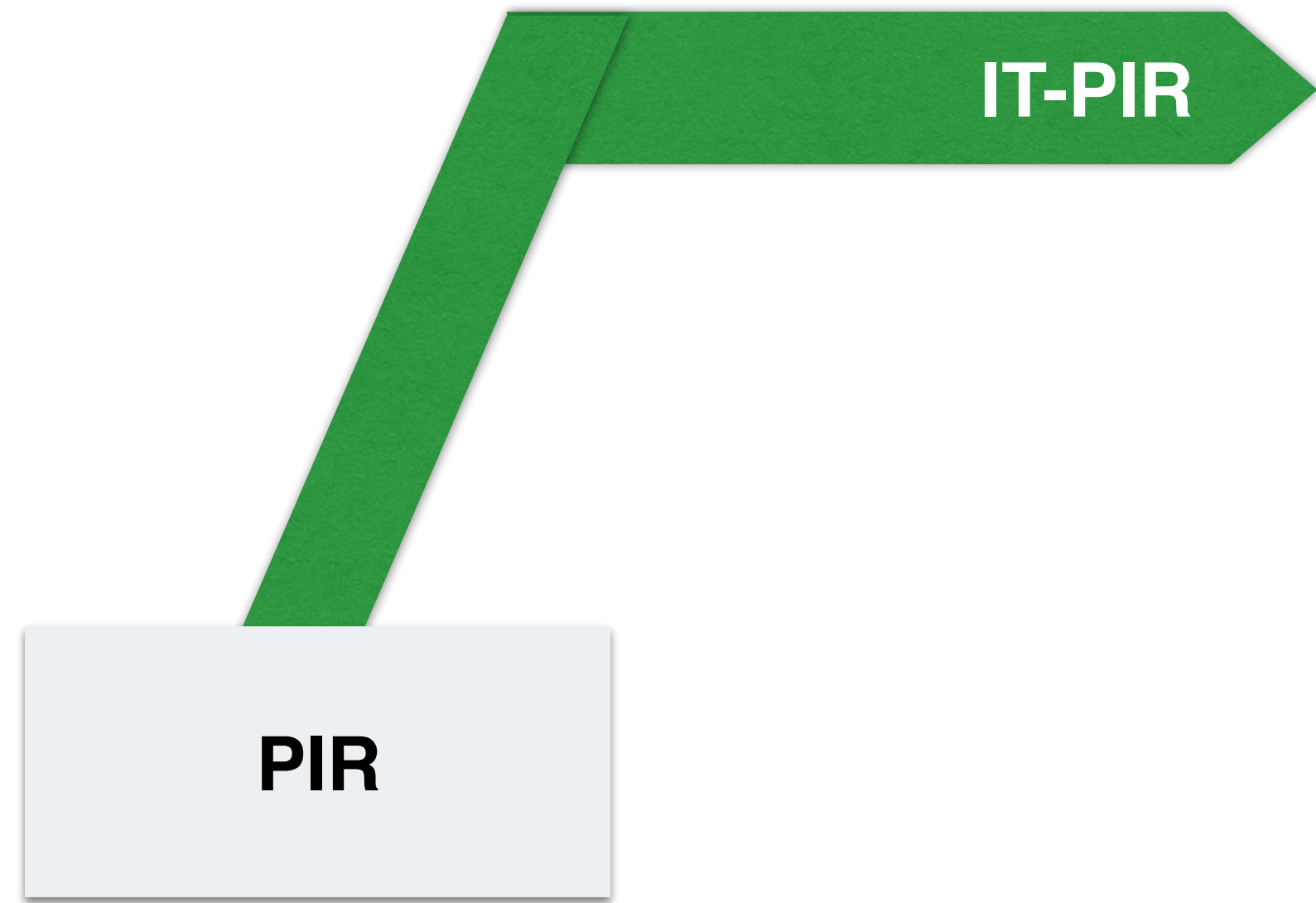
**Solution:** Download the entire DB!



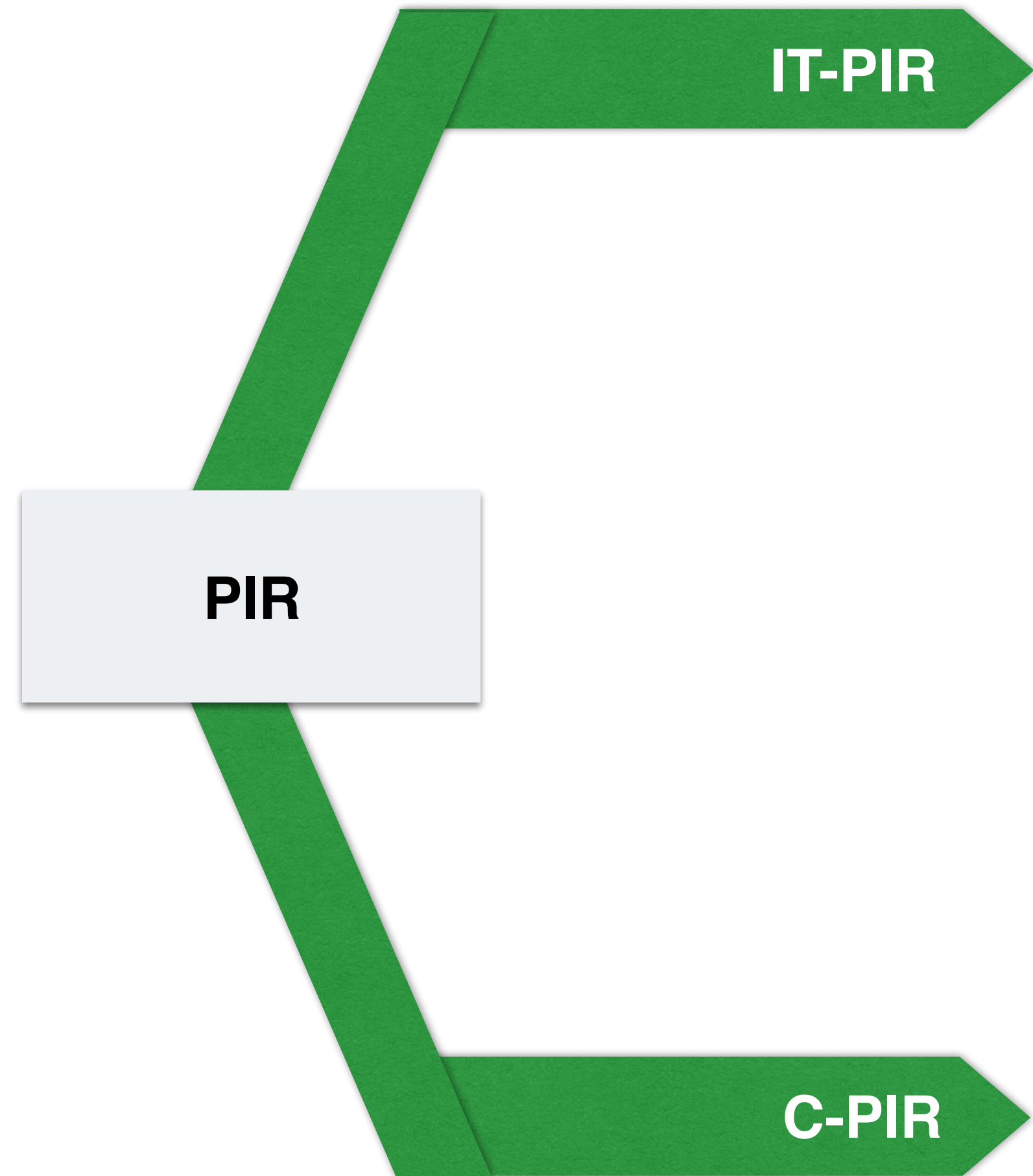
# PIR Versions

PIR

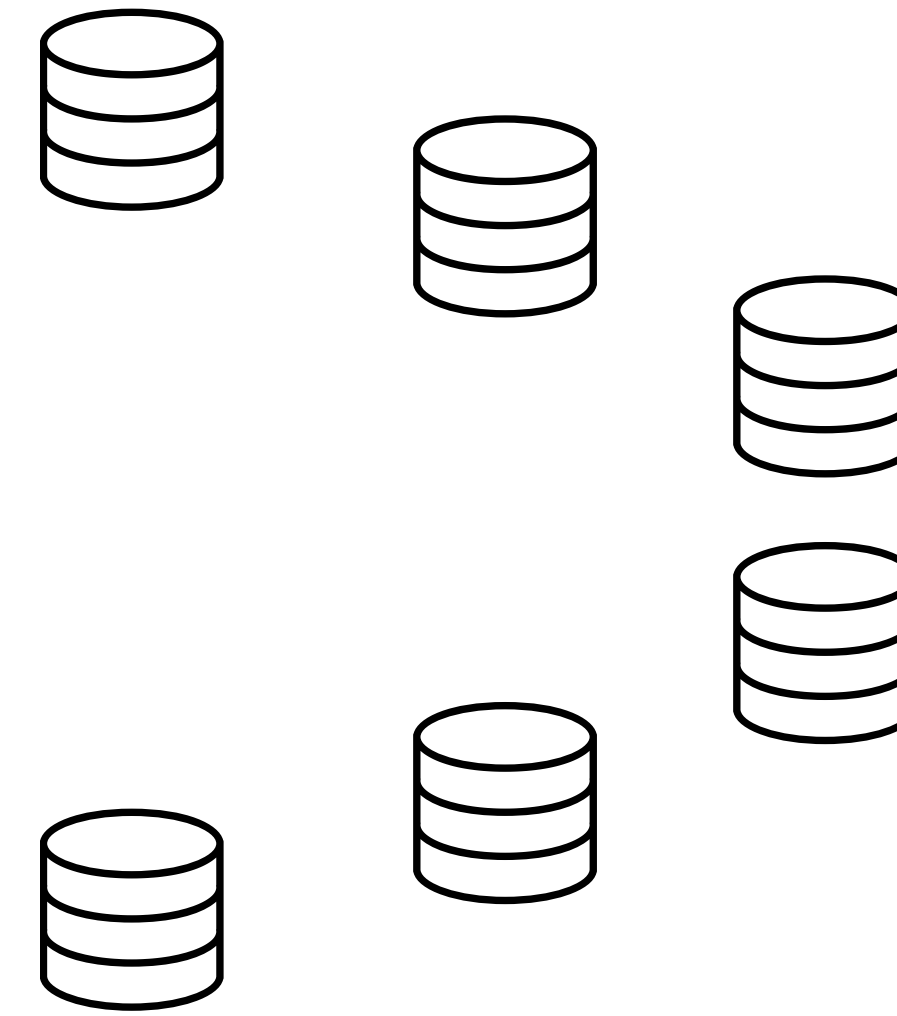
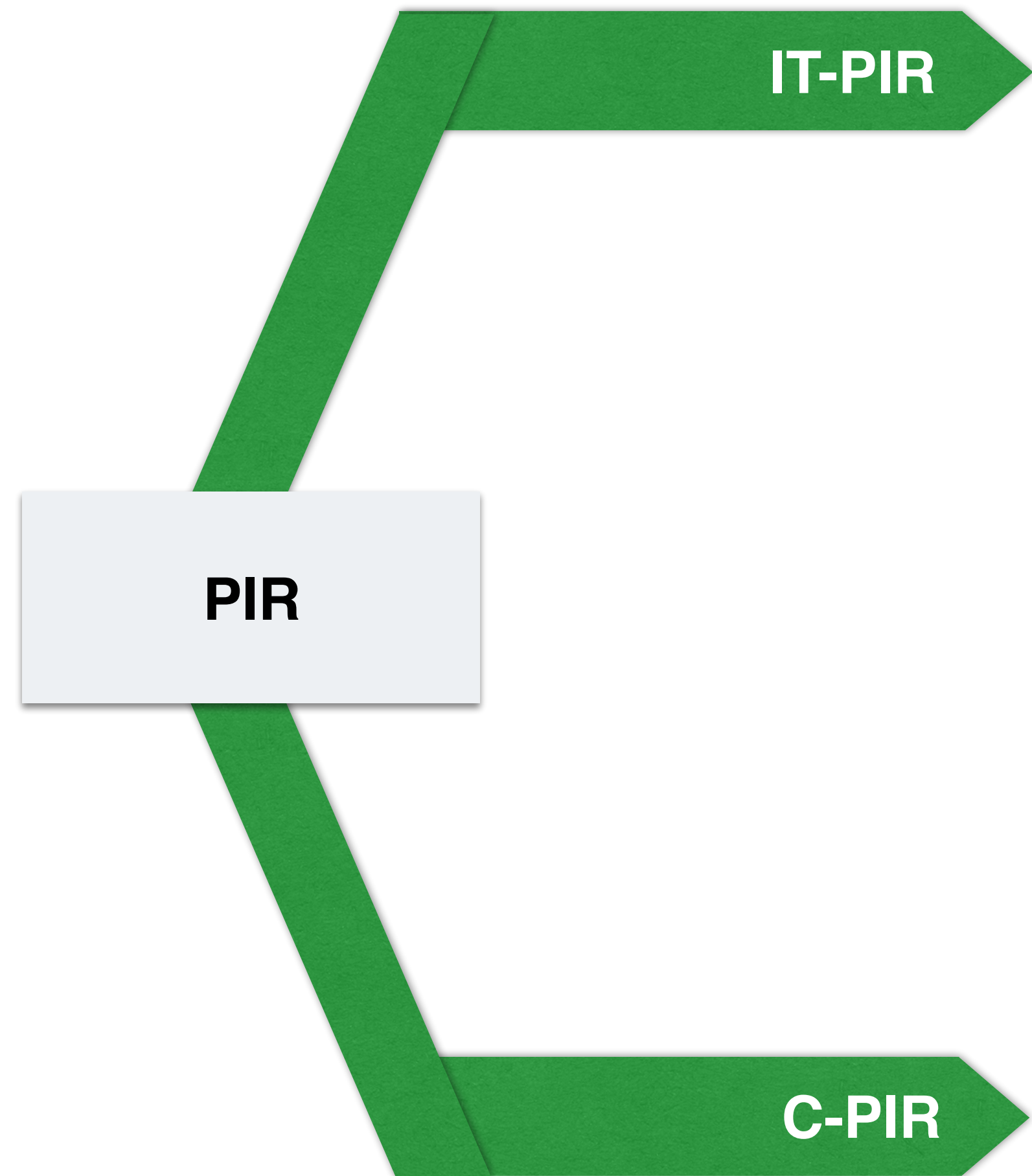
# PIR Versions



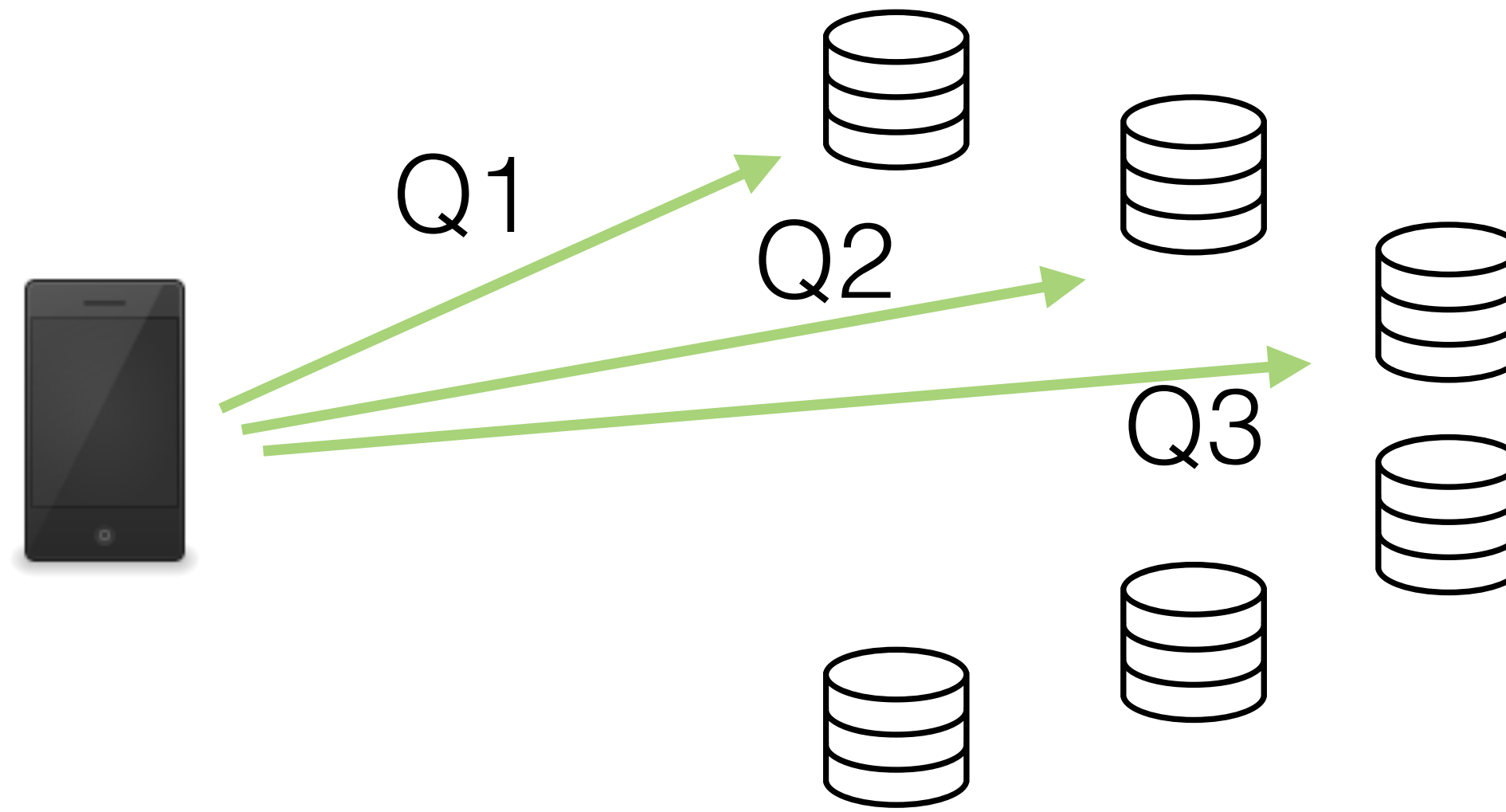
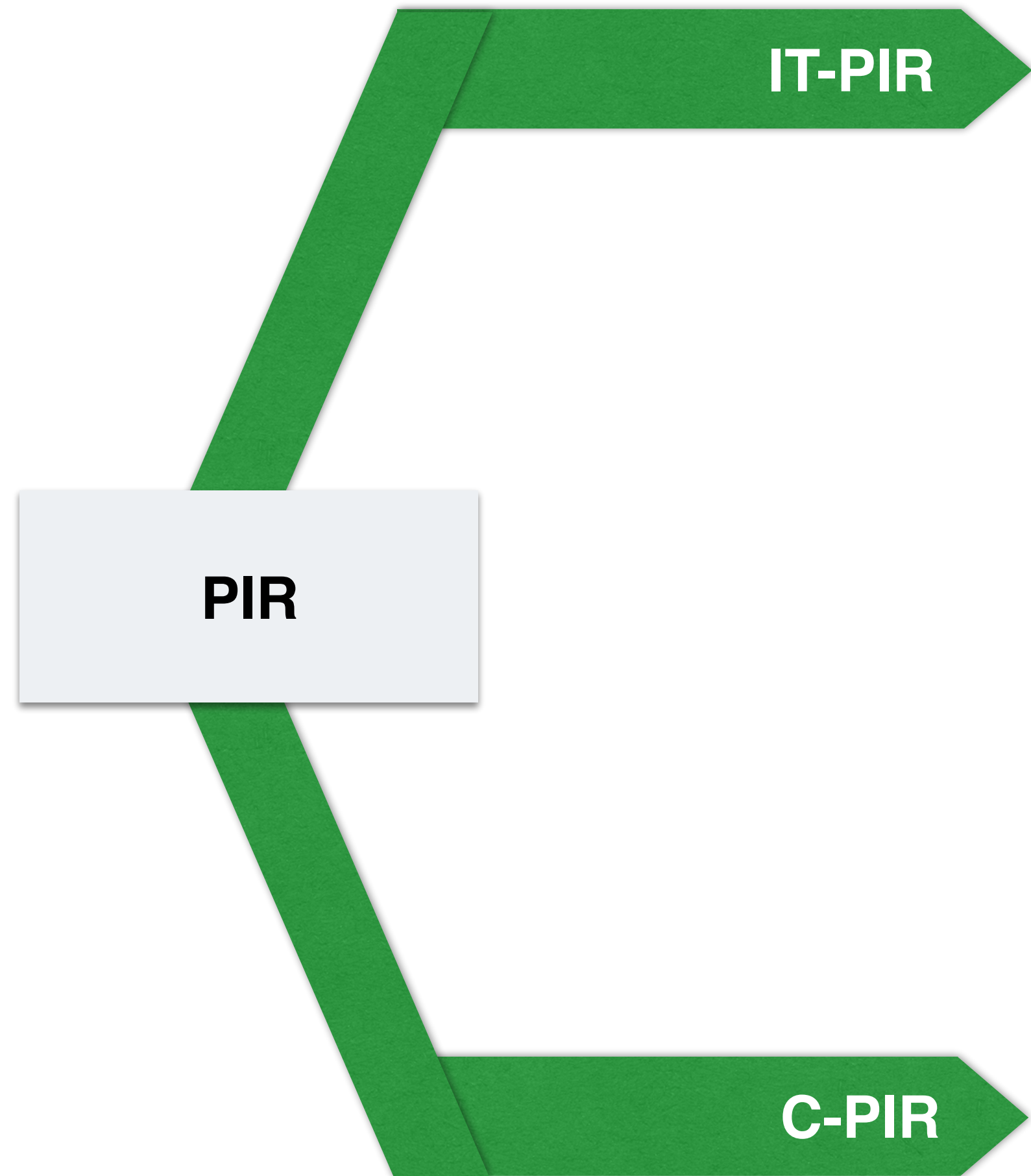
# PIR Versions



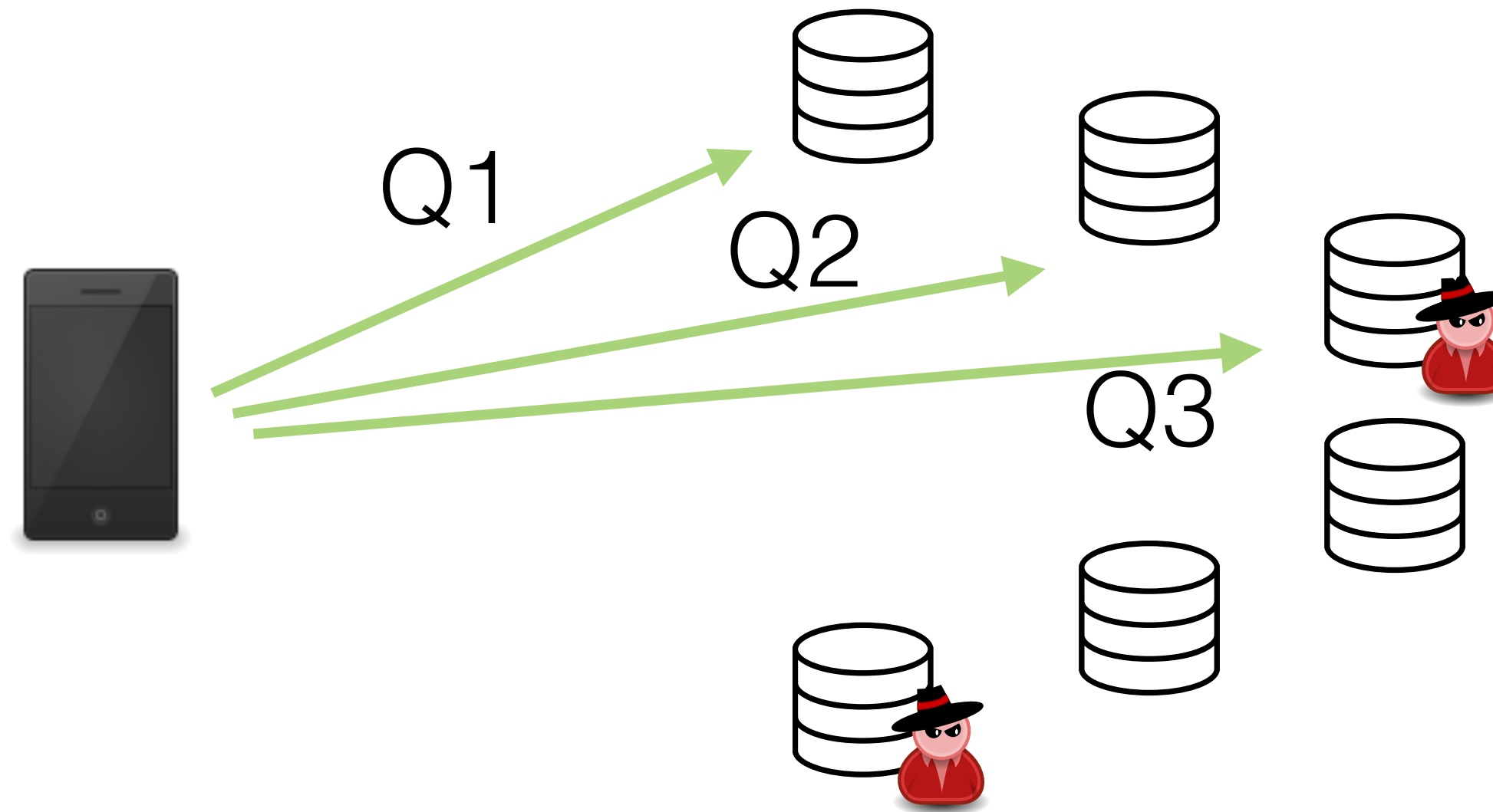
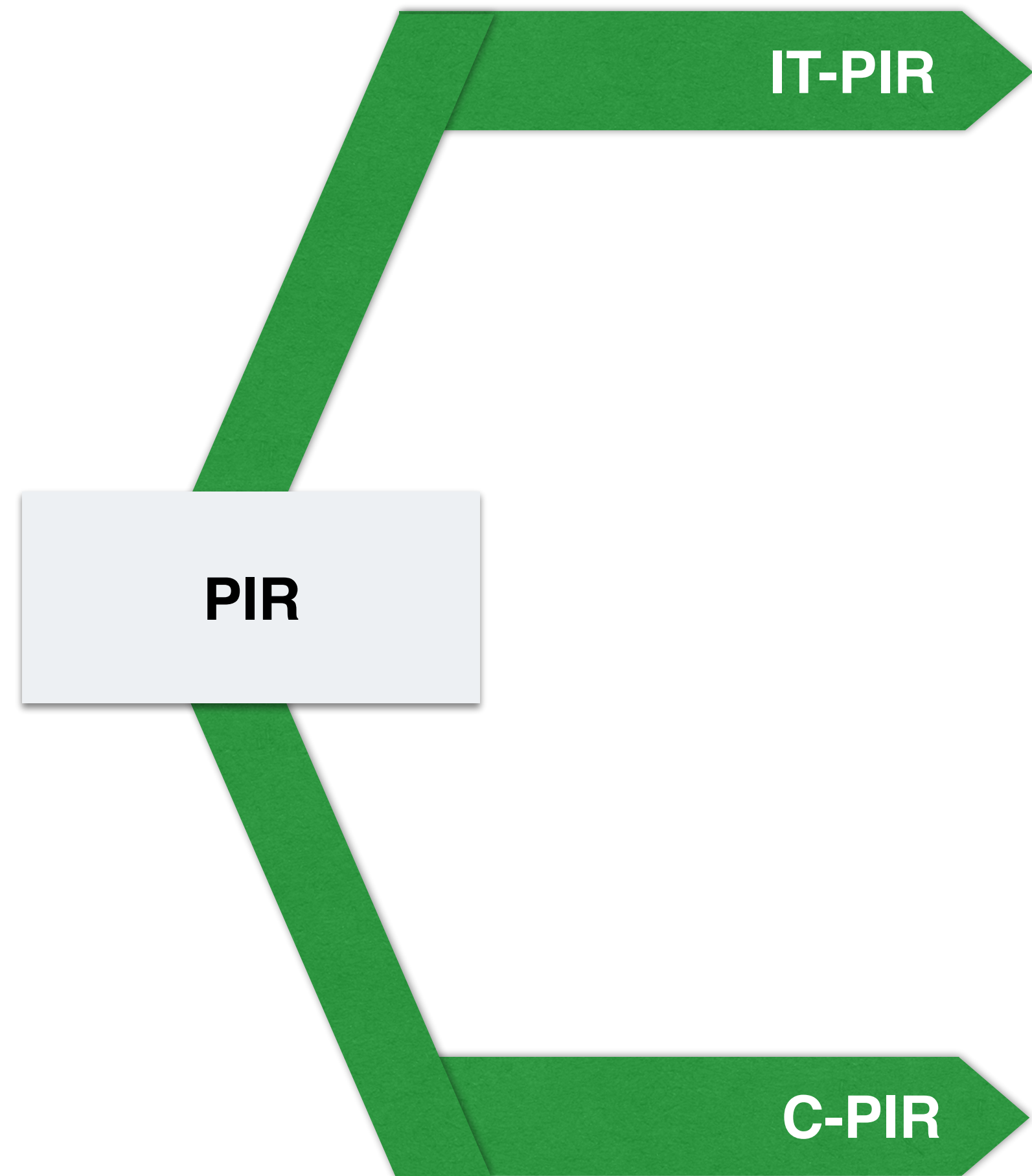
# PIR Versions



# PIR Versions

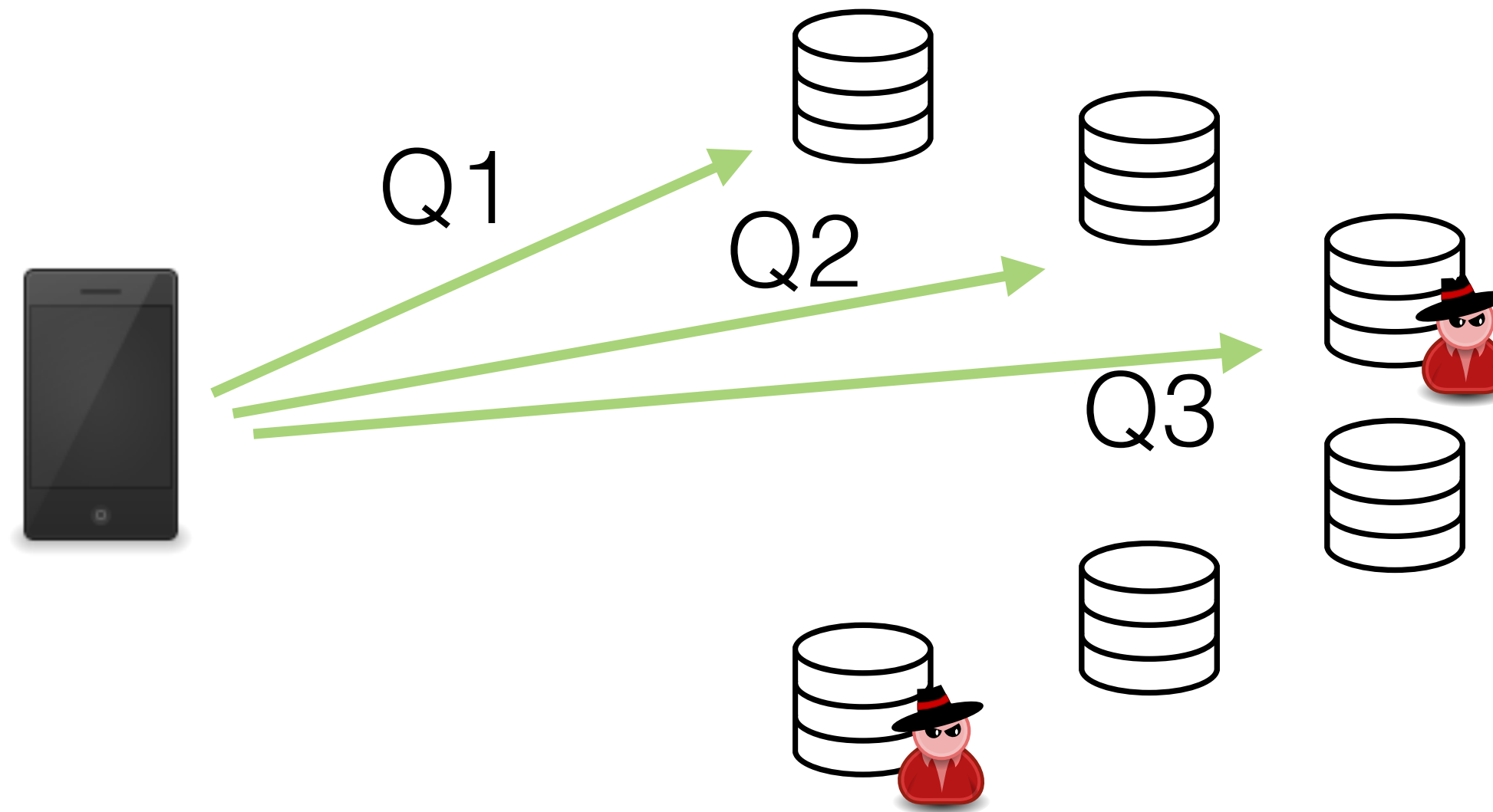
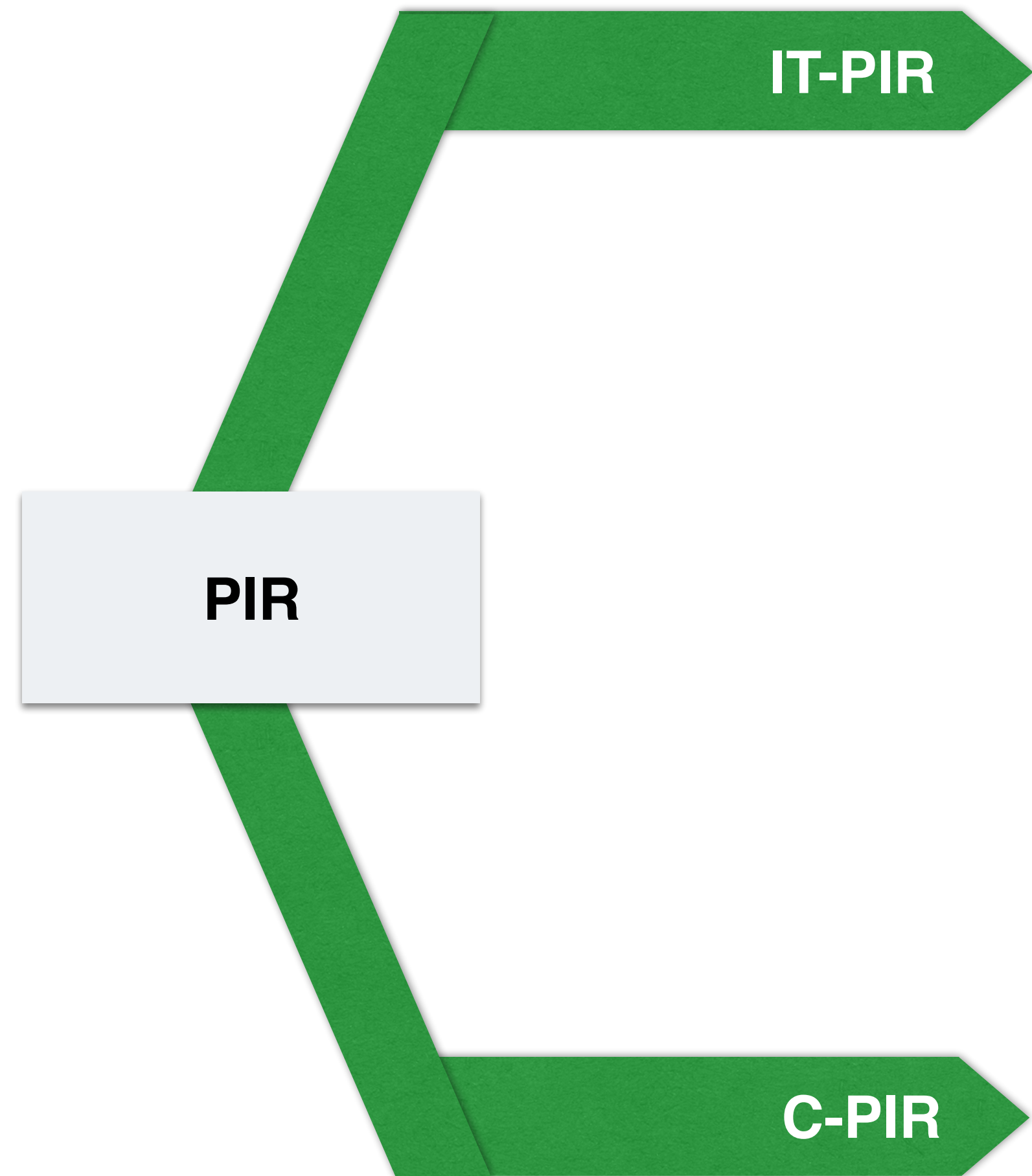


# PIR Versions

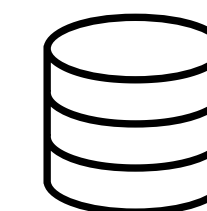


Information Theoretic security, assuming no collision up to a certain degree

# PIR Versions



Information Theoretic security, assuming no collision up to a certain degree



Computational PIR, query privacy via cryptographic means



# IT-PIR vs. C-PIR

	IT-PIR	C-PIR
Communication costs	Smaller	Bigger
Computation costs	Smaller	Bigger
Risk of Collusion	Server can mount sybil attack	Non existent
Robust to missing or incorrect server response	Robust	Non-robust

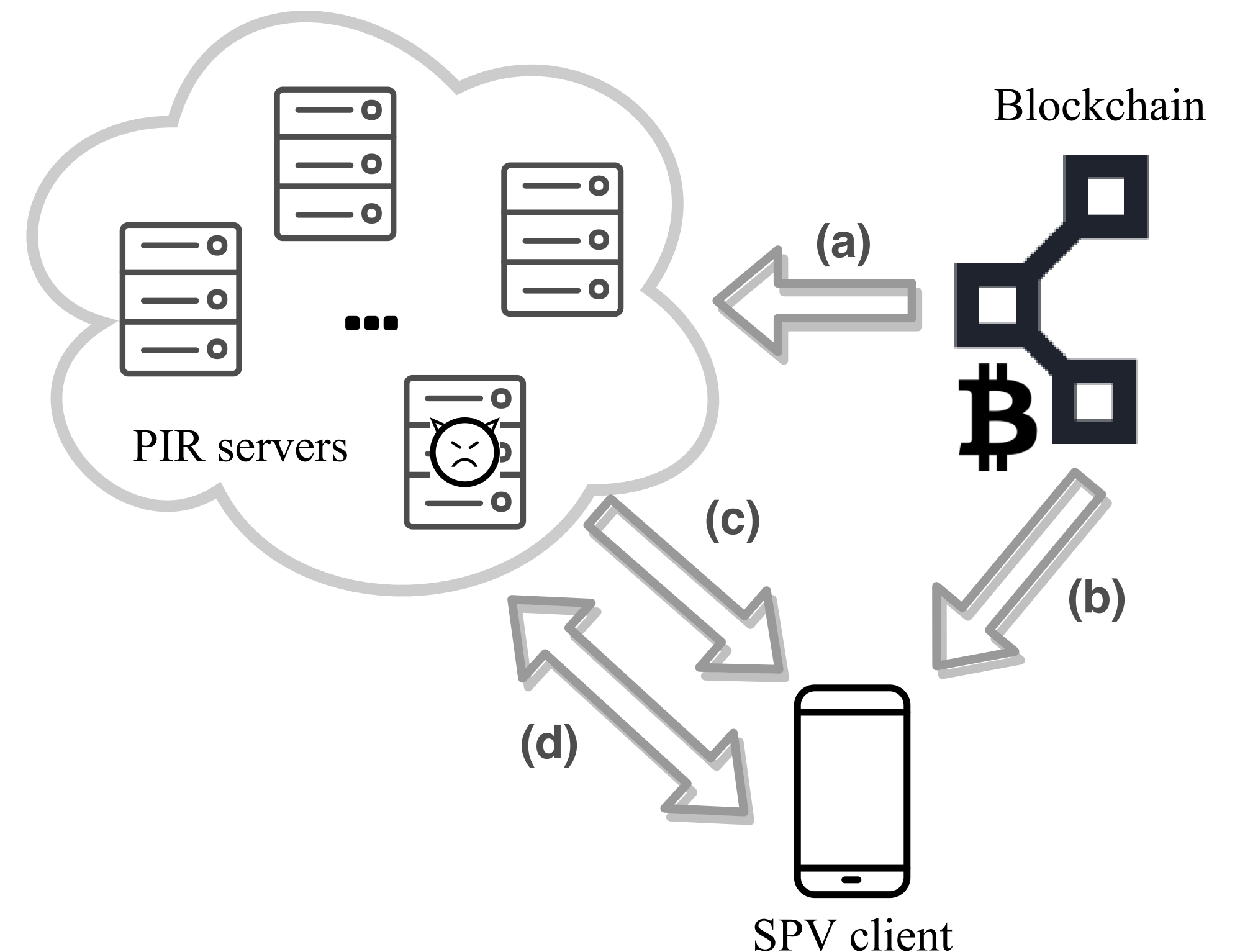
## The best of both worlds: Hybrid PIR

- combines the IT-PIR protocols with the C-PIR protocols
- queries are operated in a recursive way
- maintains partial privacy of client query information if the assumptions made by one of the inner protocols is broken
- open-source Percy++ library

Devet, C. and Goldberg, I., The best of both worlds: Combining information-theoretic and computational PIR for communication efficiency. PETS'14

# System Overview

- (a) PIR servers download the blockchain, constructs PIR databases. For each database, the PIR server creates a description file called manifest file.
- (b) The user collect all available block headers from e.g., full node peers.
- (c) The user fetch the manifest files from the PIR servers to later efficiently query the PIR database.
- (d) The user executes the PIR-SPV protocol, decodes the PIR responses for servers and then performs SPV validation



Devet, C. and Goldberg, I., The best of both worlds: Combining information-theoretic and computational PIR for communication efficiency. PETS'14

# Database structure

## Manifest files

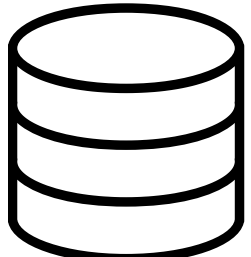
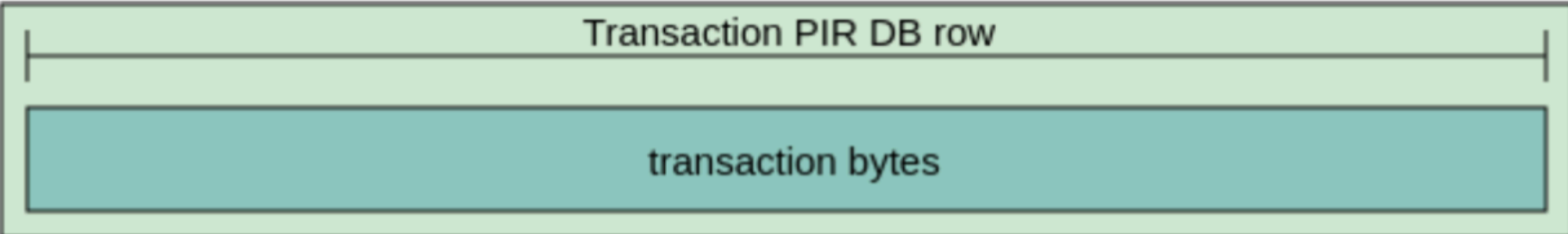
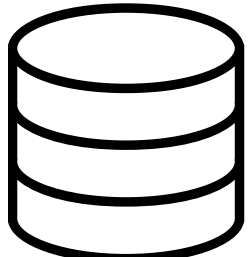
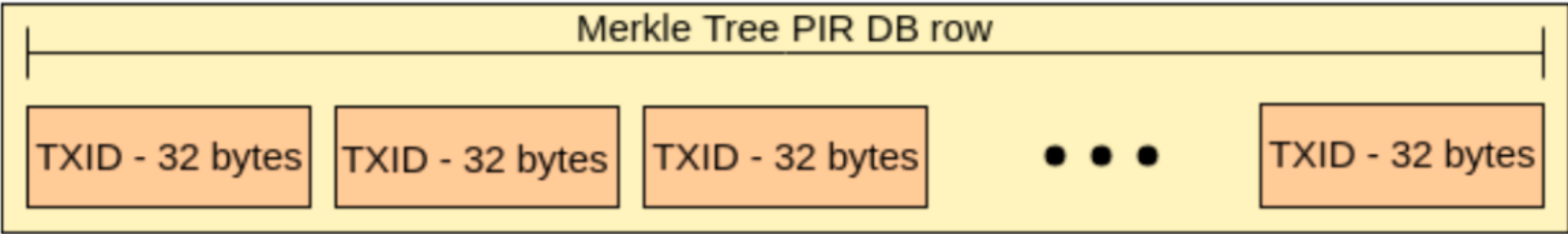
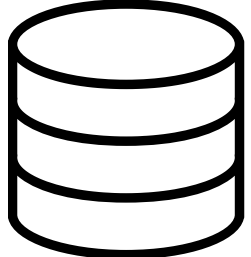
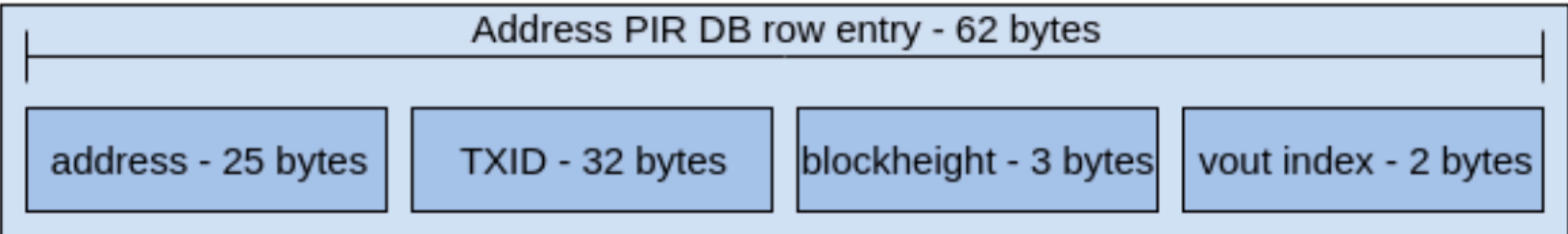
Address PIR Manifest

Merkle Tree PIR Manifest

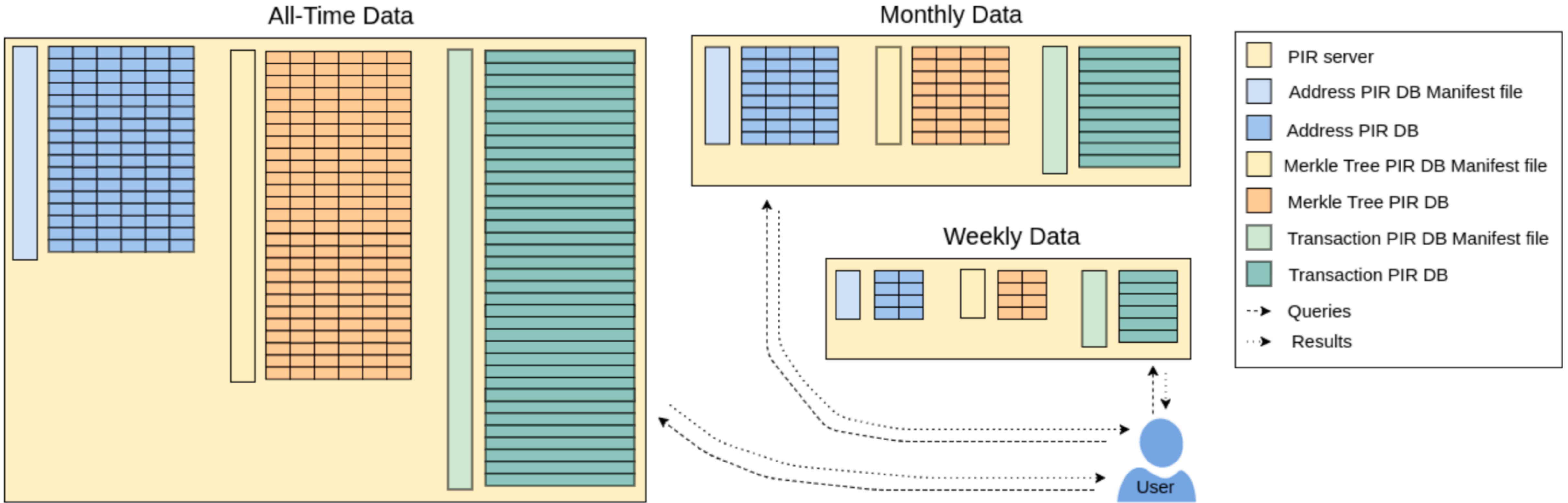
Transaction PIR Manifest

row/column  
→  
start/end

## PIR databases

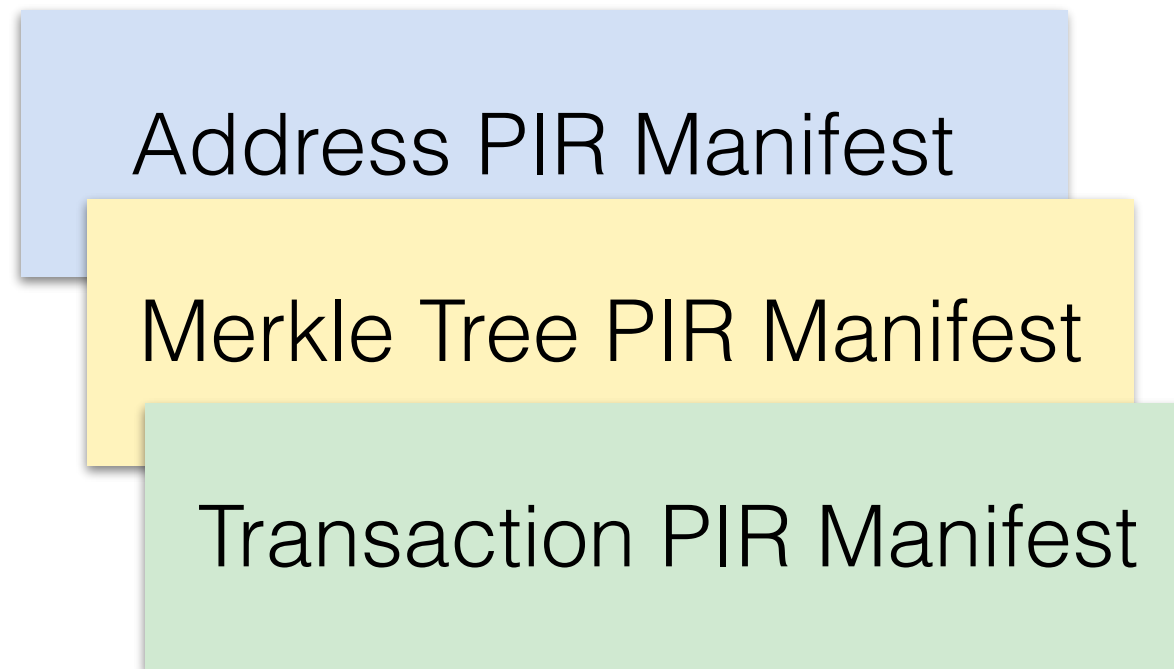


# Temporal Division



# PIR Protocol - Pre-requisites

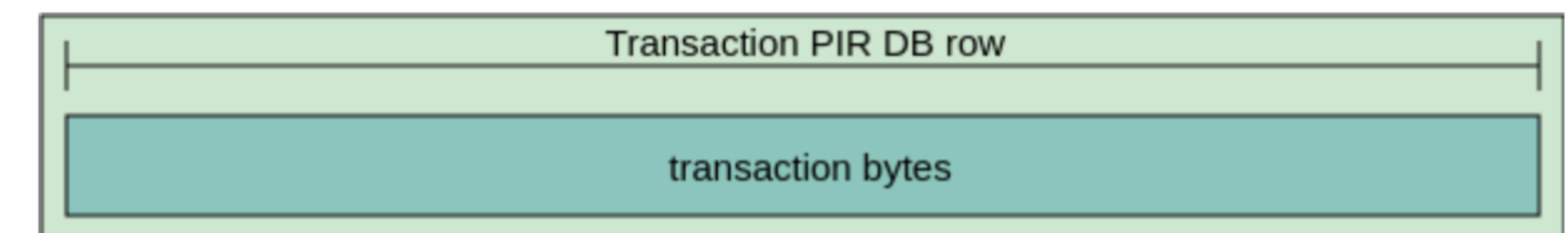
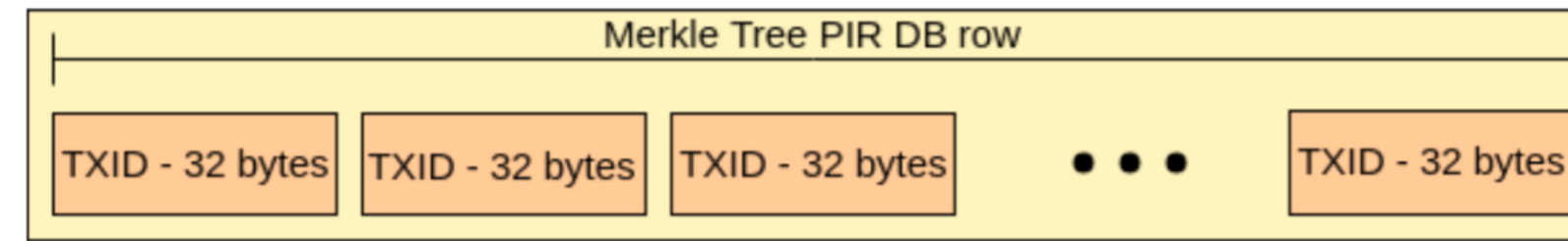
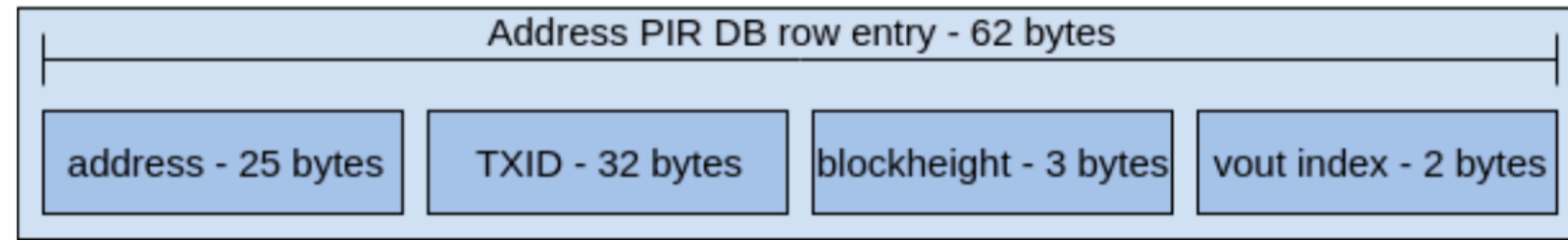
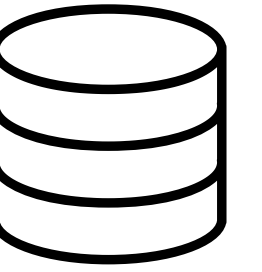
## 1) Download Manifest files



## 2) Download all Block Header

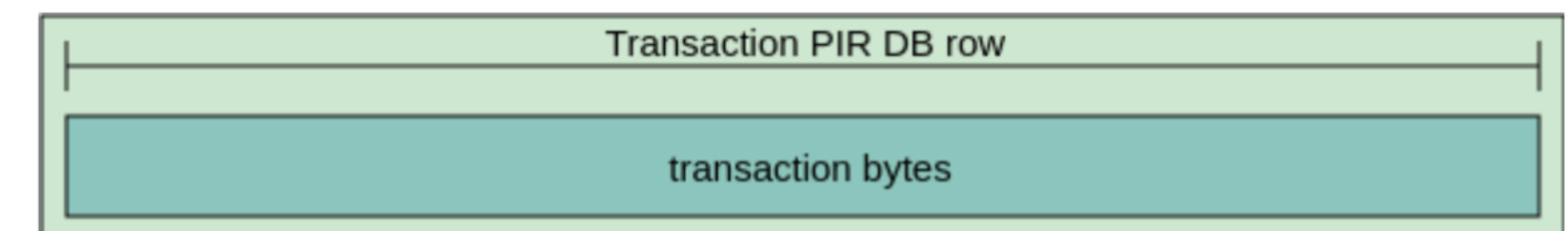
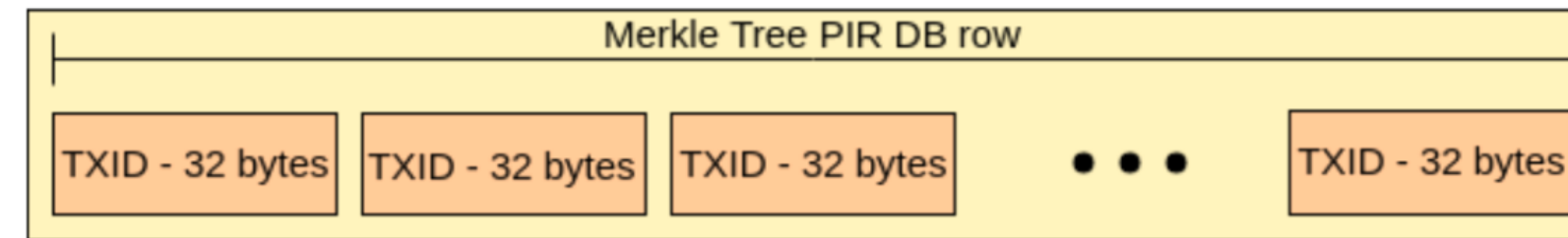
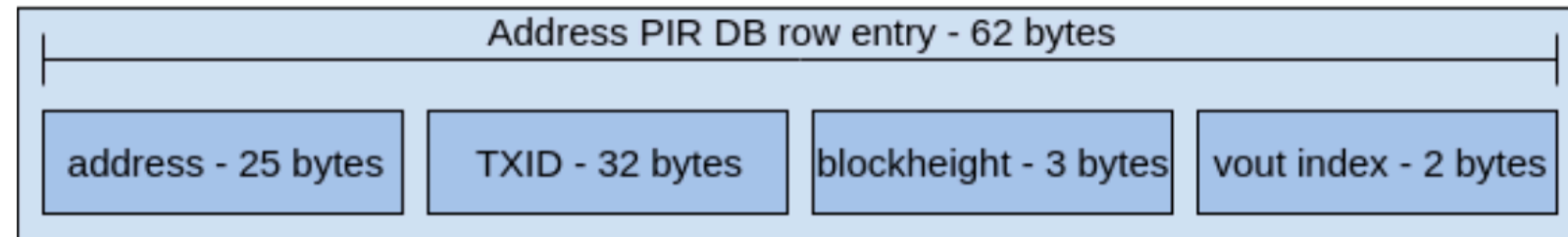
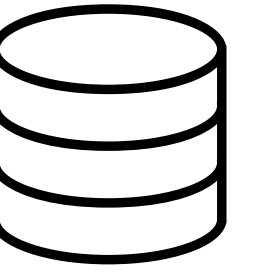


# PIR Protocol



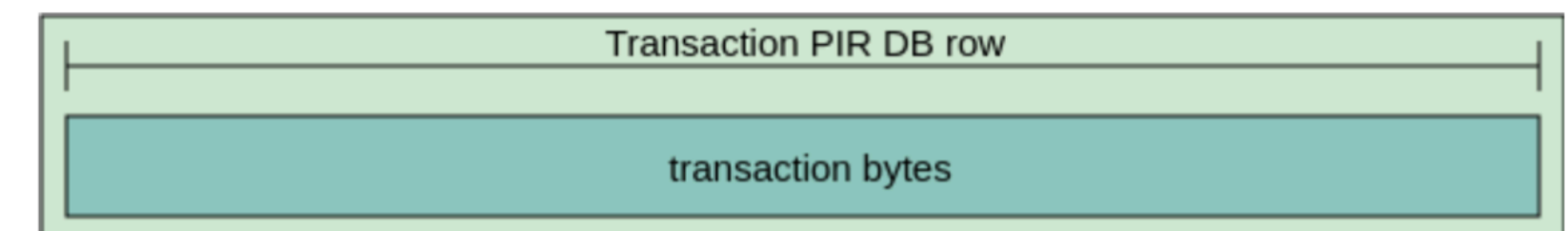
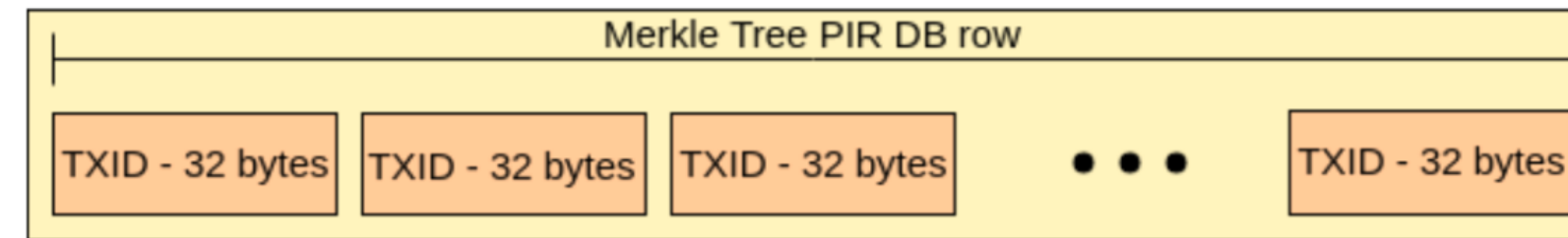
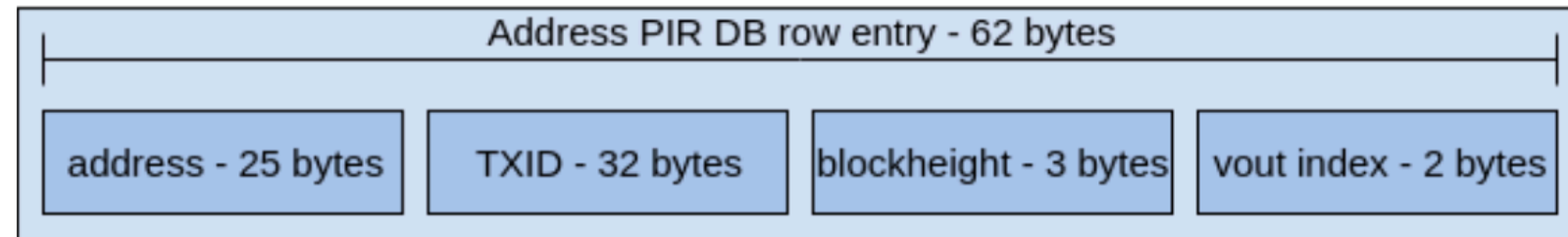
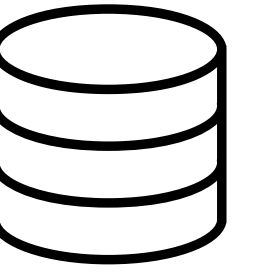


# PIR Protocol



Choose @

# PIR Protocol



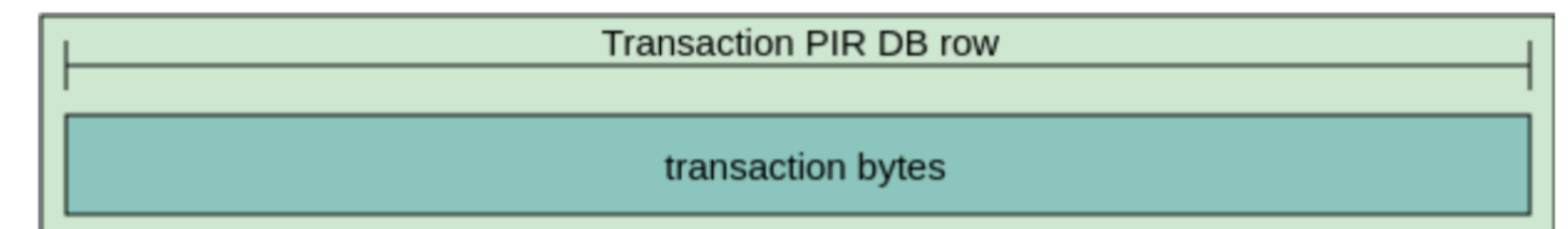
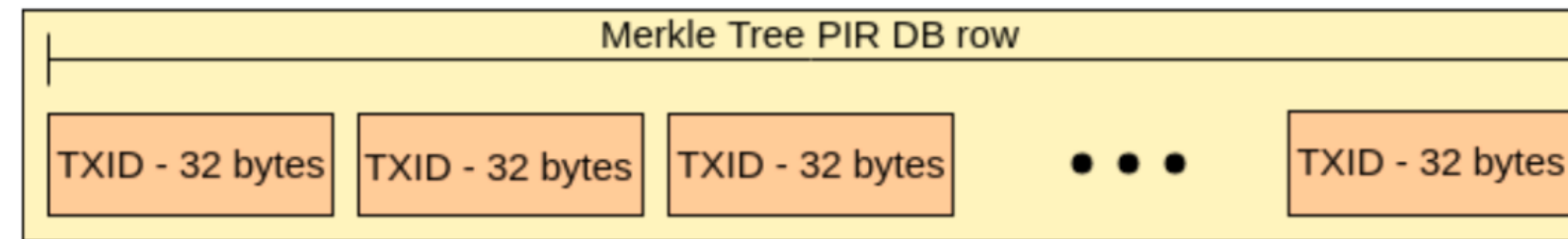
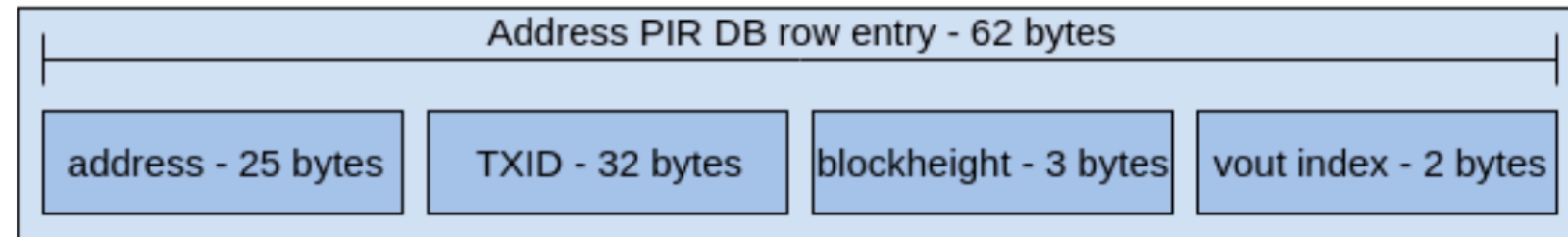
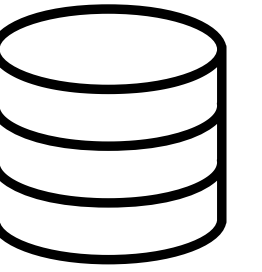
Choose @

Address PIR Manifest

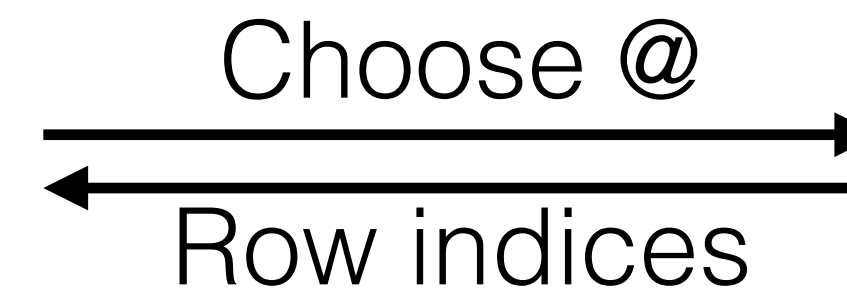
Merkle Tree PIR Manifest

Transaction PIR Manifest

# PIR Protocol



Choose @

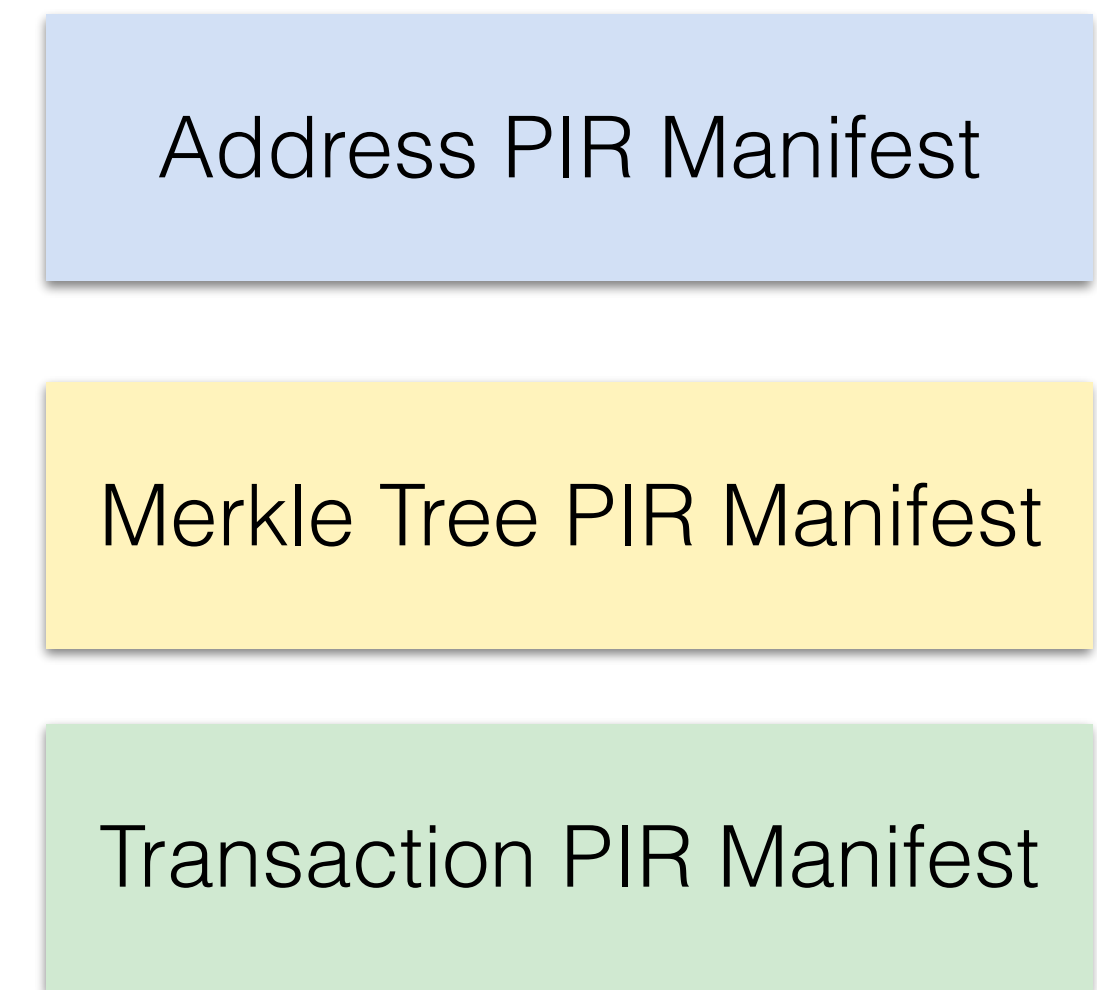
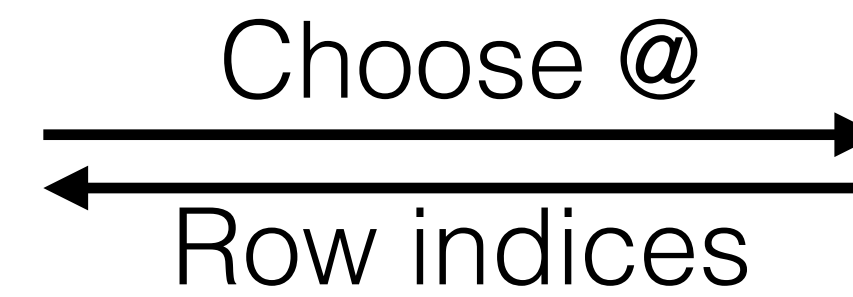
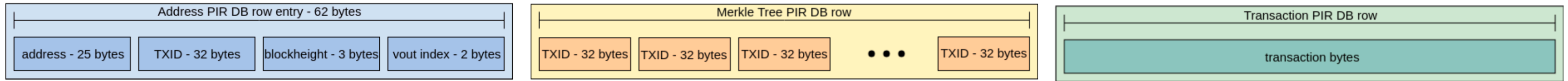
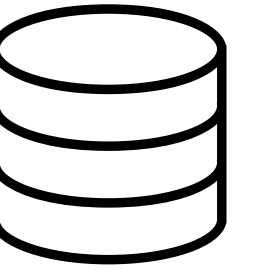


Address PIR Manifest

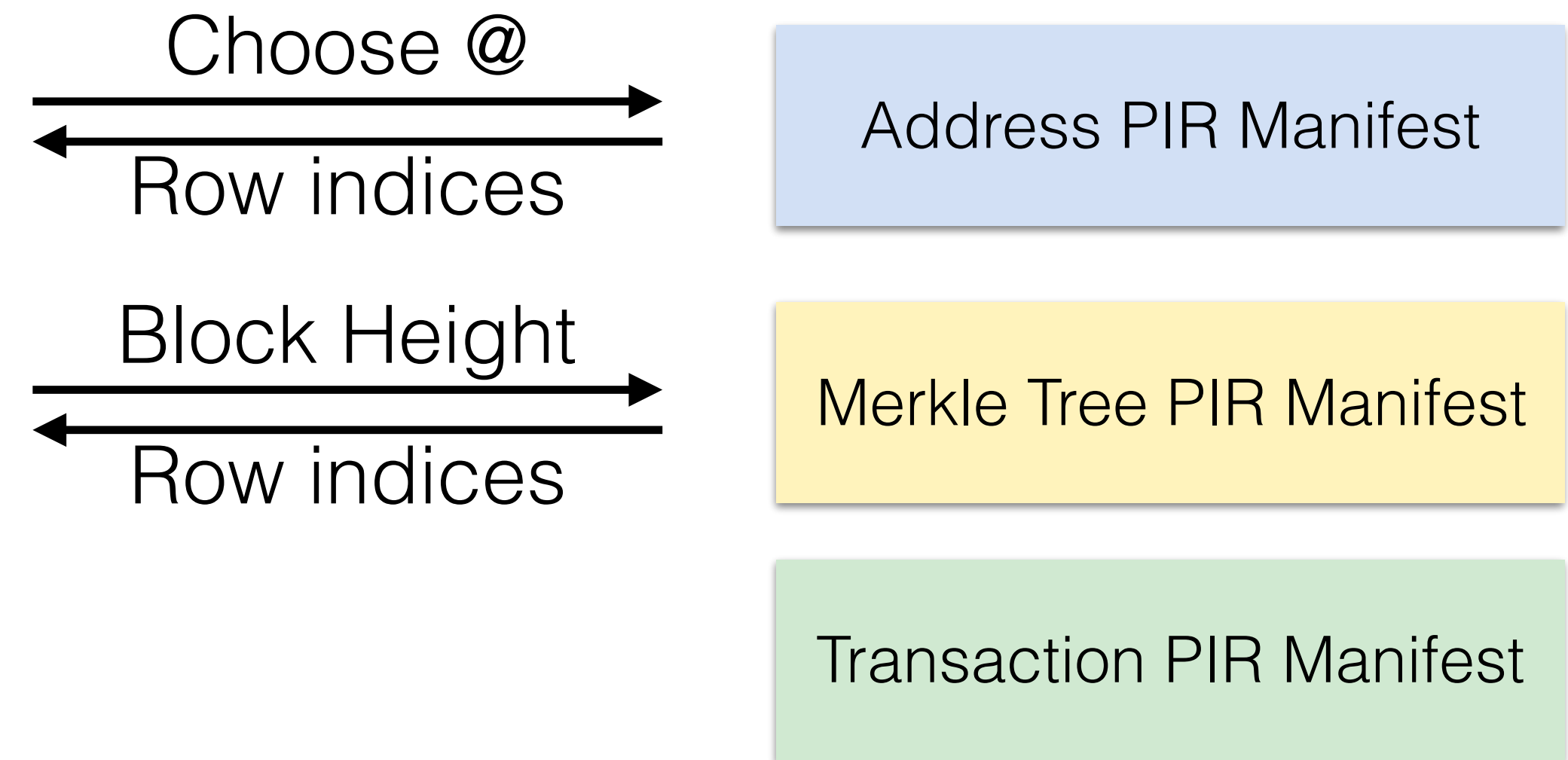
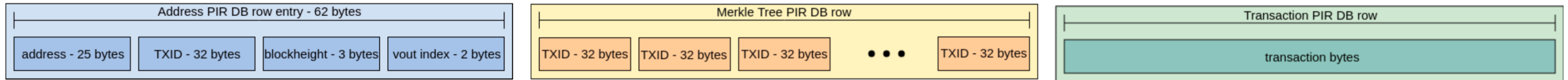
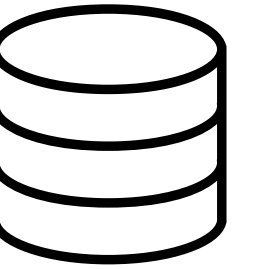
Merkle Tree PIR Manifest

Transaction PIR Manifest

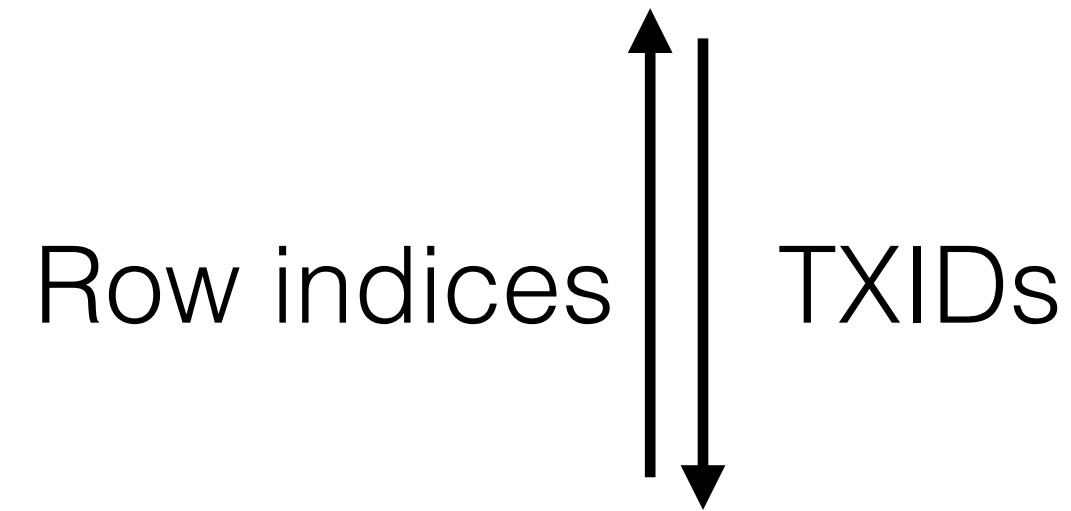
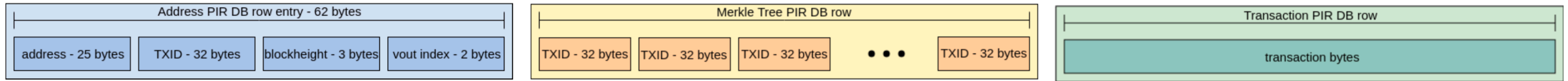
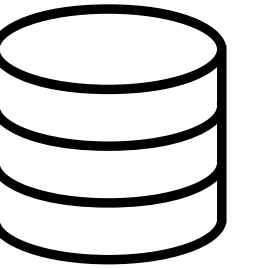
# PIR Protocol



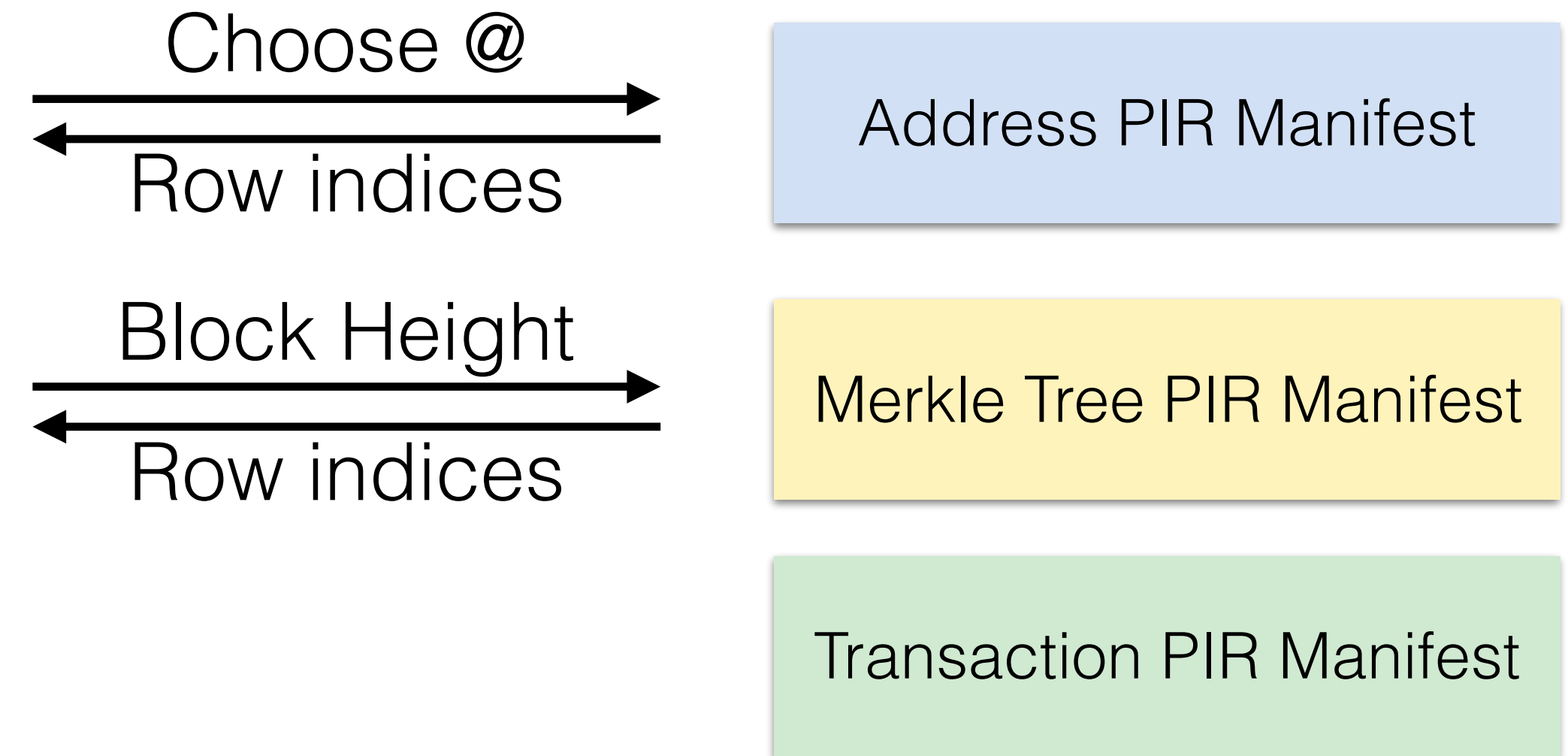
# PIR Protocol



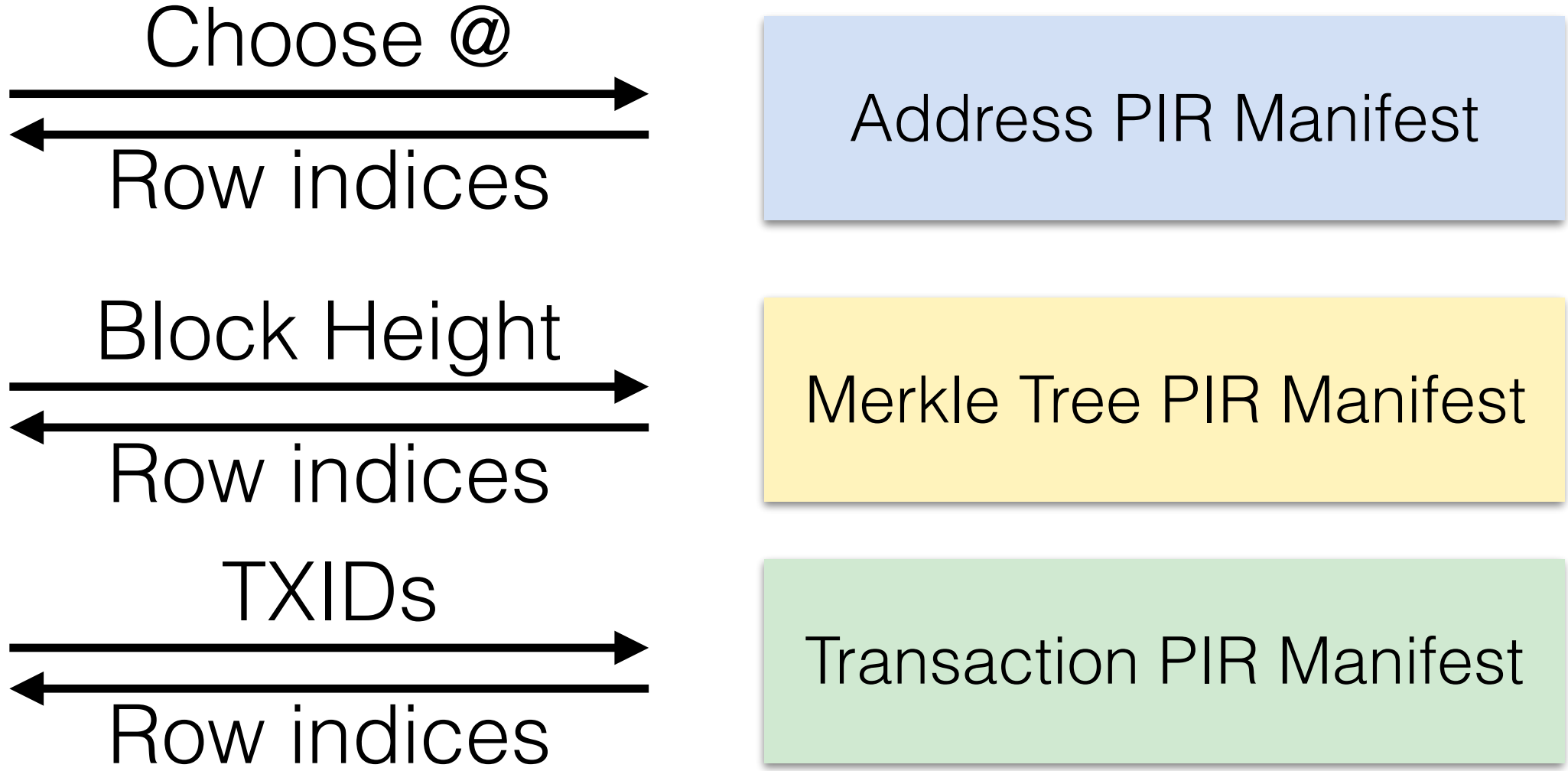
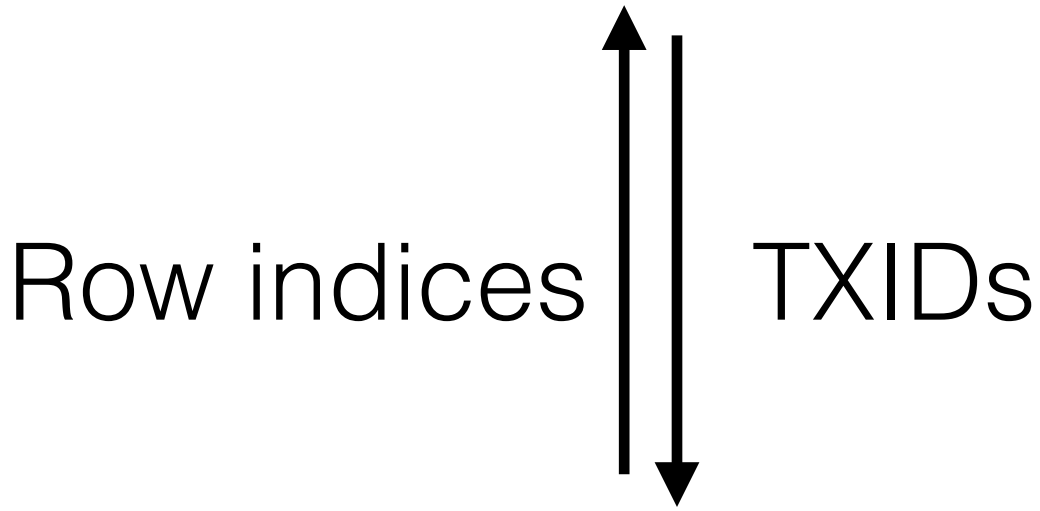
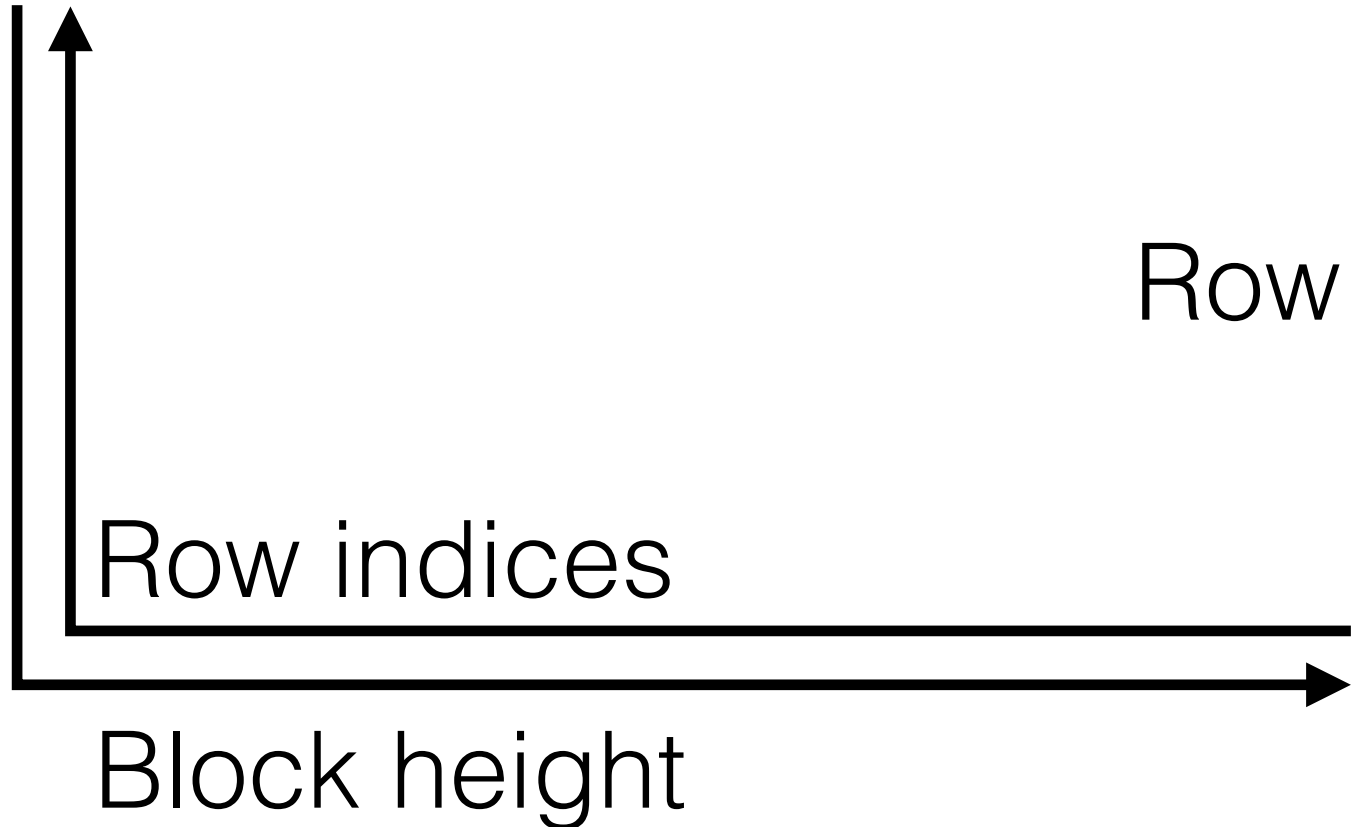
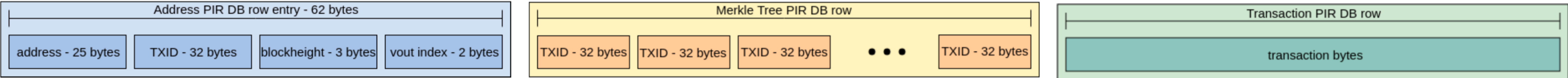
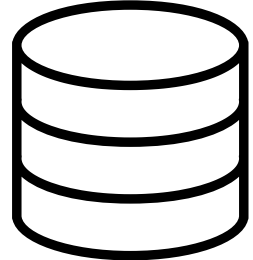
# PIR Protocol



Choose @

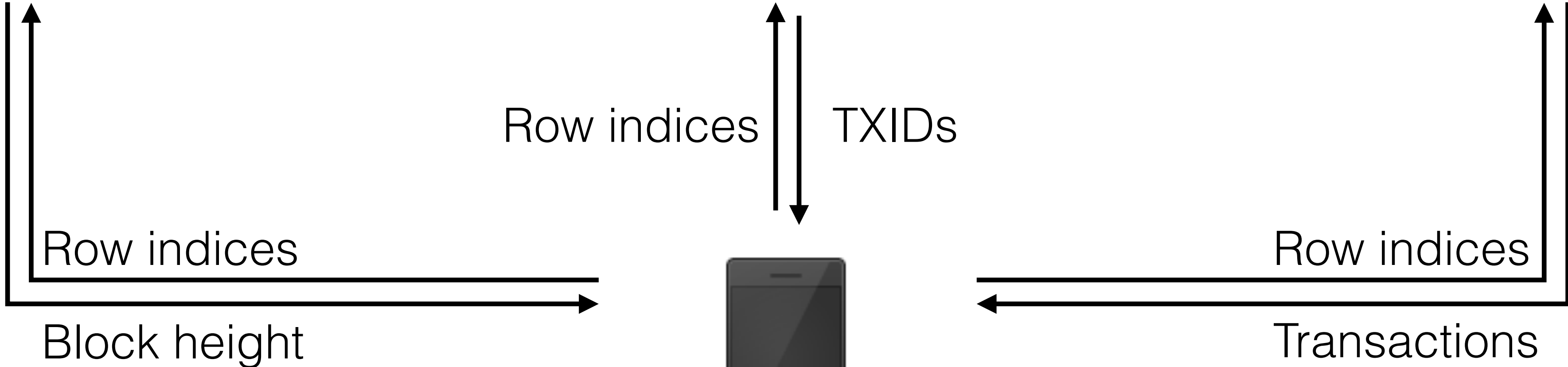
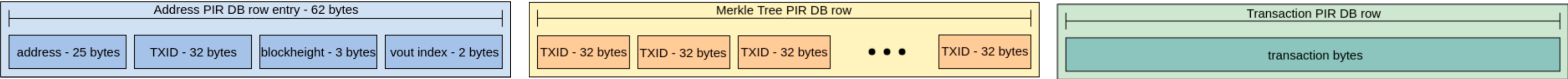
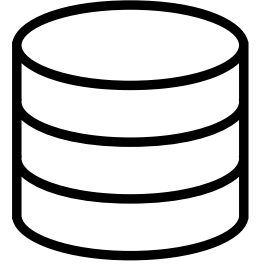


# PIR Protocol

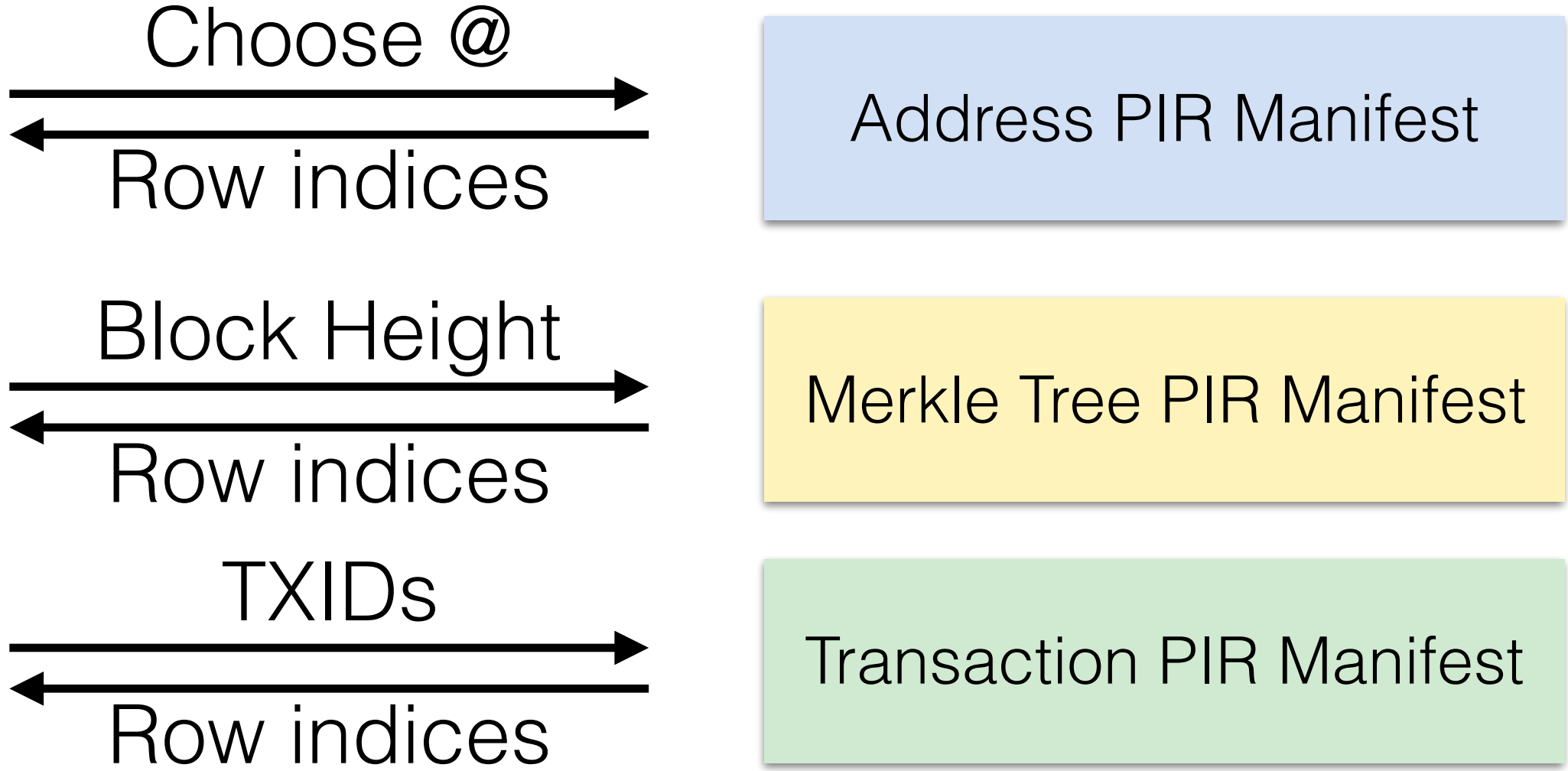




# PIR Protocol



Choose @



# PIR Protocol



# PIR Protocol



We have:

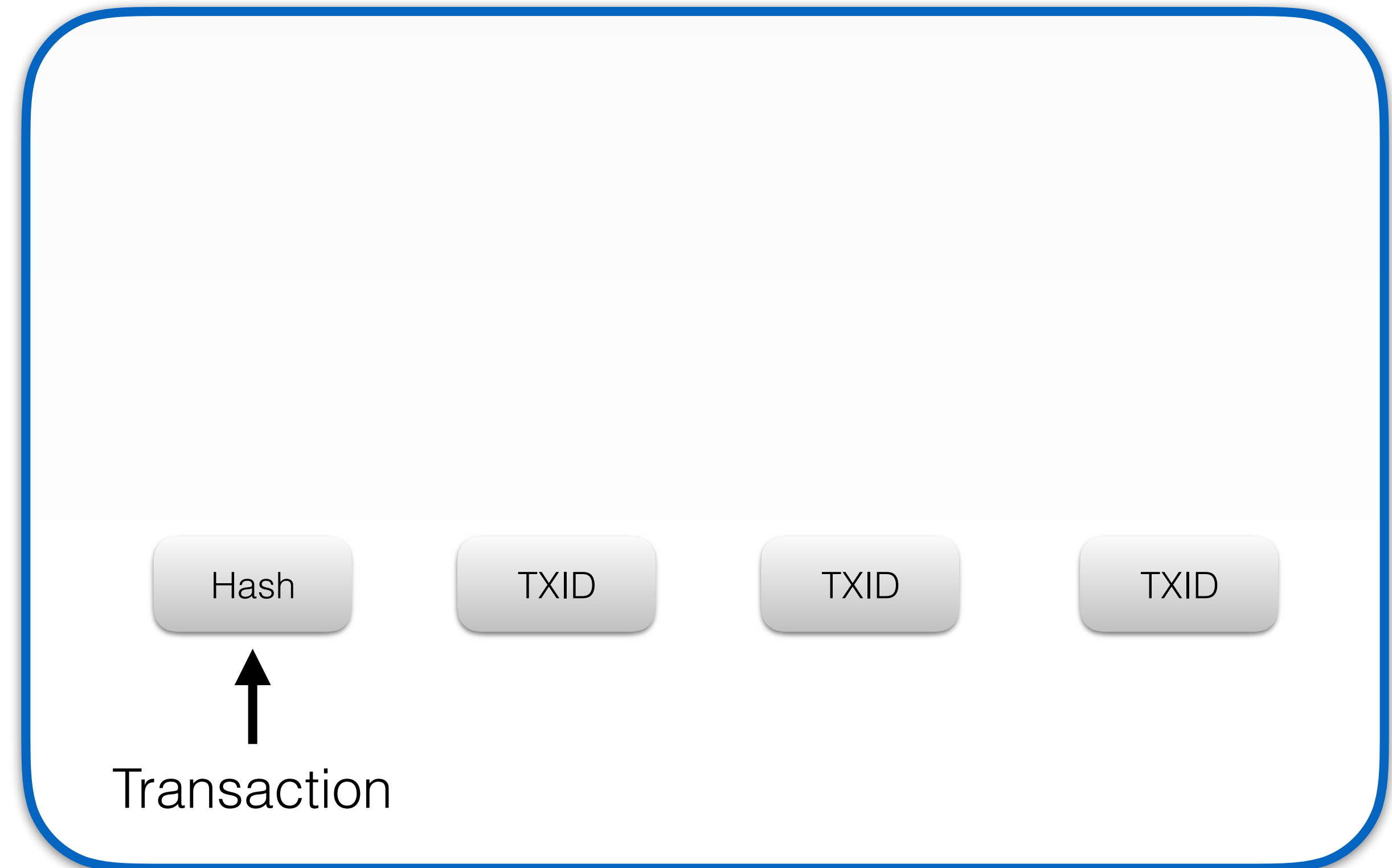
- Transaction IDs
- Block Headers
- Our raw transactions

# PIR Protocol



We have:

- Transaction IDs
- Block Headers
- Our raw transactions

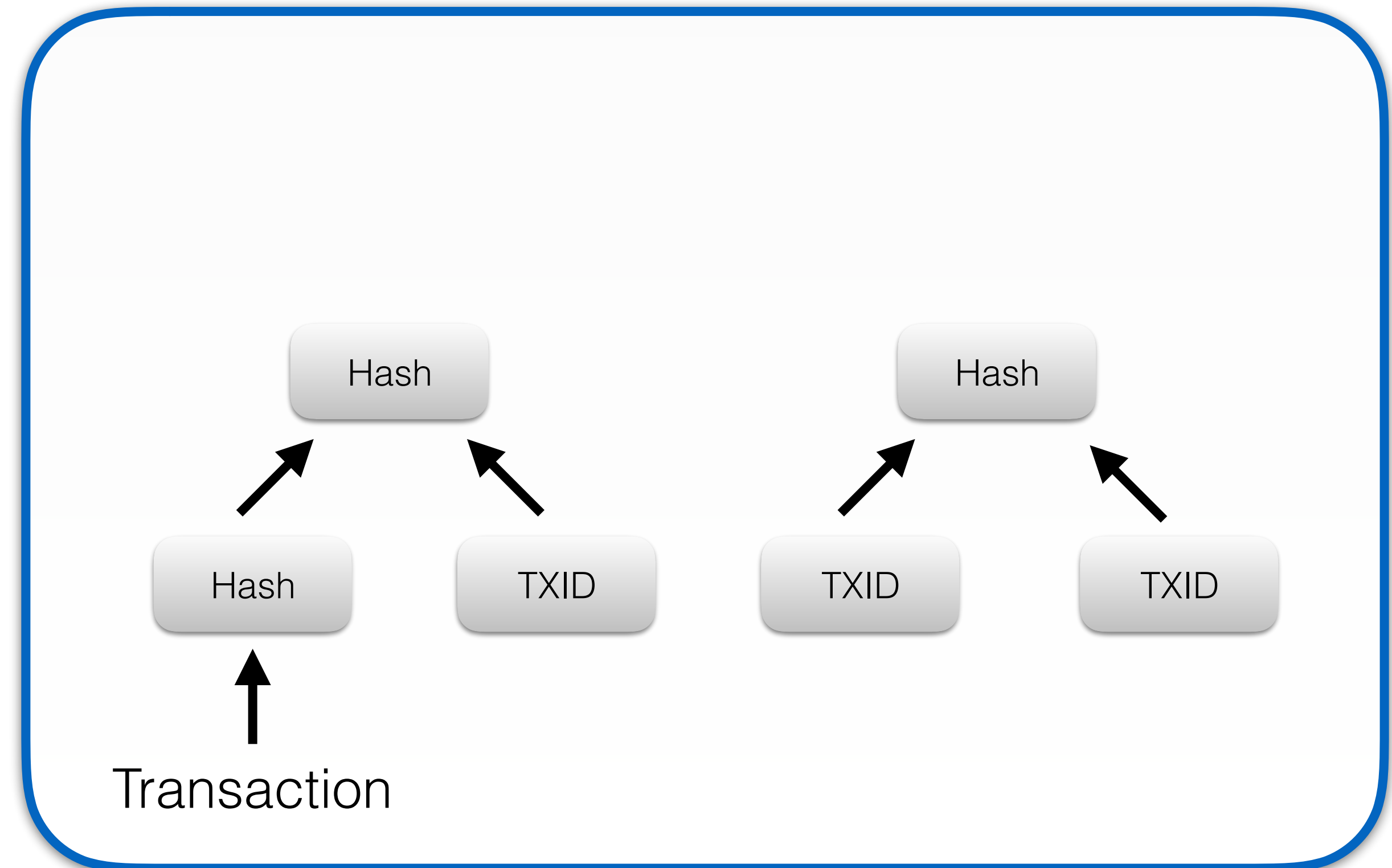


# PIR Protocol



We have:

- Transaction IDs
- Block Headers
- Our raw transactions

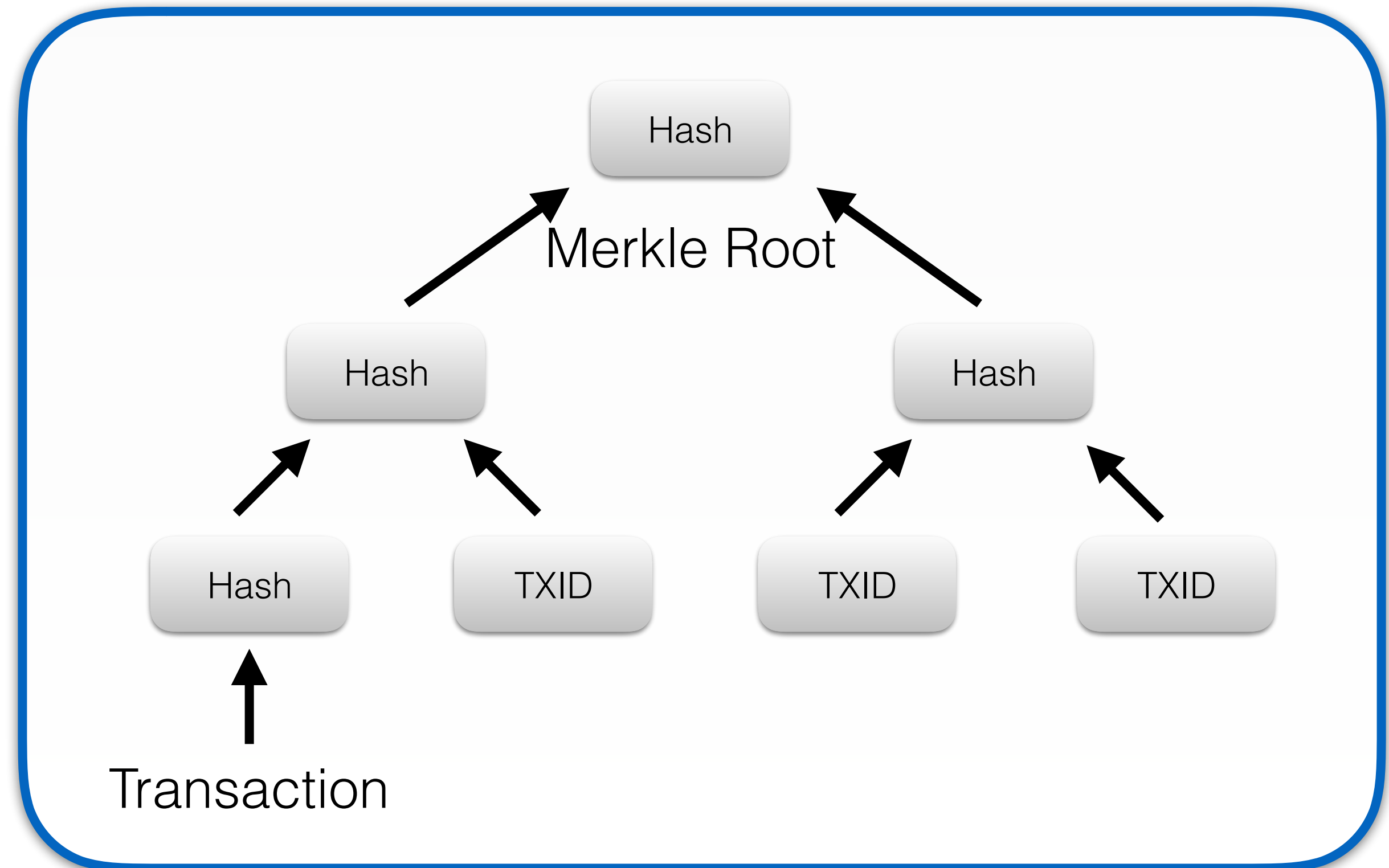


# PIR Protocol



We have:

- Transaction IDs
- Block Headers
- Our raw transactions



## Costs - PIR Database sizes

Bitcoin Data — Block 1~ 513502 (March 2018)

		All-Time blocks 1 to 508462	Monthly blocks 508463 to 512494	Weekly blocks 512495 to 513502
Address PIR DBs	Total size of DB	3.16 GB	176.04 MB	59.11 MB
	Size of manifest file	65.99 MB	175.33 MB	66.97 MB
Merkle Tree PIR DBs	Total size of DB	10.18 GB	1.46 GB	1.44 GB
	Size of manifest file	40.90 MB	0.32 MB	78.62 KB
Transaction PIR DBs	Total size of DB	15.87 GB	1.30 GB	448.91 MB
	Size of manifest file	3.03 GB	218.68 MB	72.45 MB

Platform — Ubuntu 16.04 (64-bit) OS, Intel Core i7 3.4 GHz CPU, 16 GB of RAM and a 512 GB hard drive

# Manifest File Trie Scheme

- ◆ In some cases, manifest files are very big
- ◆ Transform the simple manifest files into a format suitable for PIR queries.
- ◆ Clients perform interpolation search on these manifest files, under PIR.

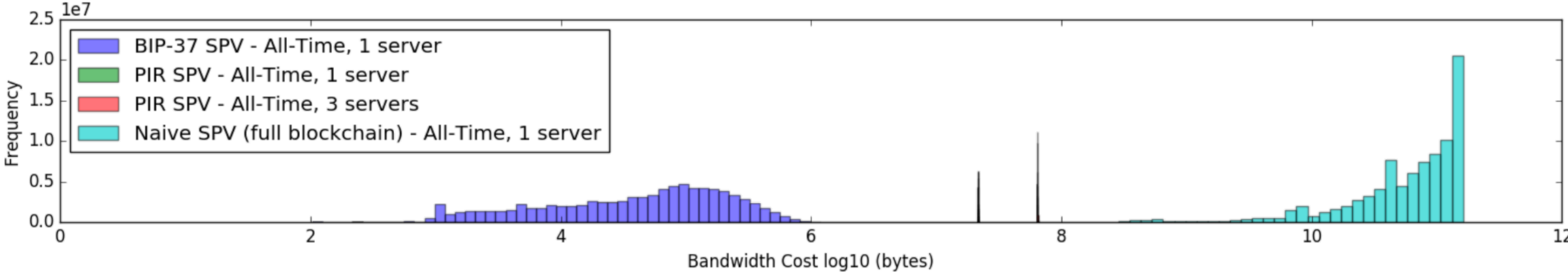


## Bandwidth comparison to verify a single transaction

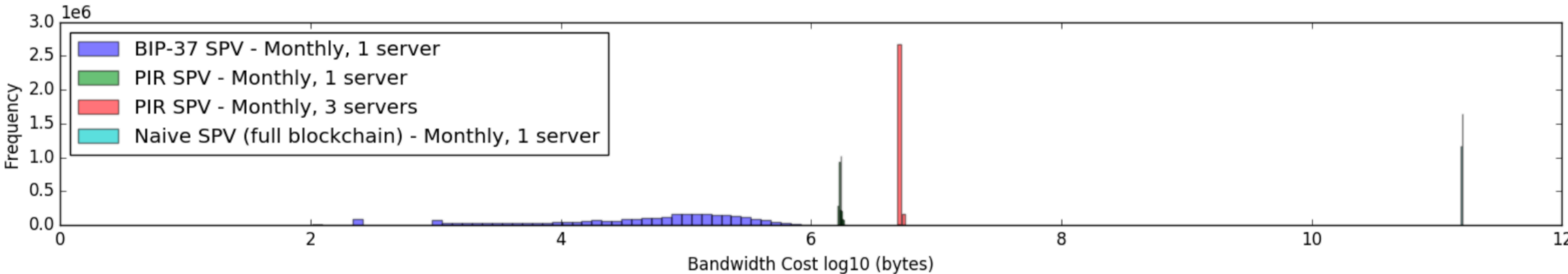
	BIP-37	PIR: 1 server	PIR: 3 servers	Naive SPV
All-Time	102.80 KB	21.54 MB	64.61 MB	80.27 GB
Monthly	132.43 KB	1.70 MB	5.11 MB	159.19 GB
Weekly	128.52 KB	666.07 KB	2.00 MB	161.47 GB

Platform — Ubuntu 16.04 (64-bit) OS, Intel Core i7 3.4 GHz CPU, 16 GB of RAM and a 512 GB hard drive

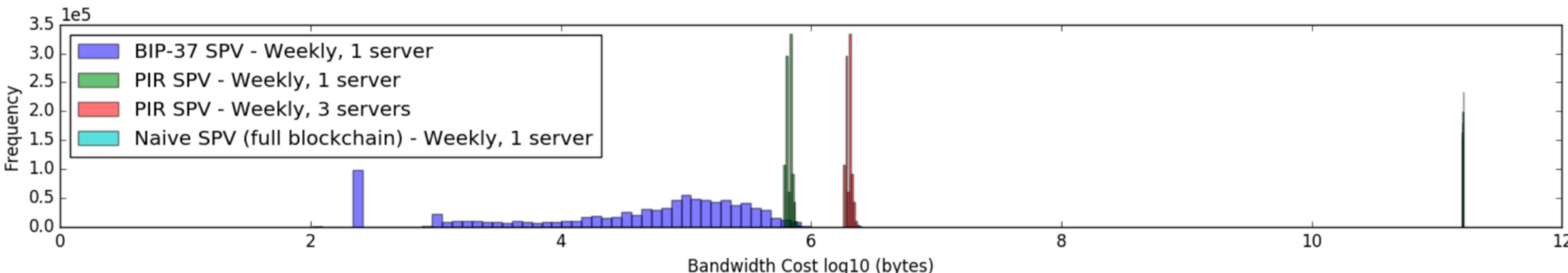
# Bandwidth costs to verify a single transaction



(a) All-Time

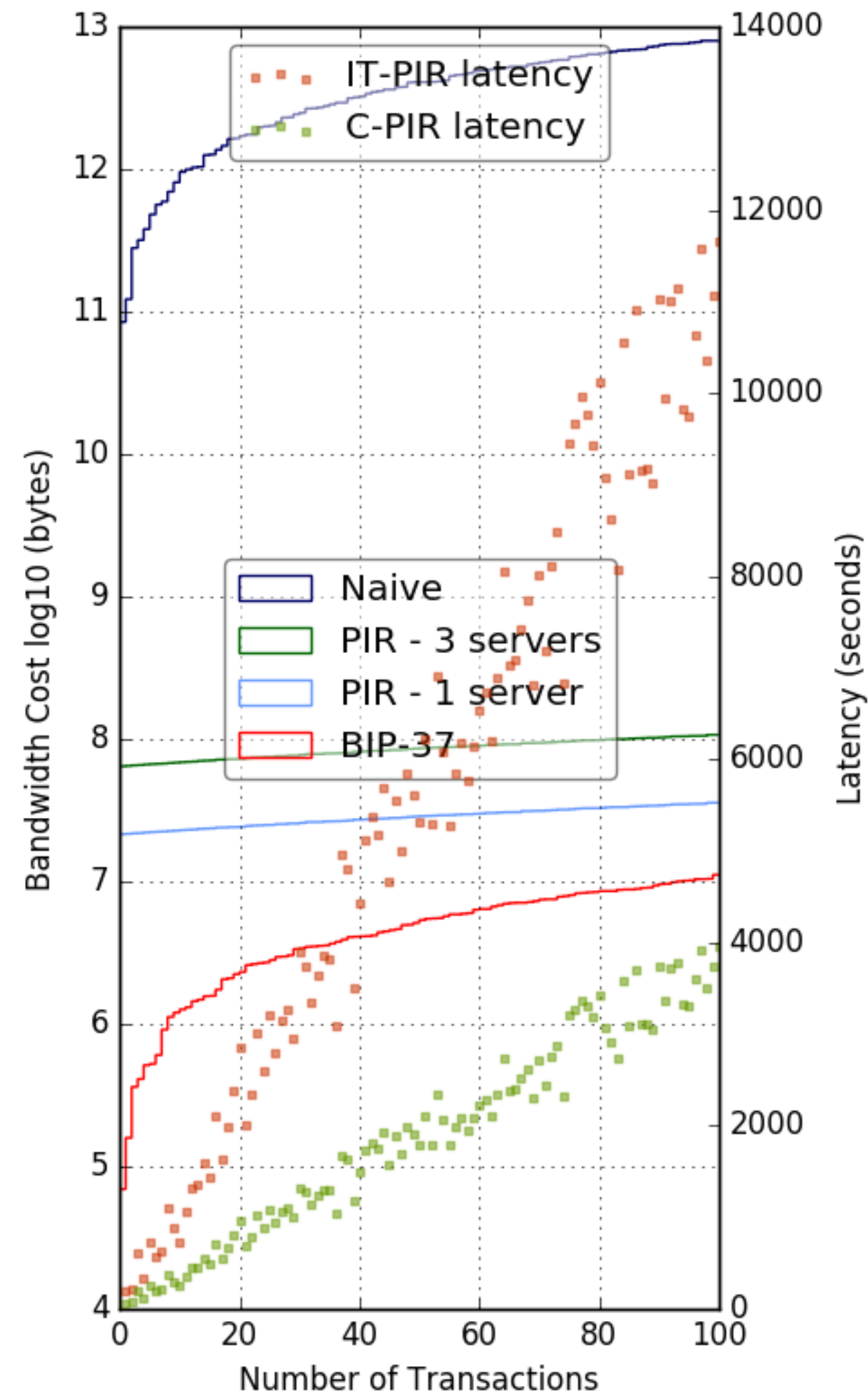


(b) Monthly

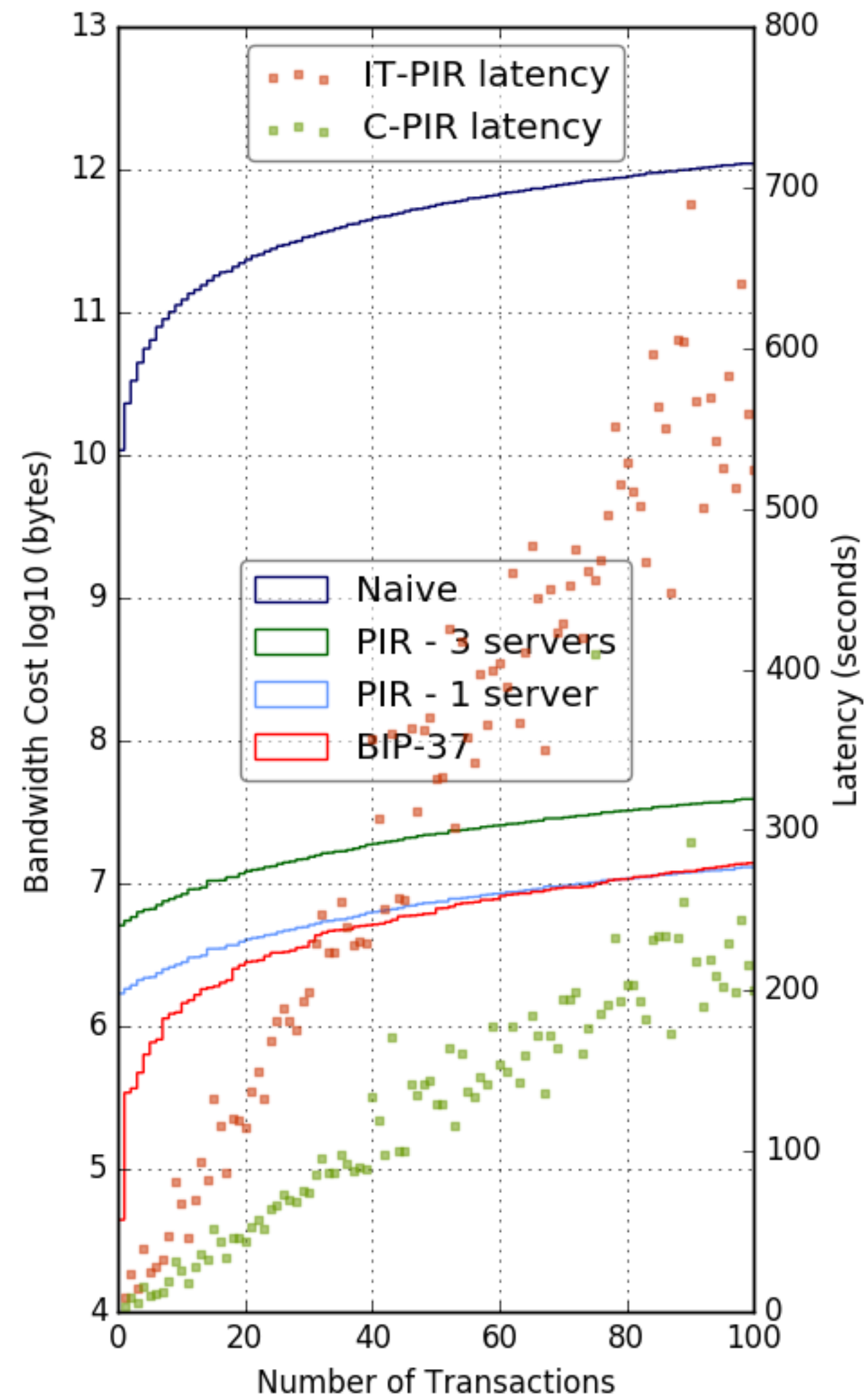


(c) Weekly

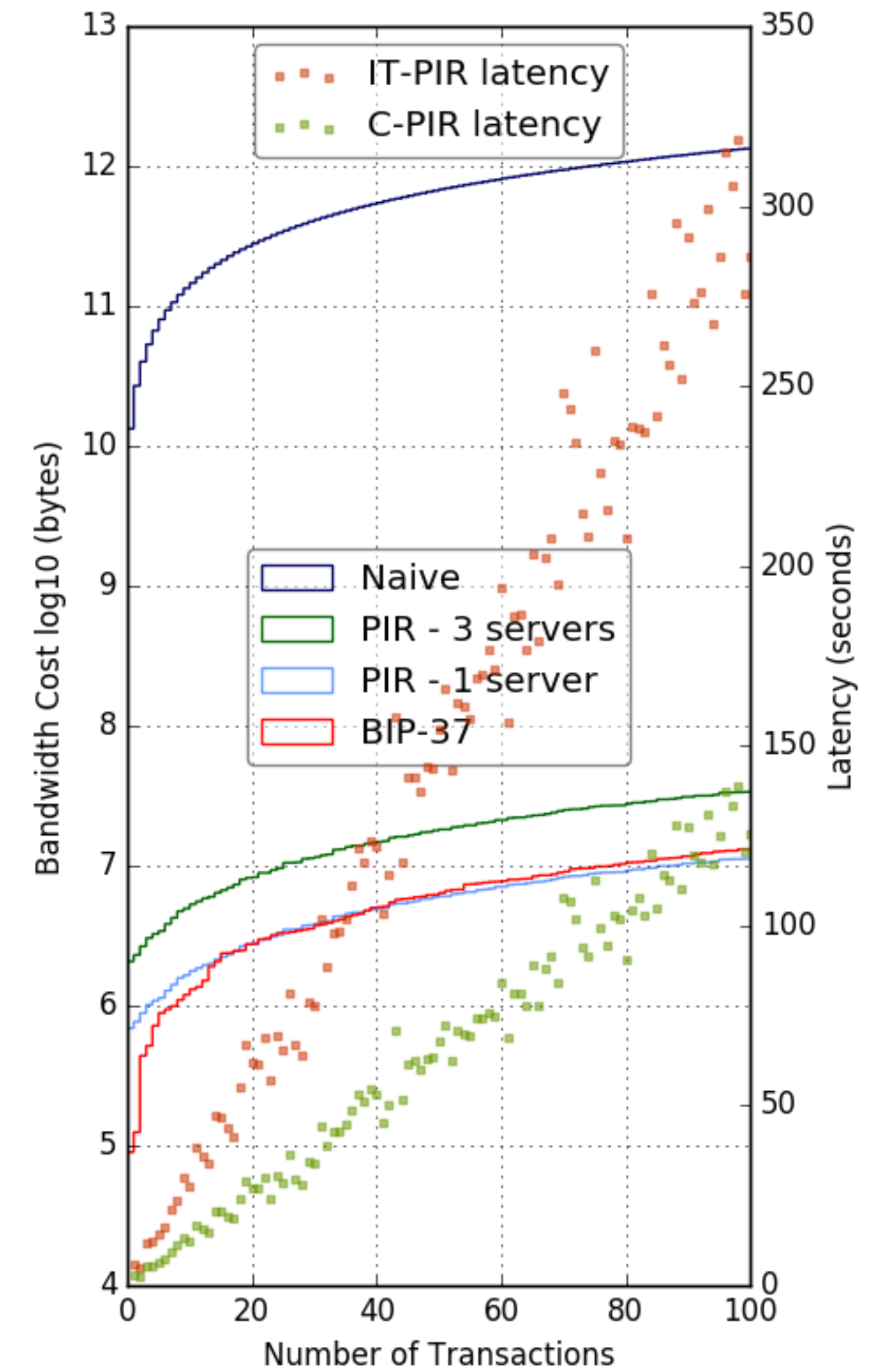
# Cumulative distribution of bandwidth costs to verify a single transaction



(a) All-Time



(b) Monthly



(b) Weekly

## Further Improvements

- ◆ Interpolative Search to skip manifest files
- ◆ More fine granular separation of databases



**Thank you!**

## Manifest Files

- Format

```
{ ...  
  "address" / "block-height" / "txid" : [  
    "row index start",  
    "row index end",  
    "column index start",  
    "column index end",  
  ]  
  ... }
```

- Manifest File Trie Scheme

- In some cases, manifest files have a nearly equivalent or even larger size compared with the database. This may incur a poor performance in bandwidth.
- Transform the simple manifest files into a format suitable for PIR queries.
- Clients perform interpolation search on these manifest files, under PIR



## Protocol

- **Data:** SPV client  $C$ , one or multiple PIR servers  $S$
- **Result:**  $C$  obtains the necessary data for a SPV privately
- **Initialization:**  $S$  constructs the PIR databases and associated manifest files;  $C$  downloads the manifest files from  $S$ ;

### a. Query the Address PIR DB

1.  $C$  selects an address to fetch a record from the Address PIR DB manifest file and generates the PIR queries based on row indices of the selected record;
2.  $S$  computes the result using the PIR queries on the Address PIR DB;
3.  $C$  parses and decodes the result to obtain one or more Address PIR DB entries;

### b. Query the Merkle Tree PIR DB

1.  $C$  uses the value of the block height field of an entry to fetch the corresponding record from the Merkle Tree PIR DB manifest file and generates the PIR queries based on the row indices;
2.  $S$  computes the result using the PIR queries on the Merkle Tree PIR DB;
3.  $C$  parses and decodes the result to obtain the requested list of TXIDs;

### c. Query Transaction PIR DB

1.  $C$  uses the value of the TXID field from the same entry that was selected in step b.1, to fetch the corresponding record from the Transaction PIR DB manifest file and generates the PIR queries based on the row indices;
2.  $S$  computes the result using the PIR queries on the Transaction PIR DB;
3.  $C$  parses and decodes the result to obtain the requested transaction.

## Evaluation

- Cumulative bandwidth cost required to verify 1~100 transactions
- Latency of PIR-SPV (1-server and 3-servers)
- Weekly
  - Single server PIR-SPV has a similar bandwidth cost to BIP-37 SPV when verifying between 20 and 100 transactions.
  - In particular, if a client is interested in performing single-server PIR SPV on 100 transactions which occurred in the past week, it will take approximately 2 minutes for this query to be executed, with a bandwidth cost of 11.18 MB. In contrast, BIP-37 SPV will require 12.85 MB in the same scenario.
  - Clients who are interested in a smaller number of transactions, such as 20, would incur a bandwidth cost of 8.31 MB in the multi-server setting, with a latency of approximately 62 seconds.
- Monthly
  - In the multi-server setting, a 20-transaction query would incur a bandwidth cost of 12.20 MB with a latency of approximately 2.3 minutes.
- All-time
  - Cost is relatively high, but all-time queries are infrequent.